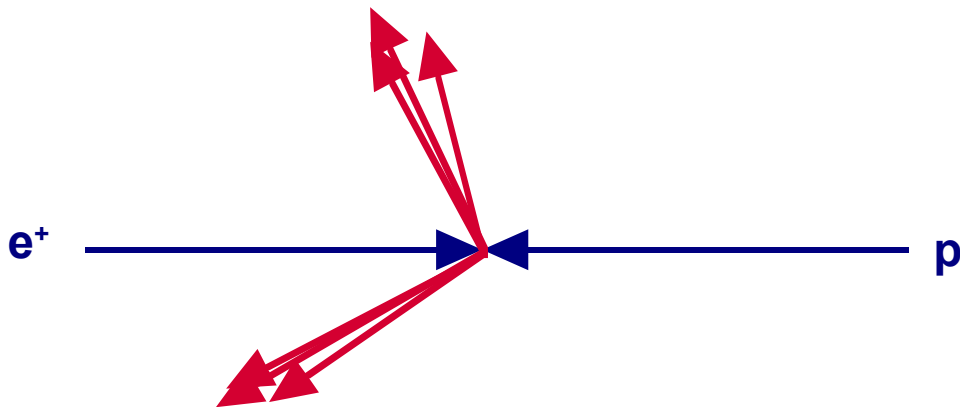


Preliminary Examination

Measurement of DiJet Cross Sections in
Deep Inelastic Scattering at ZEUS



Doug Chapin

University of Wisconsin

20 December 1996

DiJet Cross Sections in DIS

HERA

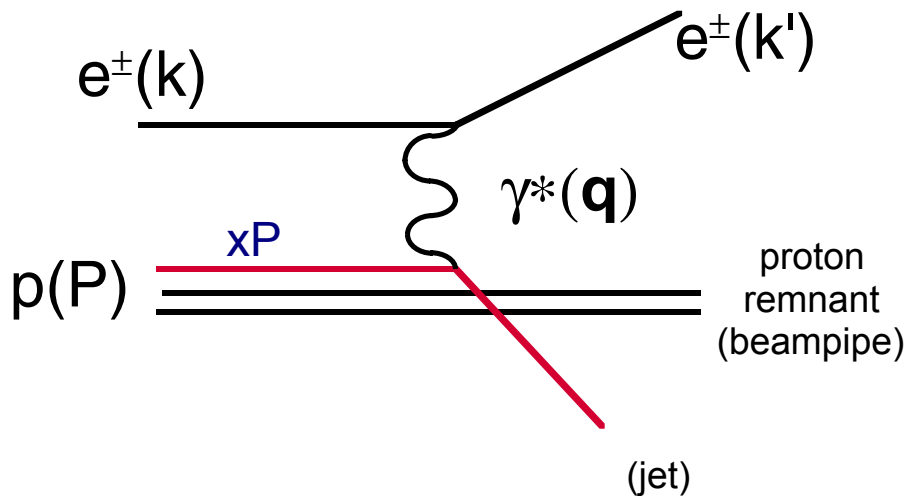
● electron proton collider

- ◆ 820 GeV protons
- ◆ 27 GeV electrons or positrons
- ◆ center of mass energy = 300 GeV
 - ◆ equivalent to a 51 TeV fixed target
- ◆ 220 bunches, 96 ns crossing time
- ◆ $L = 1.5 \times 10^{31} \text{ cm}^{-2}\text{s}^{-1}$ (1.0×10^{31} this year)
- ◆ e^+ current 58mA (40mA) p current 160mA (70mA)



DiJet Cross Sections in DIS

Deep Inelastic Scattering



$$s = (P + k)^2 = 4E_p E_e = (300 \text{ GeV})^2$$

$$Q^2 = -q^2 = -(k - k')^2 = sxy$$

the scale at which the proton is probed is proportional to $1/Q$

$$x_{bj} = \frac{Q^2}{2P \cdot q}$$

fraction of the proton's momentum carried by the struck quark

$$y = \frac{P \cdot q}{P \cdot k}$$

fraction of the electron's energy transferred to the struck quark in the proton's rest frame

DIS Cross Section

The differential cross section for photon exchange is:

$$\frac{d\sigma^2(ep \rightarrow eX)}{dxdy} = \frac{4\pi s \alpha_{em}^2}{Q^4} \left[\left(1 - y + \frac{y^2}{2}\right) F_2(x, Q^2) - \frac{y^2}{2} F_L(x, Q^2) \right]$$

α_{em} is the electromagnetic coupling constant

The structure function $F_2(x, Q^2)$ gives the interaction between transversely polarized photons and spin 1/2 partons. F_2 depends on the quark distributions of the proton.

The structure function $F_L(x, Q^2)$ gives the interaction due to longitudinally polarized photons that interact with the proton. The partons that interact have transverse momentum.

Scaling Violation

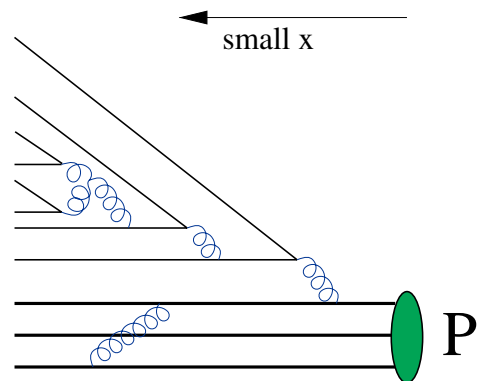
● Naive parton model

- ◆ No parton - parton interactions
- ◆ Partons have no transverse momentum
- ◆ F_2 is only a function of x
- ◆ Bjorken Scaling

But scaling is violated...

Parton-Parton interactions, mediated by the **gluons**, generate parton transverse momentum.

The structure functions gain a Q^2 dependence.



Parton Distribution Functions

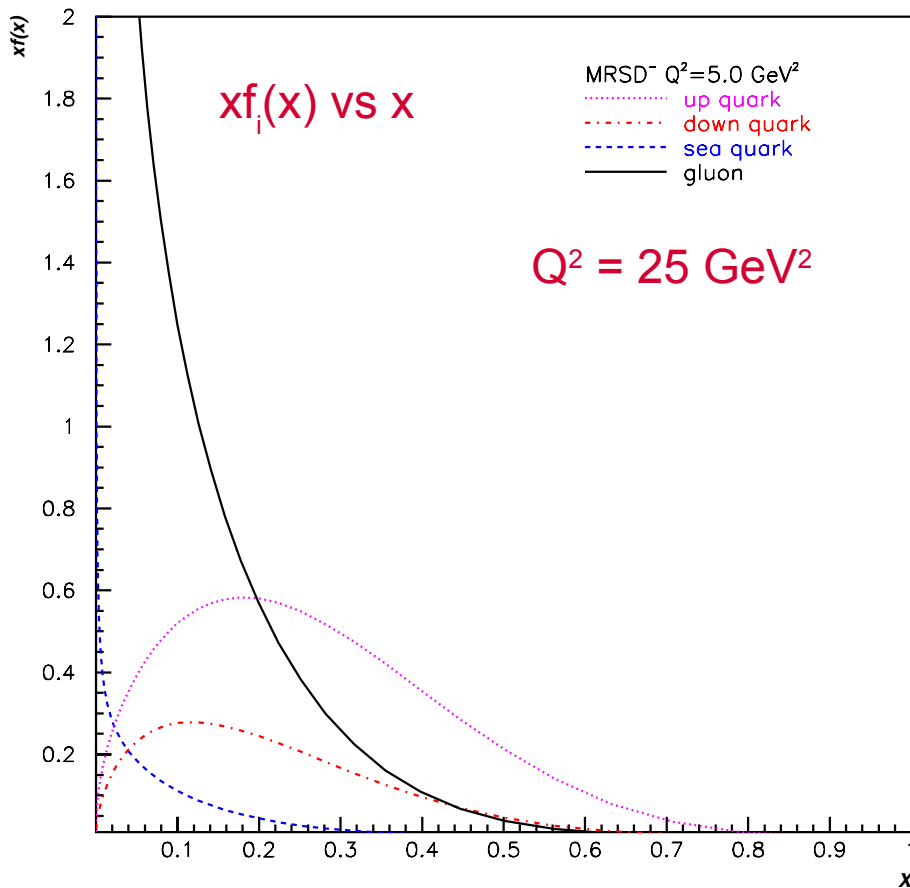
$$f_i = f_i(x, Q^2)$$

$$i = q, \bar{q}, g$$

average number of partons
of type i with momentum
fraction between x and dx

The distribution functions are not calculated by theory. They must be determined from experiment.

Parton Distribution Functions



DiJet Cross Sections in DIS

Extracting Gluon Density From F_2

$$\frac{d\sigma^2(ep \rightarrow eX)}{dxdy} = \frac{4\pi s \alpha_{em}^2}{Q^4} \left[\left(1 - y + \frac{y^2}{2}\right) F_2(x, Q^2) - \frac{y^2}{2} F_L(x, Q^2) \right]$$

$$F_2(x, Q^2) = x \sum_q Q_q^2 f_q(x, Q^2)$$

F_L depends on the gluon density.

