

# ***QCD Studies in ep Collisions***

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## **Outline:**

- **Introduction**
  - HERA & ep scattering
- **Structure Functions**
  - Parton Model & Scaling Violation
  - $F_2$ : Gluons, charm, total  $\gamma^*P$   $\sigma$
  - High  $Q^2$  NC & CC
- **Jets**
  - Deep Inelastic Scattering (DIS):  $\alpha_s$
  - Photoproduction
    - resolved vs. direct
- **Diffraction**
  - Deep Inelastic Scattering
    - structure of diffractive exchange
  - Photoproduction
    - $\sigma$ 's & jets
- **Vector mesons**
  - Photoproduction & DIS
- **Conclusions**

# *Acknowledgements*

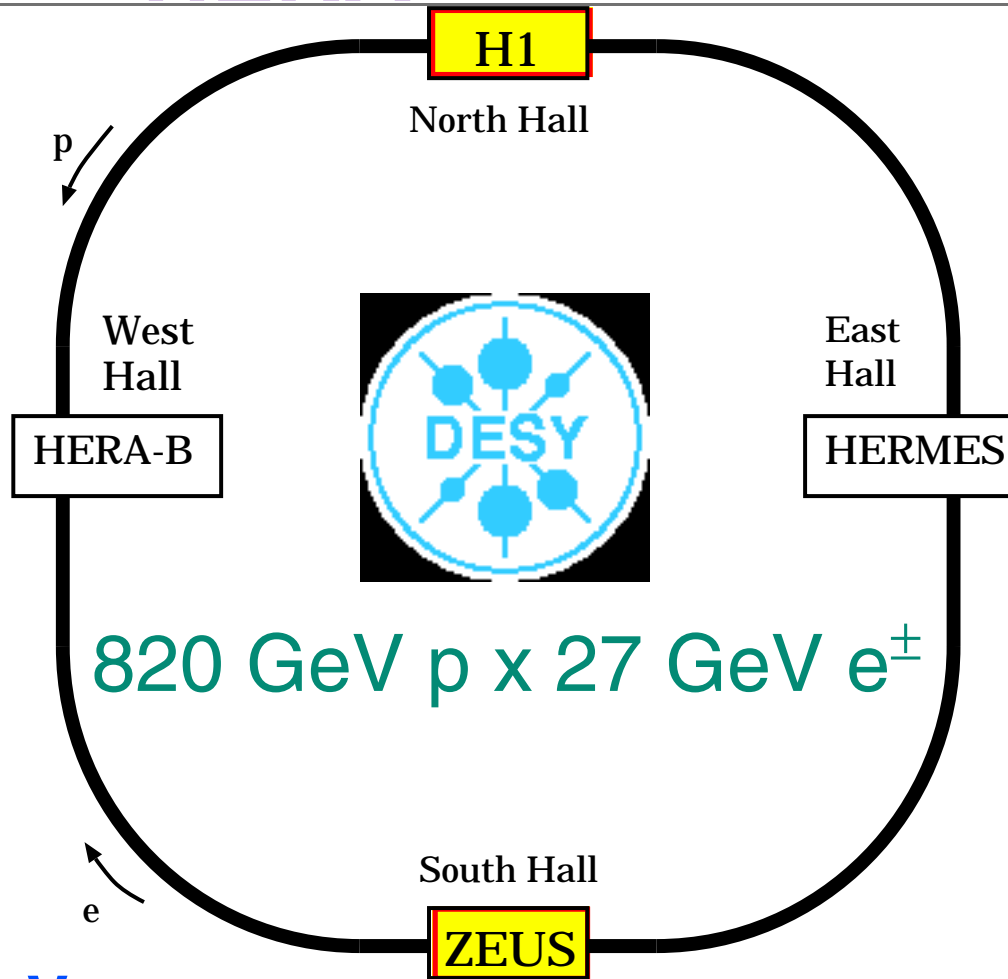
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**Appreciation for the  
help of many people  
from H1 and ZEUS:**

**(Advice, slides, etc.)**

**E. Barberis, V. Boudry, J. Bulmahn,  
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T. Trefzger, and many others.**