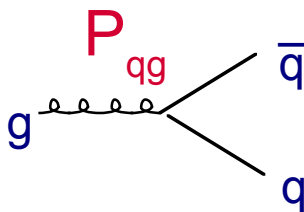
● F_2 measurement

- ◆ measure experimentally the differential cross section
- ◆ estimate F_L from QCD

QCD predicts: (Altarelli-Parisi)

$$\frac{\partial F_2(x, Q^2)}{\partial \ln Q^2} = \frac{\alpha_s(Q^2)}{2\pi} \left[2 \sum_q Q_q^2 \int_x^1 \frac{dw}{w} \left(\frac{x}{w}\right) P_{qg}\left(\frac{x}{w}\right) w g(w, Q^2) + \int_x^1 \frac{dw}{w} \left(\frac{x}{w}\right) P_{qq}\left(\frac{x}{w}\right) F_2(w, Q^2) \right]$$

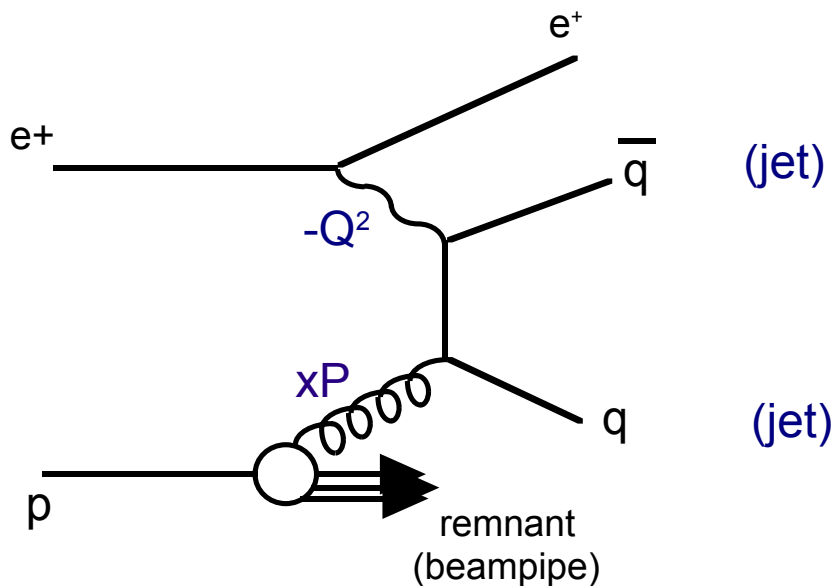
α_s is the strong coupling constant



related to the probability of $g \rightarrow qq$

Dijet Process

Boson Gluon Fusion



$$x = x_{bj} \left(1 + \frac{M_{jj}^2}{Q^2} \right)$$

M_{jj}^2 is the invariant mass squared of the dijet system

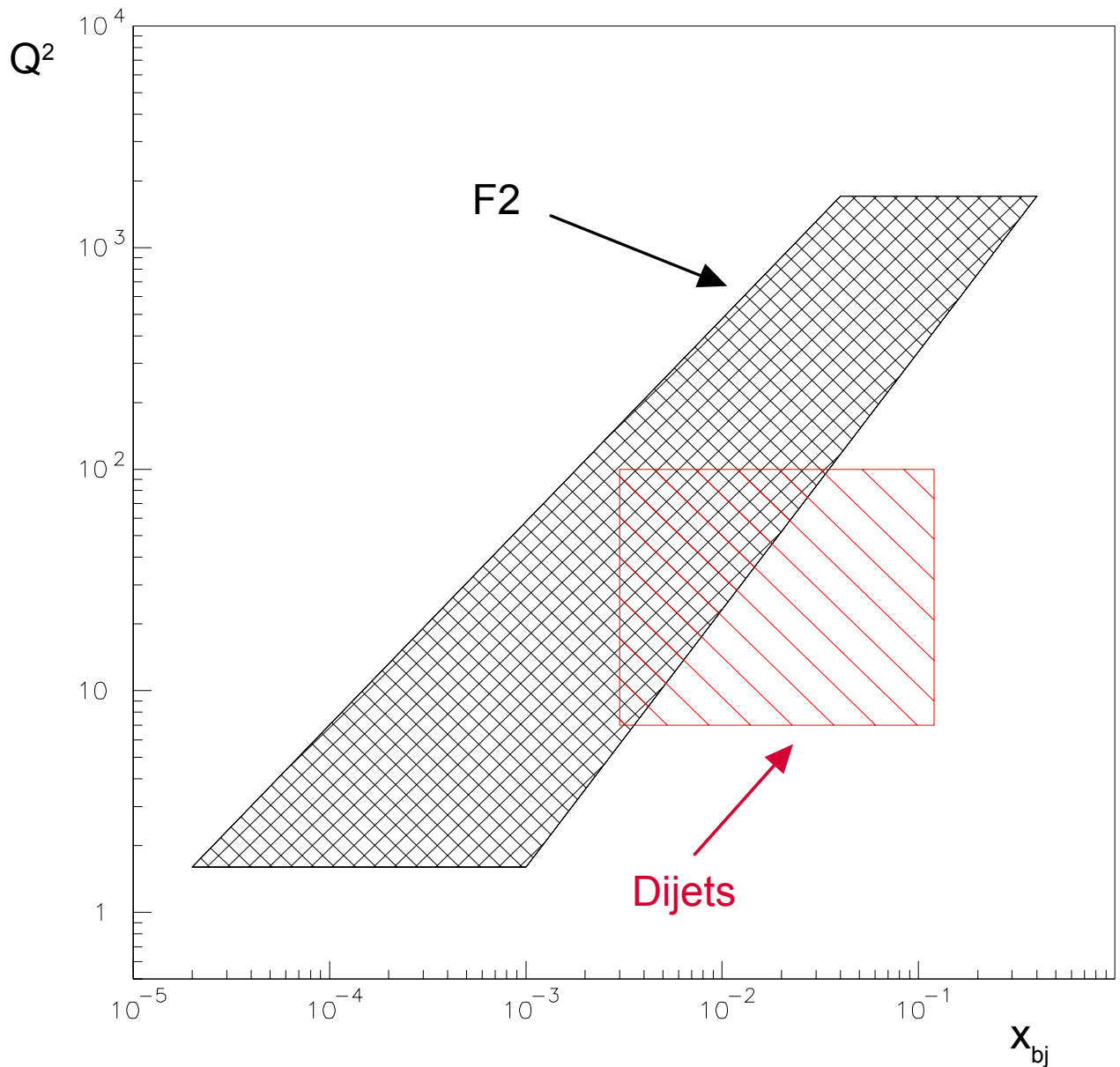
Rate depends directly on the gluon density in the proton.

At what scale is the proton probed in this process?

for $M_{jj}^2 \gg Q^2$, then use p_T of the jets

for $M_{jj}^2 \approx Q^2$, then use Q

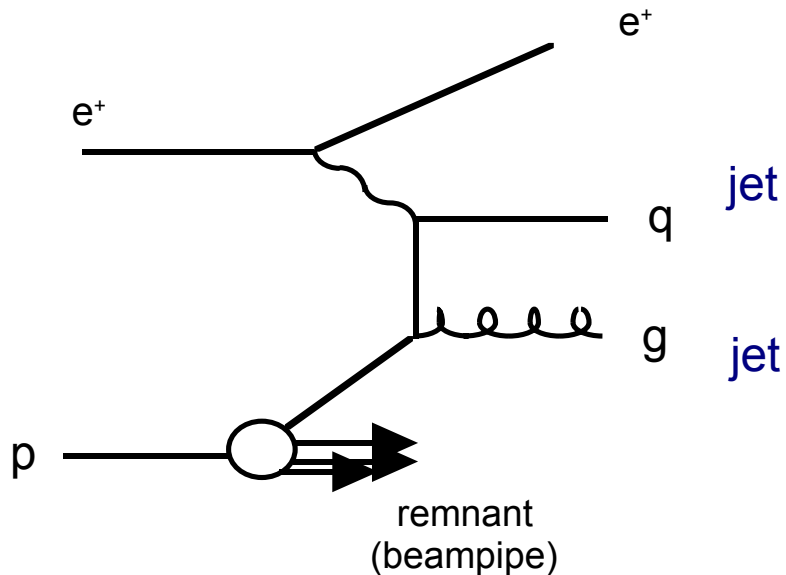
Kinematic Range



DiJet Cross Sections in DIS

Background Process

QCD Compton



For low x this process is dominated by the Boson Gluon Fusion process.

Getting at the Gluon via Dijets

Leading Order

$$\begin{aligned}\sigma_{dijet} &\approx \sigma_{BGF} + \sigma_{QCDC} & x &= x_{bj} \left(1 + \frac{M_{jj}^2}{Q^2}\right) \\ &\approx \hat{\sigma}_g(x)g(x, \mu^2) + \hat{\sigma}_q(x)f_q(x, \mu^2)\end{aligned}$$

$$g(x, \mu^2) \approx \frac{\sigma_{dijet}(x) - \hat{\sigma}_q(x)f_q(x, \mu^2)}{\hat{\sigma}_g(x)}$$

$f_q(x, \mu^2)$ and $g(x, \mu^2)$ are the densities of the quarks and gluons respectively. $f_q(x, \mu^2)$ from other experiments must be used.

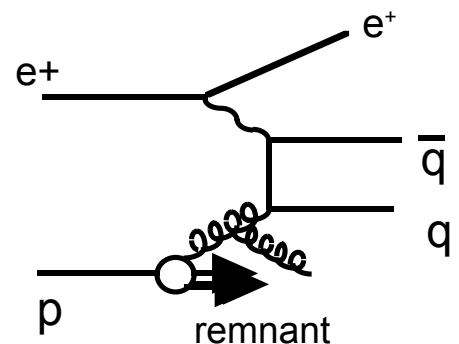
$\hat{\sigma}_q$ and $\hat{\sigma}_g$ are the partonic cross sections for processes initiated by the quarks and gluons respectively. They must be calculated by theory.

μ^2 is the scale at which the proton is probed. It is also called the factorization scale.

NLO

$$\hat{\sigma}(x) \rightarrow \hat{\sigma}(x, \mu^2)$$

NLO calculations reduce dependency on the factorization scale.



Selecting Scale

- **renormalization scale** $\alpha_s(\mu_r^2)$
 - ◆ scale at which the running coupling constant α_s is evaluated
- **factorization scale** $f_i(x, \mu_f^2)$
 - ◆ scale at which the parton densities are evaluated

$$\mu_f^2 = \mu_r^2 = \mu^2$$

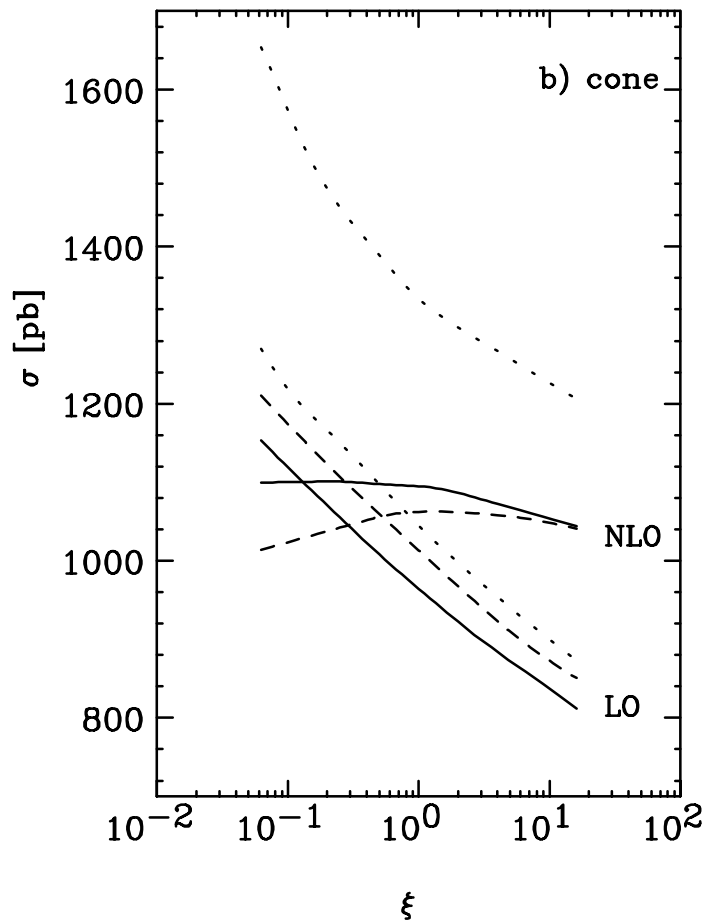
dijet choices:

$$Q^2, p_t^2, k_t^2, ???$$

$$\mu^2 = \xi Q^2$$

$$\mu^2 = \xi p_t^2$$

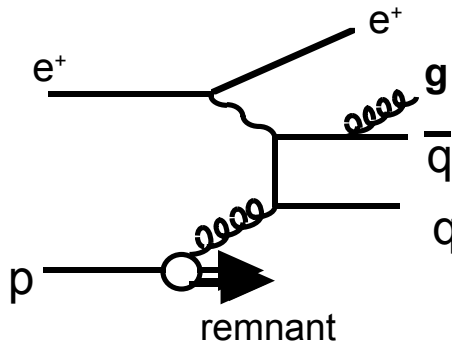
$$\mu^2 = \xi k_t^2$$



DiJet Cross Sections in DIS

Other Concerns

● final state recombination



- ◆ Jet definitions can be sensitive to the recombination scheme used.
- ◆ A large effect on the cross section is possible.

● calculated cross section and detector measured cross section comparison

- ◆ fragmentation of partons into hadrons
- ◆ detector acceptances

Monte Carlo Generators

- **generate events at parton level**
 - ◆ inputs: parton distributions and scale
- **kinematic cuts**
- **jet finding**

Two NLO programs exist: MEPJET and DISENT

They differ in the methods of handling:

renormalization

factorization

final state recombination

Previous Dijet Gluon Results

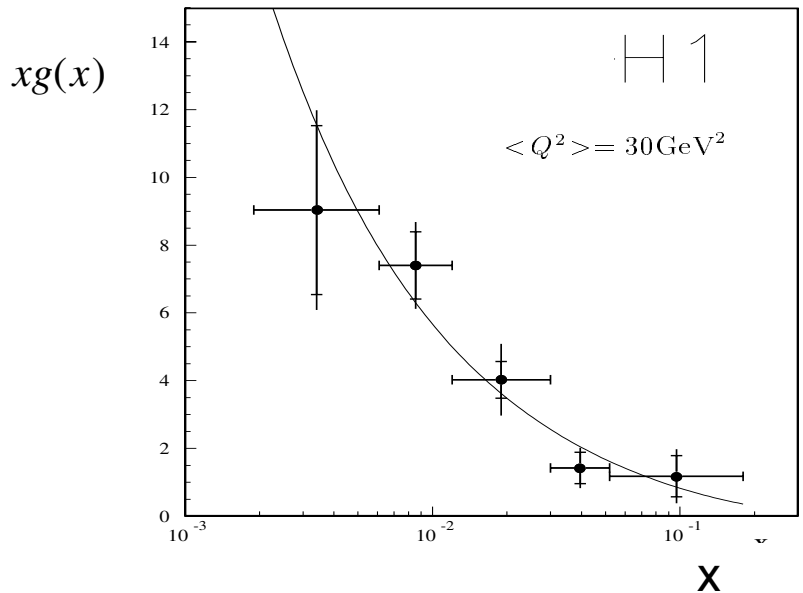
LO

1993 H1 data

MC used: LEPTO

scale used: Q^2

results compatible
with previous F_2
measurements



NLO

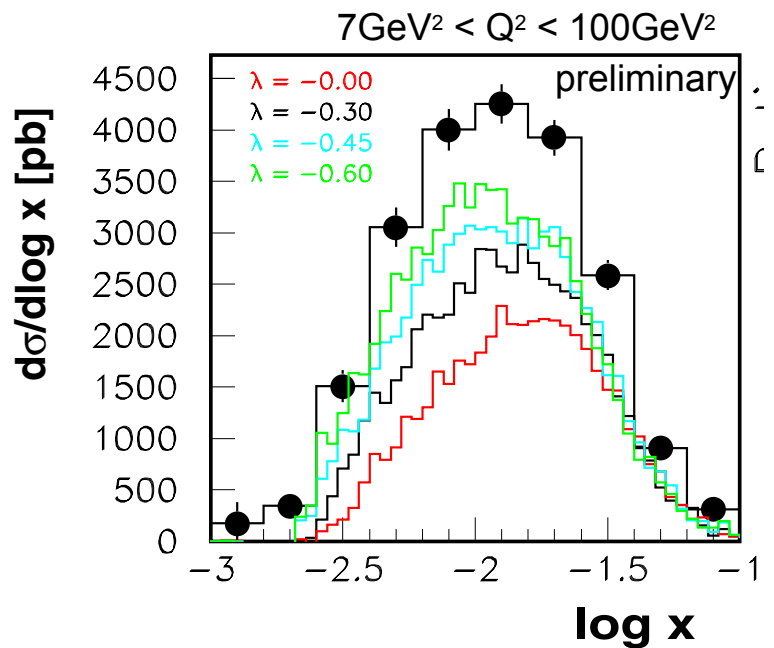
1994 ZEUS data

$$xg(x, \mu_0^2) \propto x^\lambda$$

measure λ

MC used: MEPJET

scale used: Q^2



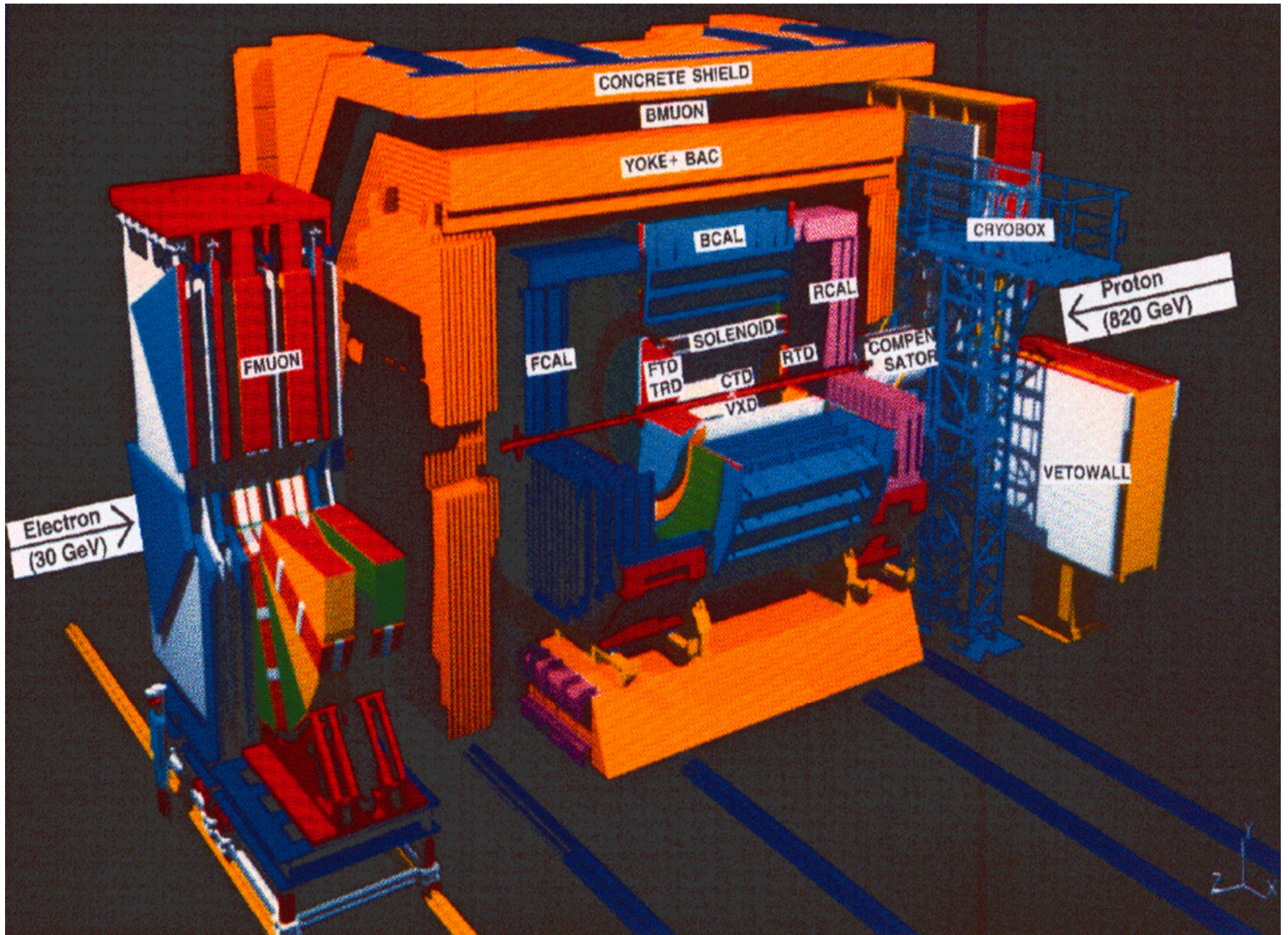
DiJet Cross Sections in DIS

Physics Motivation

proton structure

- 50% of the proton's momentum is carried by gluons
- the F_2 method is an indirect measurement of the gluon density
- the dijet cross section is directly proportional to the gluon density of the proton
- dijet method is sensitive in an extended region of x - Q^2

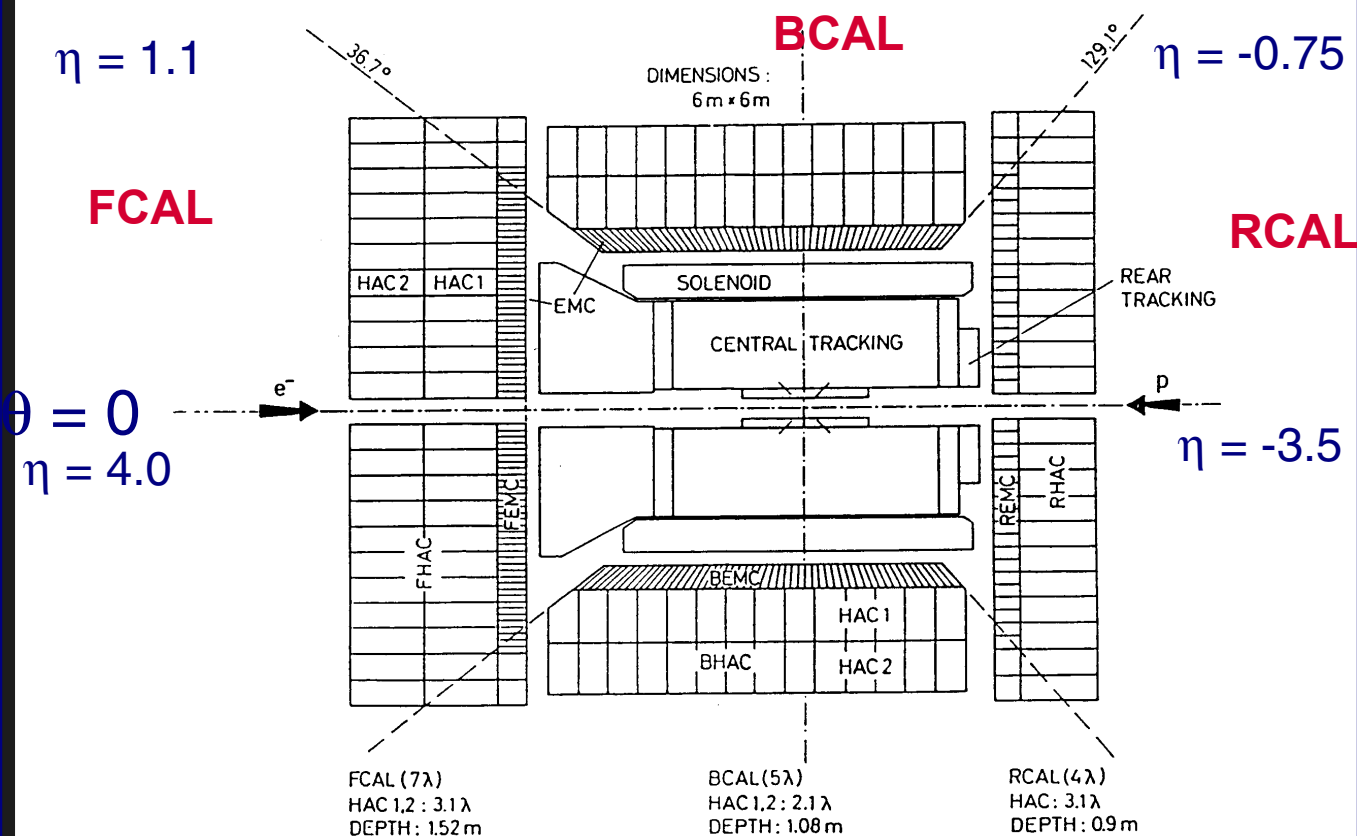
ZEUS



Calorimeter

- **depleted uranium and scintillator**

- ◆ 99.7% solid angle coverage
- ◆ electron res: $18\%/\sqrt{E}$ hadronic res: $35\%/\sqrt{E}$

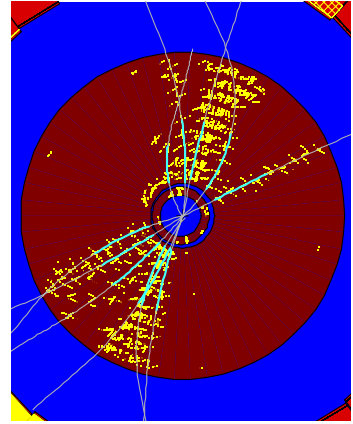


$$\eta = -\ln\left[\tan\left(\frac{\theta}{2}\right)\right]$$

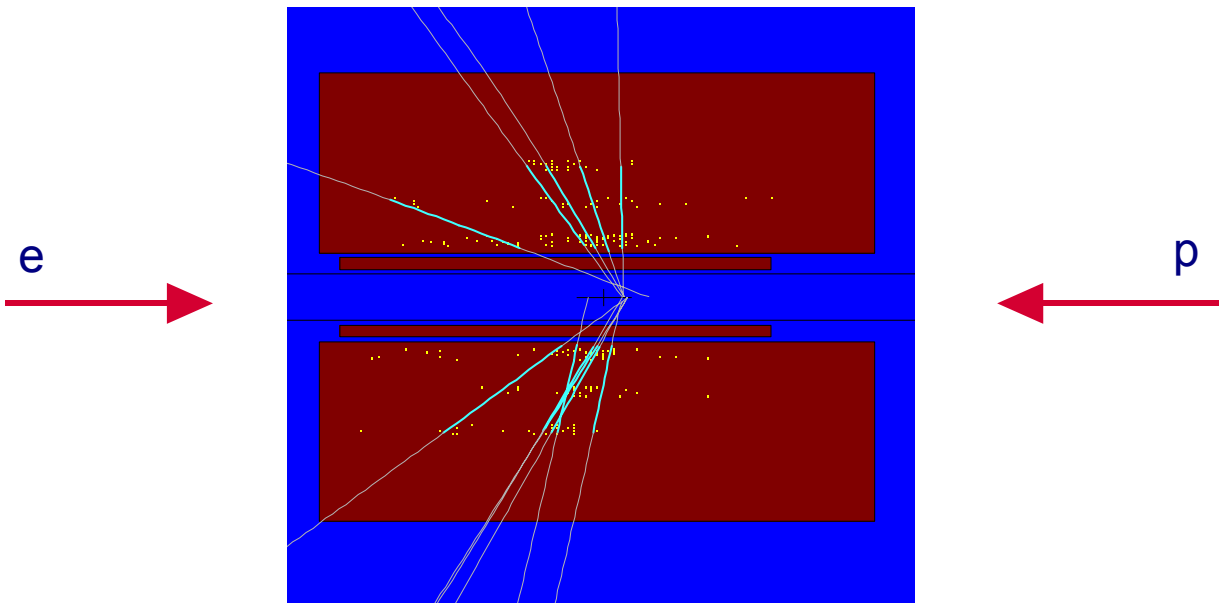
DiJet Cross Sections in DIS

Central Tracking Detector

- drift chamber
- 1.43T solenoid
- vertex resolution
 - ◆ 1mm transverse
 - ◆ 4mm in z



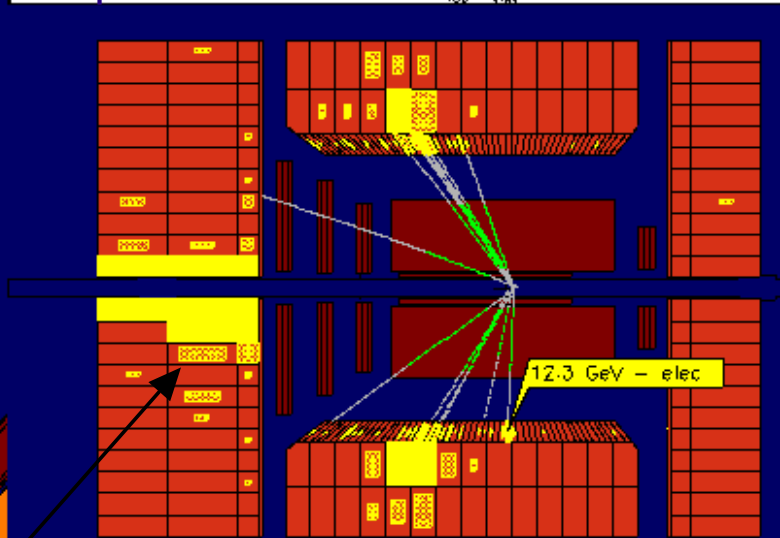
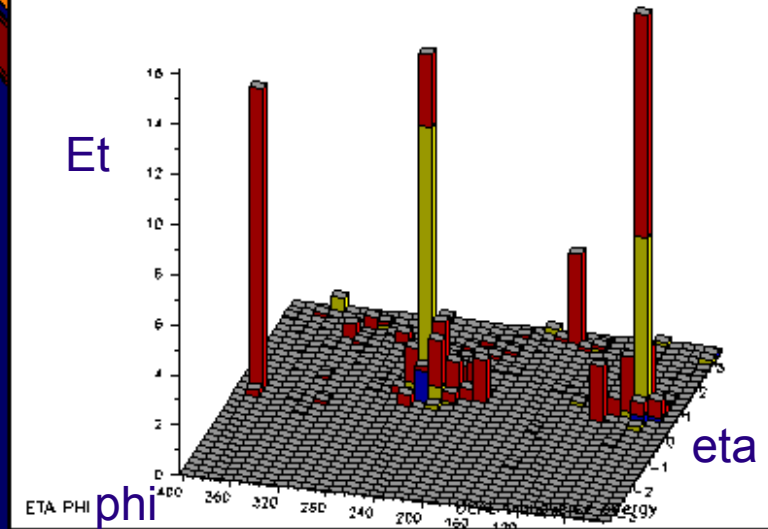
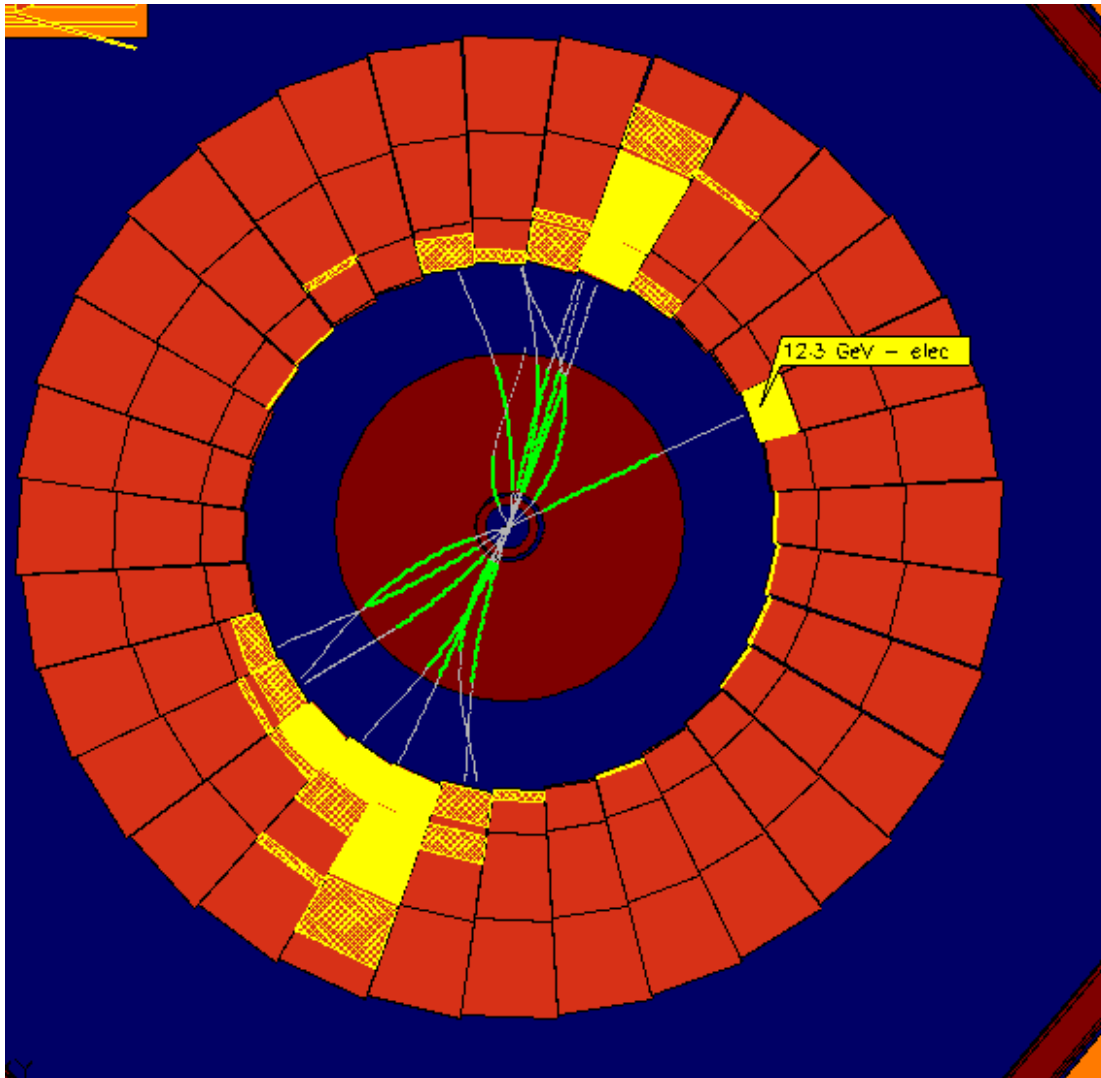
transverse view



side view

DiJet Cross Sections in DIS

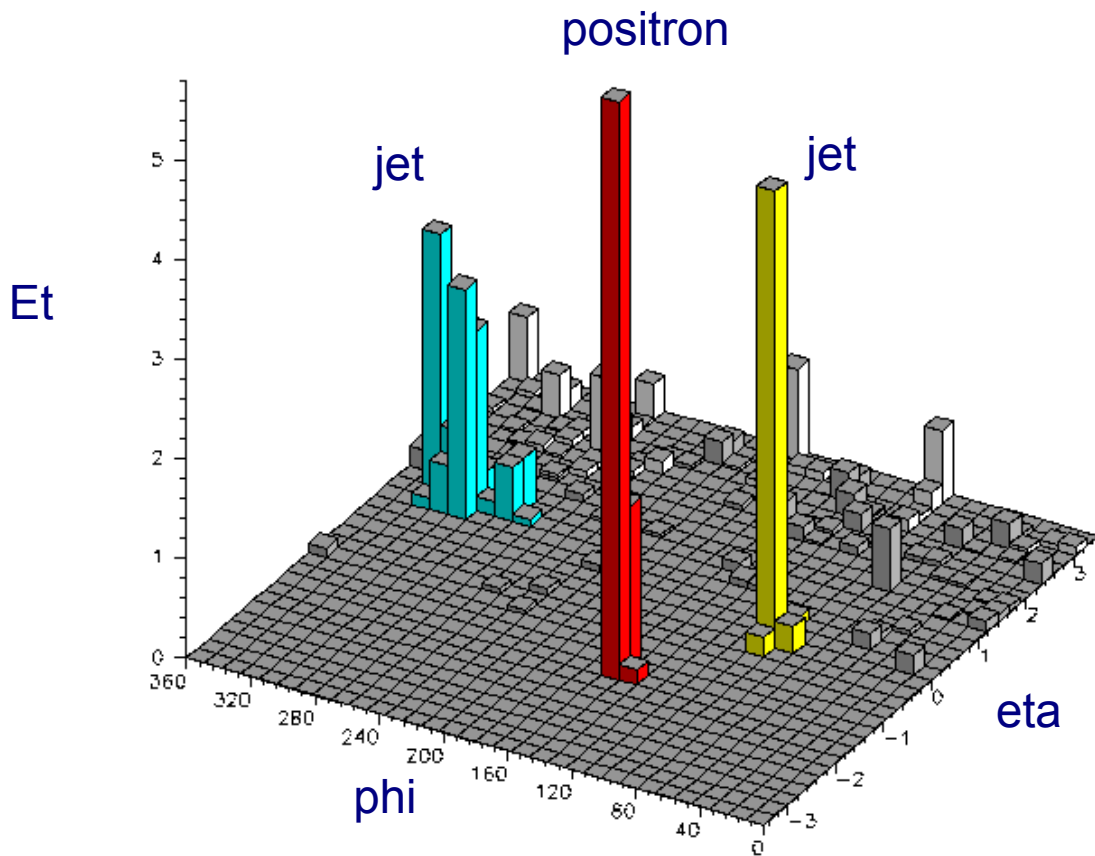
DIS DIJET EVENT



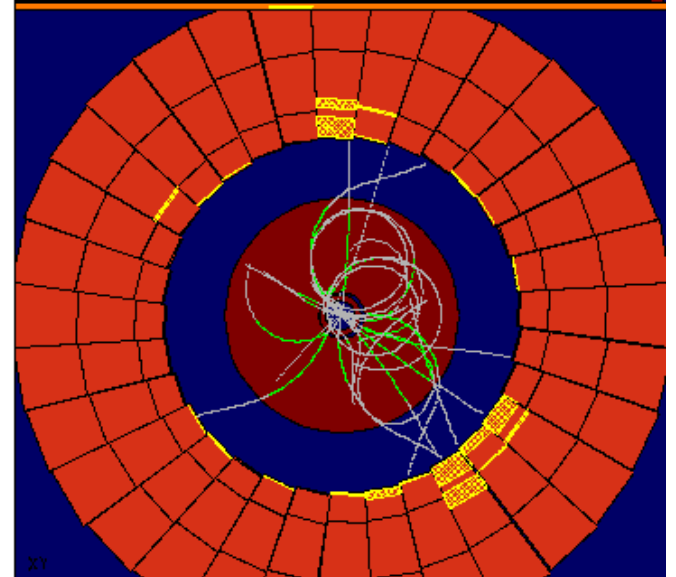
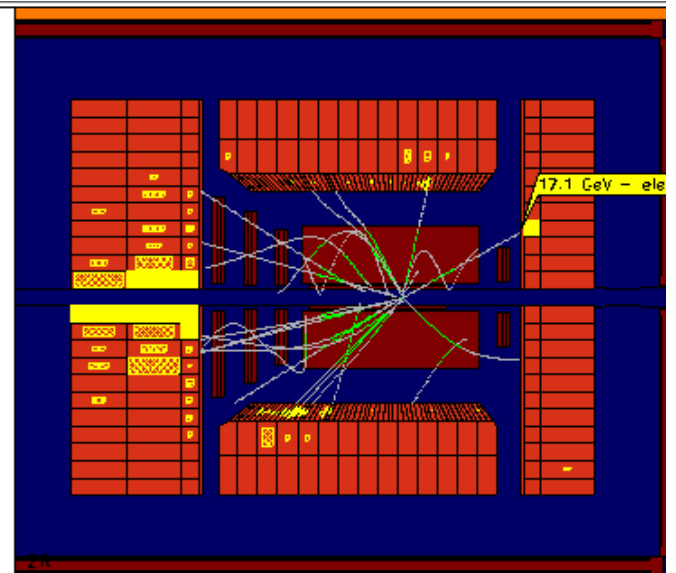
proton remnant

e \longrightarrow \longleftarrow p

DIS DIJET EVENT $Q^2=100 \text{ GeV}^2$



Eta Phi Cone Jets



UCAL transverse energy

Trigger

10^7 crossings/sec

10^5 Hz background rate

10 Hz physics rate



FLT

● First level

- ◆ dedicated hardware
- ◆ no deadtime
- ◆ global and regional energy sums
- ◆ isolated electron and muon recognition
- ◆ tracking information

400 Hz



SLT

● Second level

- ◆ timing cuts
- ◆ e- p_z
- ◆ simple physics filters
- ◆ electron finding
- ◆ additional tracking information

40 Hz



TLT

● Third level

- ◆ full event information available
- ◆ advanced physics filters
- ◆ jet and electron finding

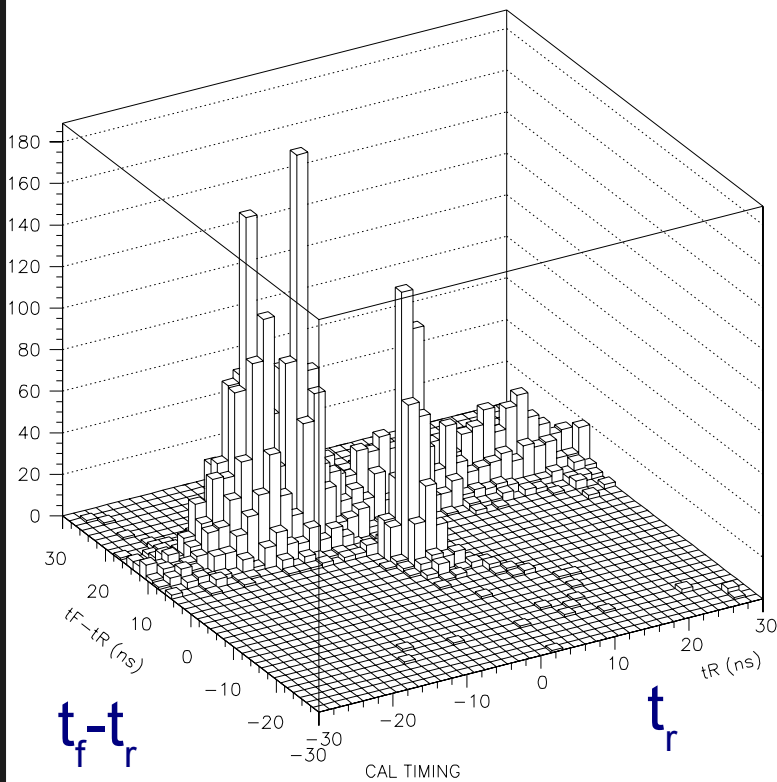
14 Hz



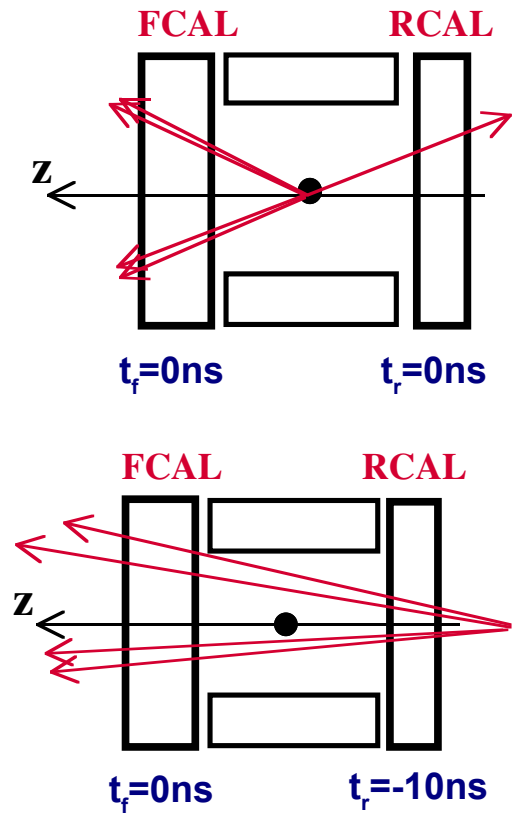
mass storage

100kBytes/event

Timing and $E-P_z$



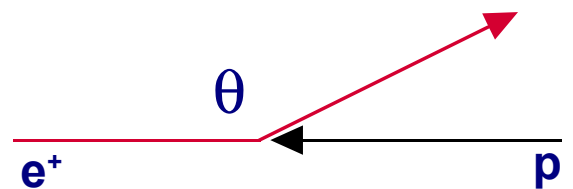
**calorimeter timing
resolution < 1ns**



$$E - P_z = \sum_{\text{cells}} E(1 - \cos \theta)$$

Initially:

$$E_p - E_{pz} + E_e - (-E_{ez}) = 2E_e$$



**measured value is
conserved if no energy
lost down rear beam pipe**

Analysis Plan

- **apply cuts to detector data to select sample of dijet events**
 - ◆ 1996: 10.8 pb^{-1} integrated luminosity
 - ◆ a sample of 50k events are expected after cuts
- **measure cross section from data**
 - ◆ bin events in x
 - ◆ make corrections due to detector acceptances
- **generate Monte Carlo event samples and apply equivalent cuts**
- **compare MC with data**

Cone Jet Identification Algorithm

First finds largest E_t cluster. Then it sums all clusters within

$$R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2} = 1$$

The resulting combination is called a jet and removed.

Stops when the E_t of the summed clusters is less than a specified value.

Lorentz invariant

Good in ZEUS central region, but overefficient in the ZEUS forward region. Proton remnant can be misidentified as a jet.

Currently used in the ZEUS third level trigger

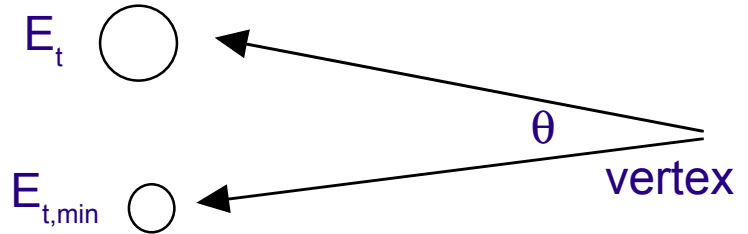
Relatively independent of the MC recombination scheme

Other Jet Identification Algorithms

k_t

First finds largest E_t cluster

$$k_{\perp} = 2E_{t,\min}^2 (1 - \cos \theta)$$



The two clusters with minimum k_{\perp} are found.

If k_{\perp} larger than a threshold value then the largest cluster is called a jet and removed.

Otherwise the two clusters are combined, and the process is repeated.

Good in ZEUS forward region.

Relatively independent of the MC recombination scheme

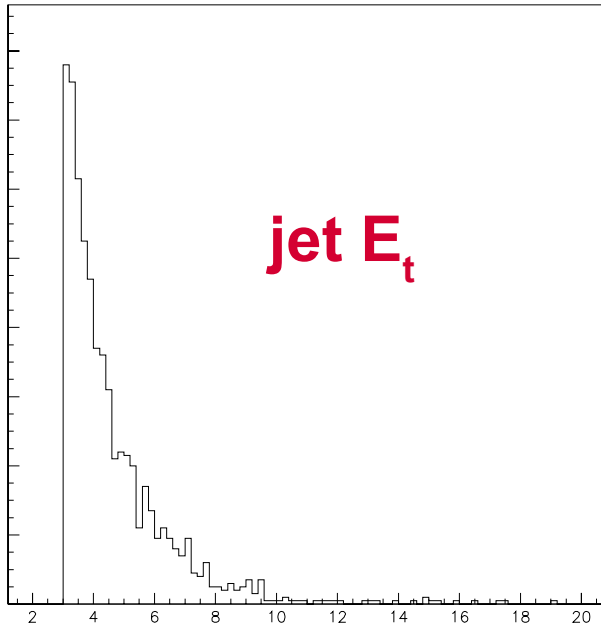
JADE

Similar to k_t , except the relevant quantity is

$$M = 2EE_{\min} (1 - \cos \theta) \quad \text{energy weighted combination}$$

large recombination scheme dependence

Jet Properties

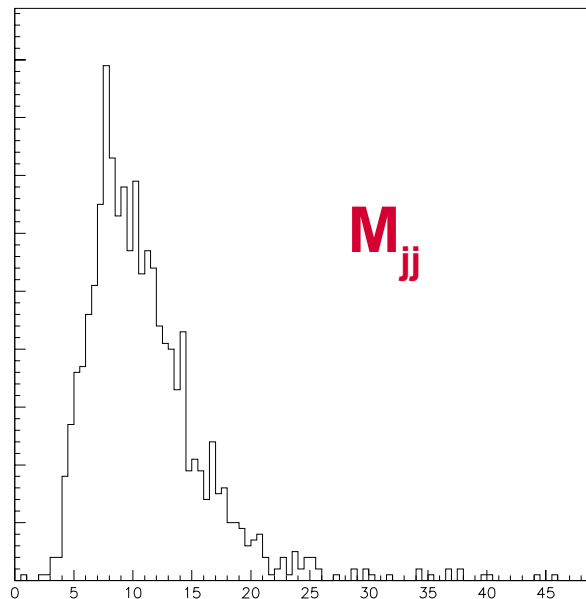


jet $E_t > 3\text{GeV}$

$2.5 < \eta < -3.0$

cone algorithm

Transverse Energy (GeV)



Energy (GeV)

DiJet Cross Sections in DIS

Electron Identification

- **electron signature is**
 - ◆ energy deposit in electromagnetic calorimeter cells
 - ◆ energy contained in a few calorimeter cells
 - ◆ electromagnetic / hadronic energy ratio
- **ZEUS uses several finders**
 - ◆ use electron signature
 - ◆ primary finder is > 95% efficient for electron energy > 10 GeV
- **improvements can be made using additional components-- Small Rear Tracking Detector and the RCAL Presampler**
- **Calorimeter First Level Trigger is 99% efficient for isolated electrons above 5 GeV (RCAL)**

Variable Reconstruction - Electron Method

$$y = 1 - \frac{E'_e}{2E_e}(1 - \cos \theta)$$

θ = positron
scattering angle

E'_e = scattered
positron energy

$$Q^2 = 2E'_e E_e (1 + \cos \theta)$$

$E_e = 27$ GeV

$$x_{bj} = \frac{E'_e(1 + \cos \theta)}{2yE_p}$$

$E_p = 820$ GeV

$$x = x_{bj} \left(1 + \frac{M_{jj}^2}{Q^2}\right)$$

$$M_{jj}^2 = 2E_{jet1}E_{jet2}(1 - \cos \theta_{jets})$$

best x resolution at low Q^2

sensitive to miscalibrations

General Dijet Cuts

- **positron found with $E > 10 \text{ GeV}$**
 - ◆ good efficiency
- **x_{bj} , Q^2 and y determined from electron method**
 - ◆ best resolution
- **$E - P_z > 35 \text{ GeV}$**
 - ◆ selects DIS events
- **$y > 0.04$**
 - ◆ uncertainty is large for small values of y
- **vertex cut $-40\text{cm} < z < 40\text{cm}$**
 - ◆ removes beamgas
- **$7 \text{ GeV}^2 < Q^2 < 100 \text{ GeV}^2$**
 - ◆ BGF dominant below 100GeV^2
 - ◆ above 7GeV^2 positron fully contained in RCAL
- **two jets found by cone algorithm**
 - ◆ $E_t > 3.0 \text{ GeV}$
 - ◆ $-3.0 < \eta < 2.5$

Measurement Uncertainties

● event misidentification

- ◆ photoproduction events (scattered positron goes down rear beampipe)
 - ◆ a particle in a jet may mimic a scattered positron
 - ◆ observed E-Pz is not conserved
- ◆ ~ 1% effect

● y, x_{bj}, Q^2 , and x resolution

- ◆ improvement over 1994 analysis
 - ◆ SRTD and RCAL presampler

● jet energy resolution

- ◆ cross section uncertainty is very sensitive to energy scale uncertainty
- ◆ improvements using tracking information possible

Conclusions

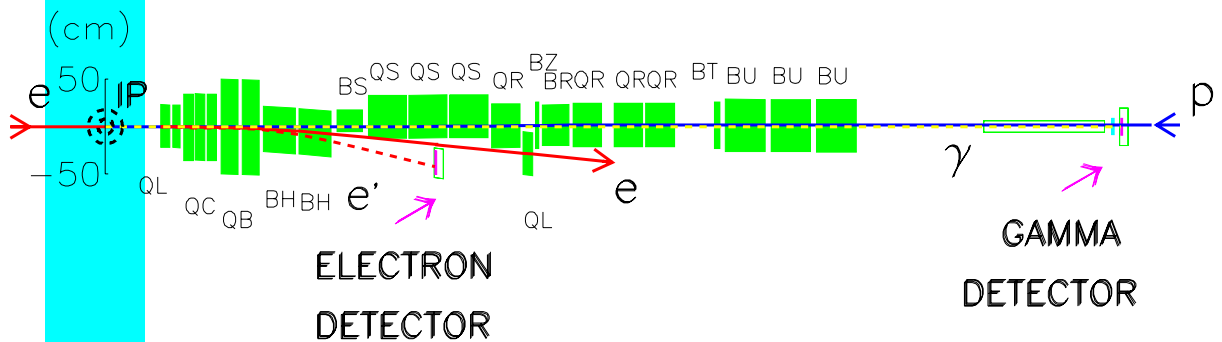
- **measure deep inelastic scattering dijet cross section using 1996 ZEUS data sample**
 - ◆ improved statistics and resolution
 - ◆ 1994: 3.2 pb^{-1}
 - ◆ 1995: 6.3 pb^{-1}
 - ◆ 1996: 10.8 pb^{-1}
- **determination of the gluon density of the proton**
 - ◆ dijet method: complementary measurement to the F_2 method
 - ◆ dijet cross section has direct dependence on gluon density
 - ◆ extended kinematic range

Luminosity Monitor

Luminosity = particles per second per unit area.

Number of events = integrated luminosity X cross section

T U N N E L W A L L



T U N N E L W A L L

uses the known hard Bremsstrahlung ($ep \rightarrow ep\gamma$) cross section

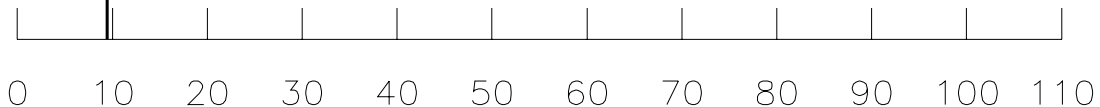
tags the electron and photon in separate Pb/scintillator detectors

resolution = $18\%/\sqrt{E} \oplus 1\%$

luminosity uncertainty < 2%

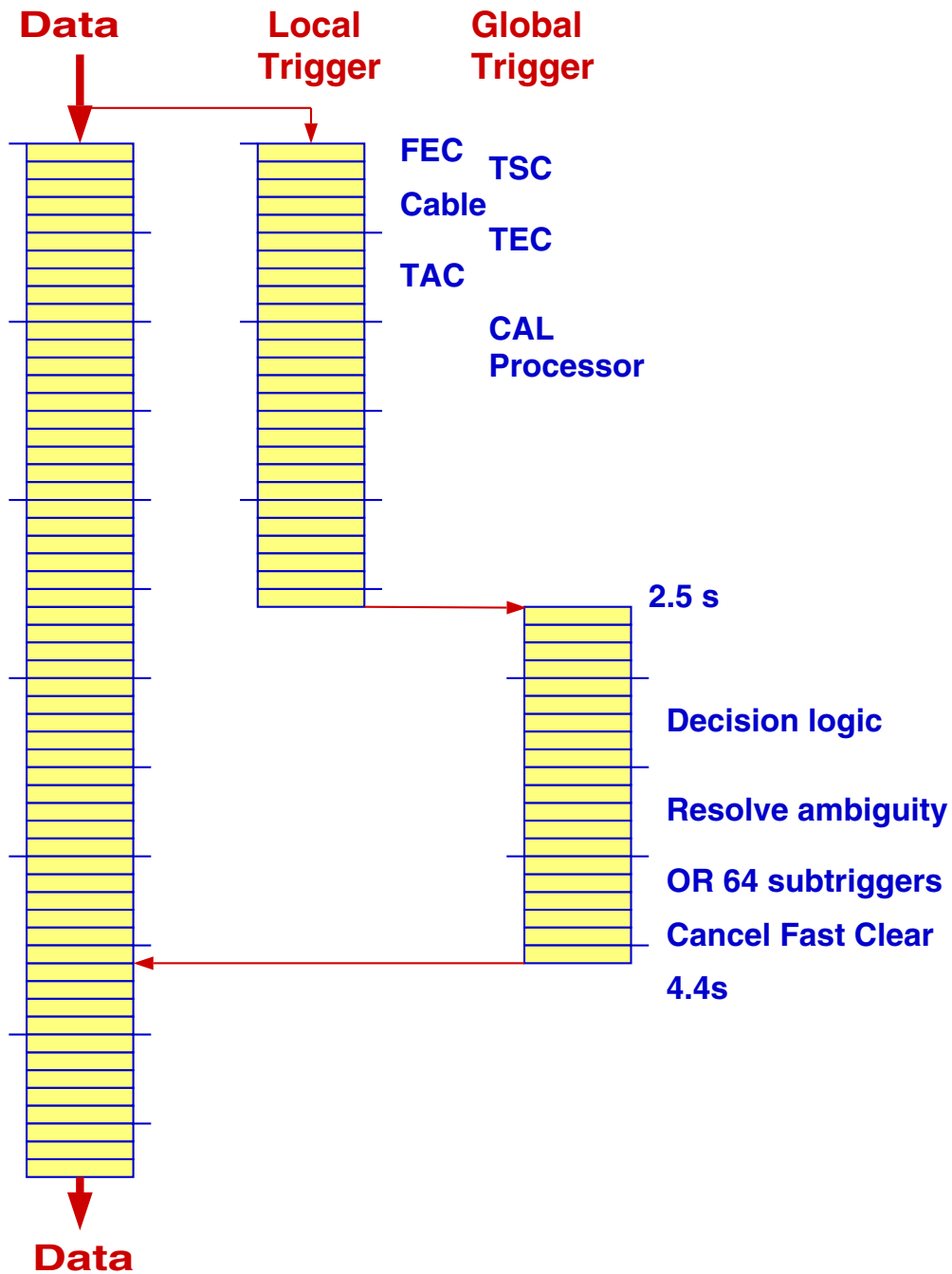
(m)

SOUTH HALL



DiJet Cross Sections in DIS

First Level Trigger



DiJet Cross Sections in DIS

Pseudorapidity

$$\text{rapdity} = \frac{1}{2} \ln \left[\frac{E + p_{\parallel}}{E - p_{\parallel}} \right]$$

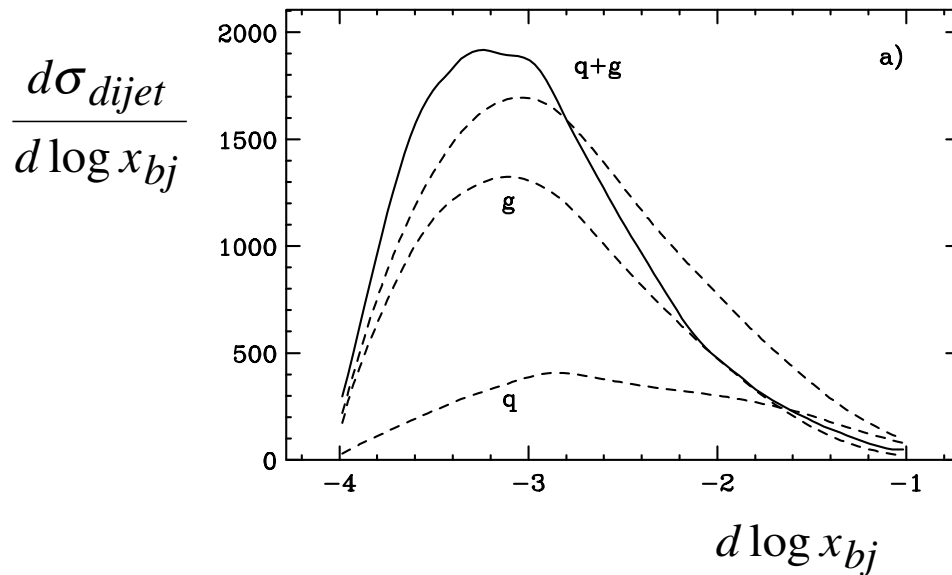
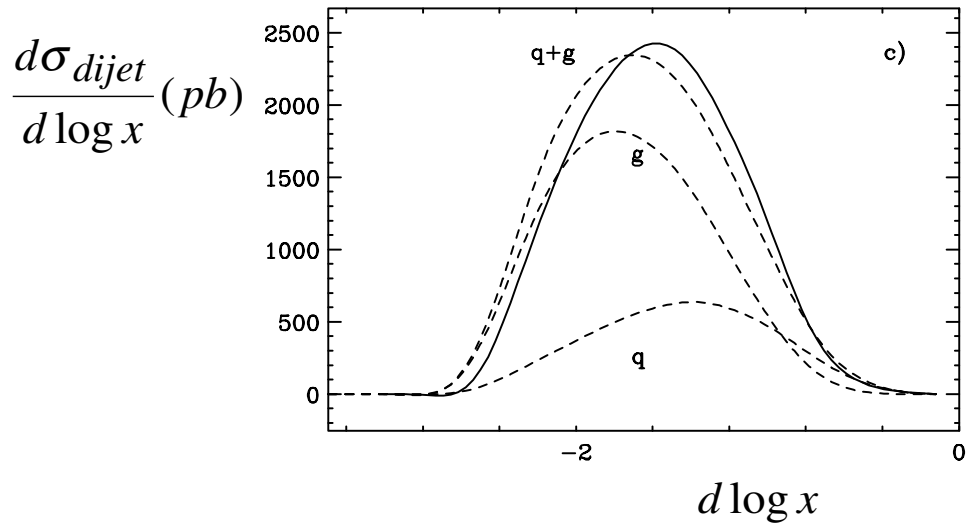
$$\text{psuedorapidity} = \eta = \frac{1}{2} \ln \left[\frac{|p| + p_{\parallel}}{|p| - p_{\parallel}} \right] = -\ln \left(\tan \frac{\theta}{2} \right)$$

Lorentz boost along the beam direction

$$\eta' = \eta + f(v)$$

$\Delta\eta$ **is unaffected**

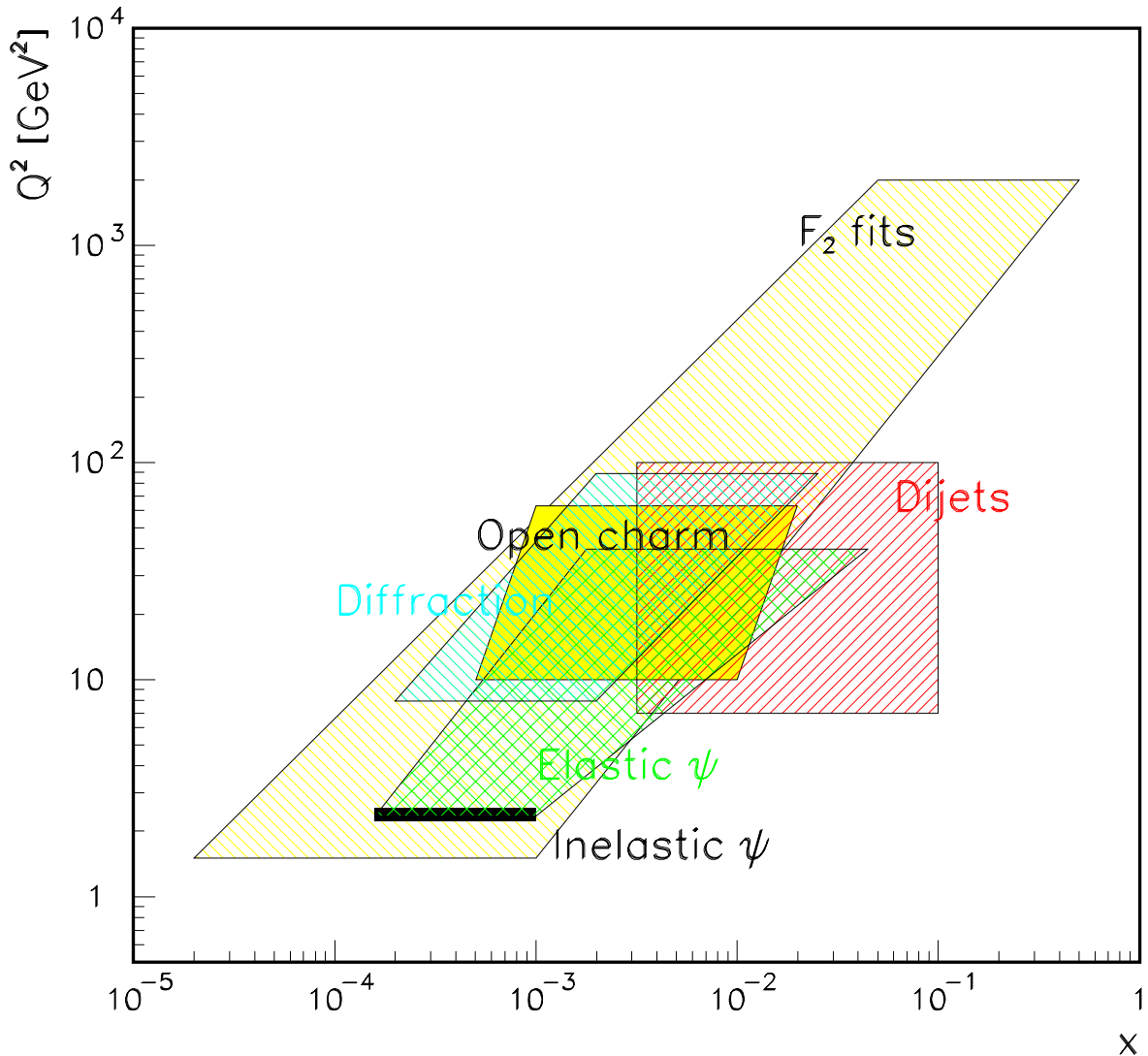
MEPJET Plots



DiJet Cross Sections in DIS

jose range

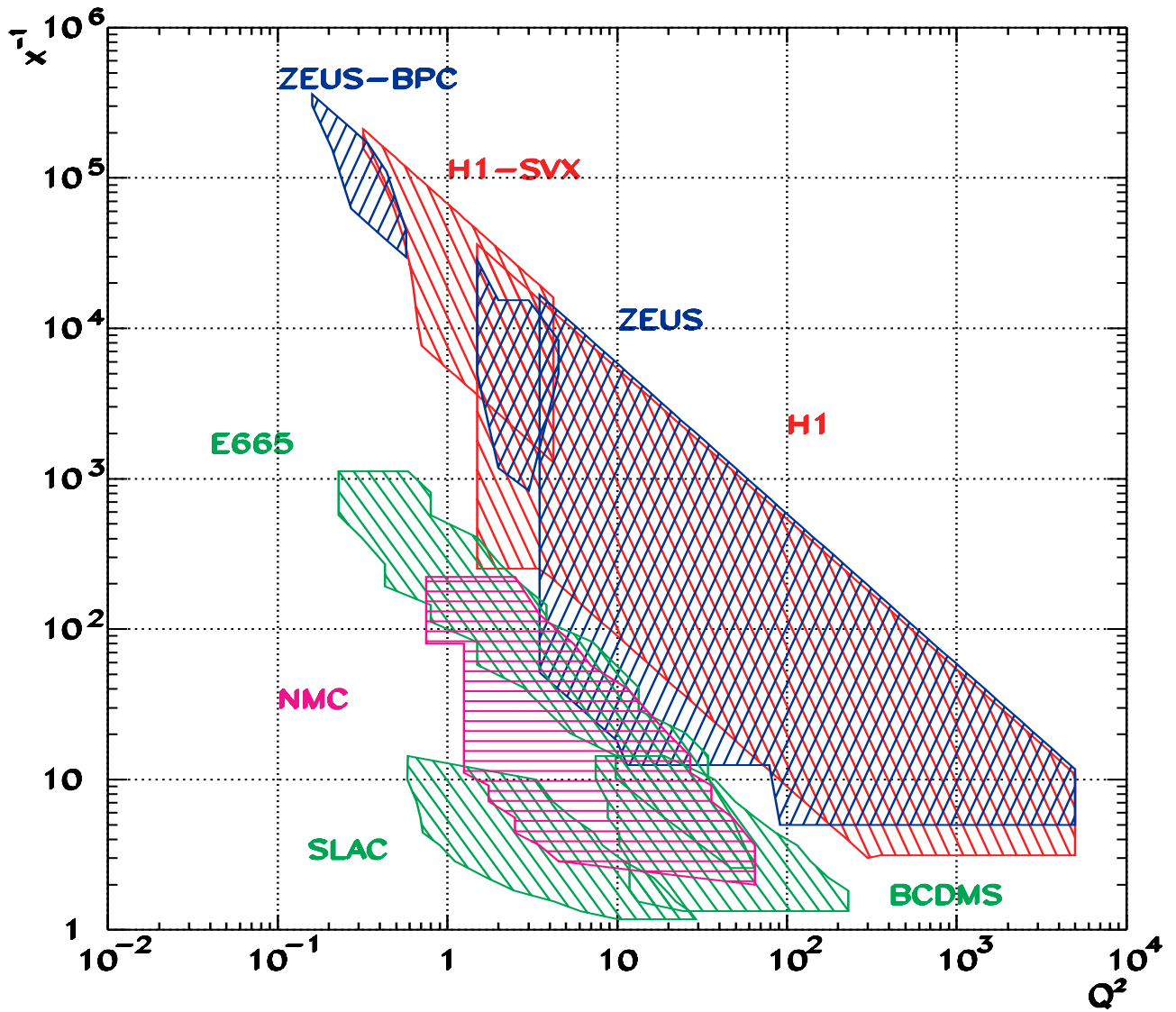
Range in $x-Q^2$



Altarelli-Parisi

DiJet Cross Sections in DIS

wesley kinematic range



DiJet Cross Sections in DIS

Double Angle Method

$$\cos \gamma = \frac{(\sum p_x)^2 + (\sum p_y)^2 - (\sum (E - P_z))^2}{(\sum p_x)^2 + (\sum p_y)^2 + (\sum (E - P_z))^2}$$

characterizes the momentum flow of the hadronic system

$$x_{DA} = \frac{E_e \sin \gamma + \sin \theta + \sin(\gamma + \theta)}{E_p \sin \gamma + \sin \theta - \sin(\gamma + \theta)}$$

$$E_e = 27 \text{ GeV}$$

$$E_p = 820 \text{ GeV}$$

$$Q_{DA}^2 = \frac{4E_e^2 \sin \gamma (1 + \cos \theta)}{\sin \gamma + \sin \theta + \sin(\gamma + \theta)}$$

θ = positron scattering angle

$$y_{DA} = \frac{Q_{DA}^2}{sx_{DA}}$$

$$x = x_{DA} \left(1 - \frac{M_{jj}^2}{Q^2}\right)$$

Depends only on energy ratios so it is less sensitive to energy scale uncertainties.

**better mean resolution over the entire x - Q^2 plane
define m_{jj} here**

junk

$$\frac{\partial f_i(x, Q^2)}{\partial \ln Q^2} = \frac{\alpha_s(Q^2)}{8\pi^2} \sum_j \int_x^1 \frac{dw}{w} P_{ij}\left(\frac{x}{w}\right) f_j(w, Q^2)$$