# HERA



## Collider:

- $\sqrt{s} = 300 \text{ GeV}$ 
  - Equivalent to 47 TeV fixed target

## Experiments:

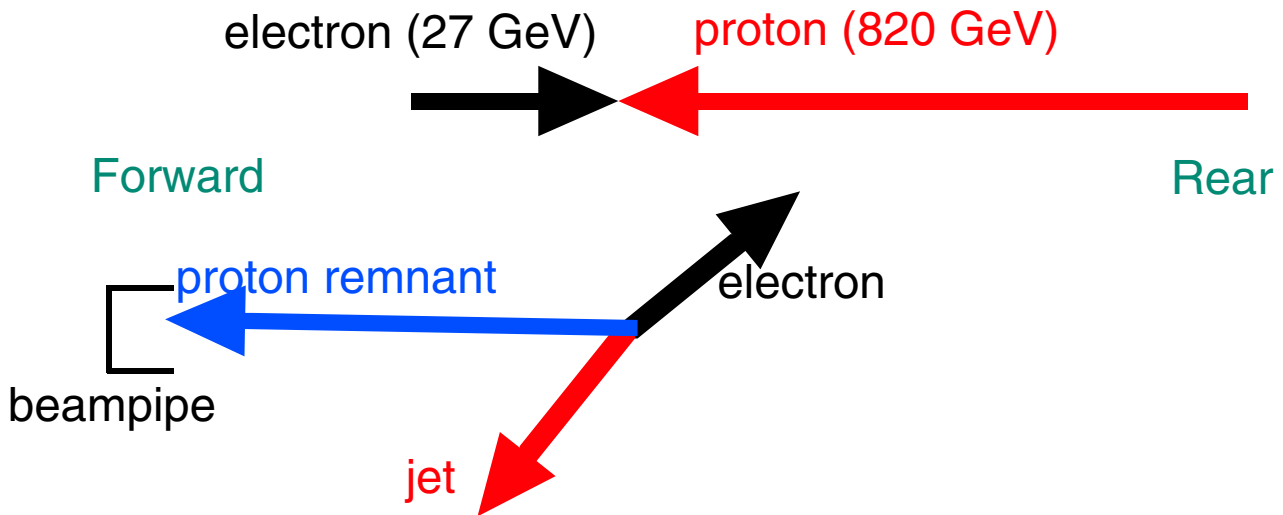
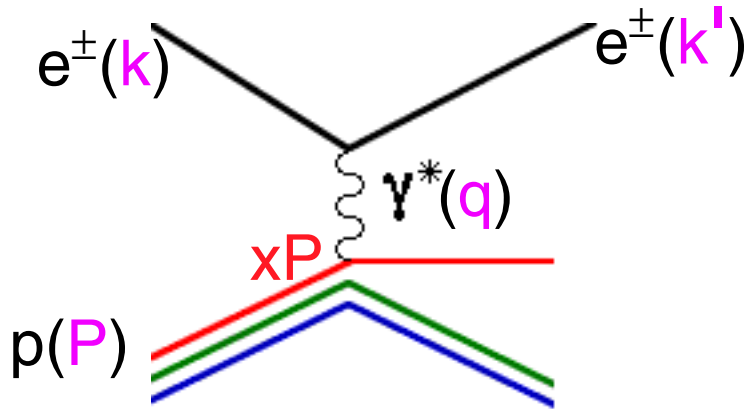
- 2 general purpose detectors (discussed):
  - H1 & Zeus
- Dedicated Fixed Target (not discussed):
  - HERMES:
    - Polarized electrons on polarized H target
  - HERA-B
    - Proton Halo on wire target



# Deep Inelastic Scattering

The DIS process

Measuring  
DIS at HERA:



$s = (k + P)^2 =$  center of mass energy

$Q^2 = -q^2 = -(k - k')^2 =$  (momentum transferred)<sup>2</sup>

$x =$  the fraction of the proton's momentum carried by the struck parton

$y =$  the fraction of the electron's energy lost in the proton rest frame

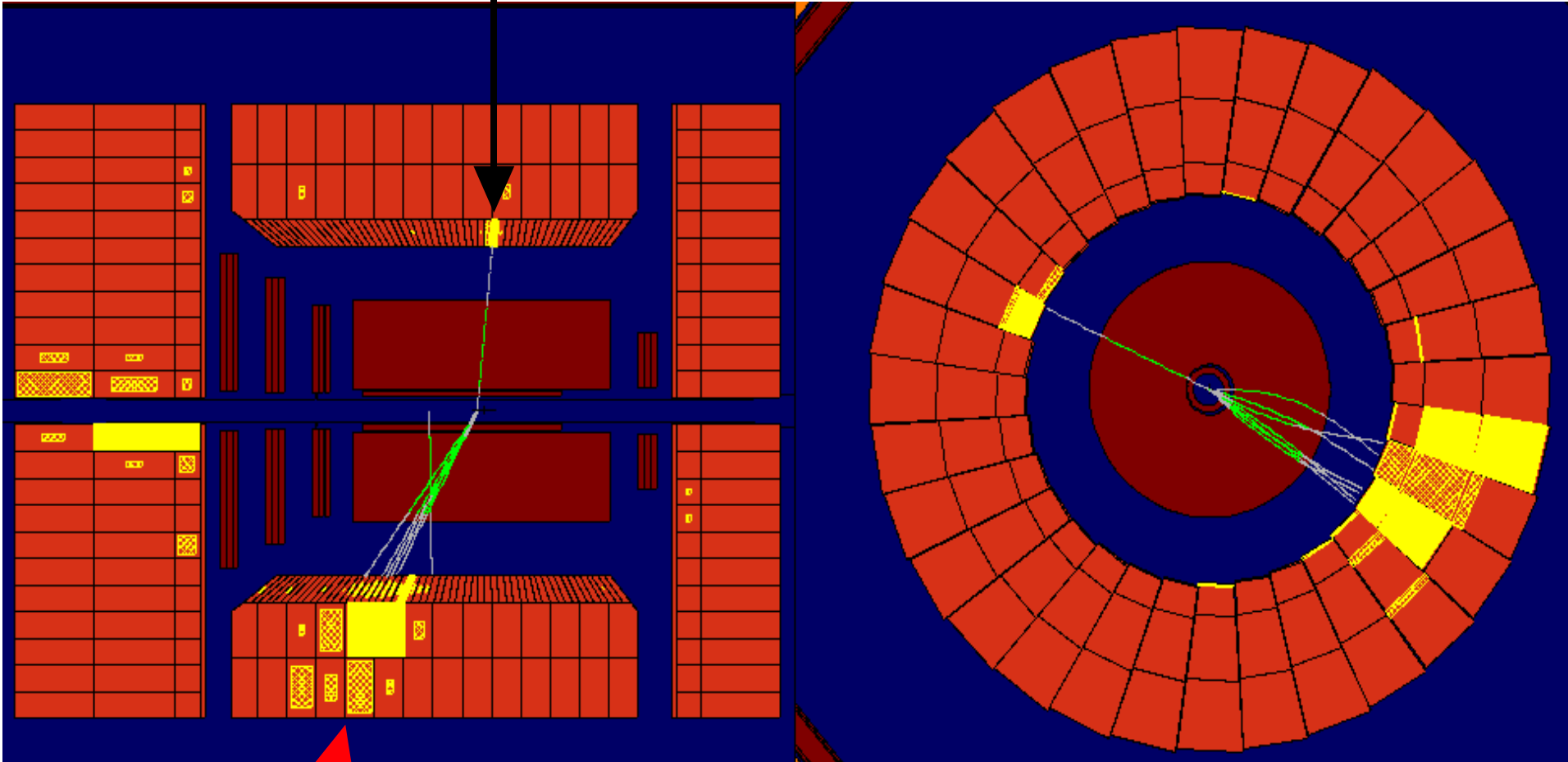
$$x = \frac{Q^2}{2P \cdot q}$$

$$y = \frac{P \cdot k}{P \cdot q}$$

$$Q^2 = sxy$$

# *DIS event $Q^2 = 1600 \text{ GeV}^2$*

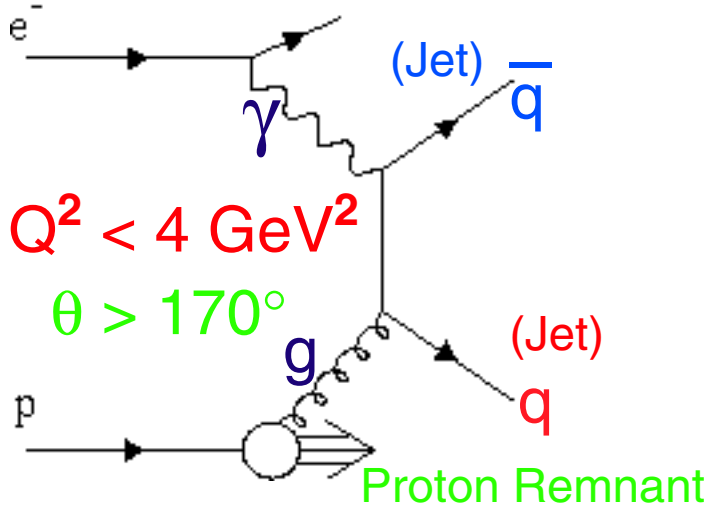
electron



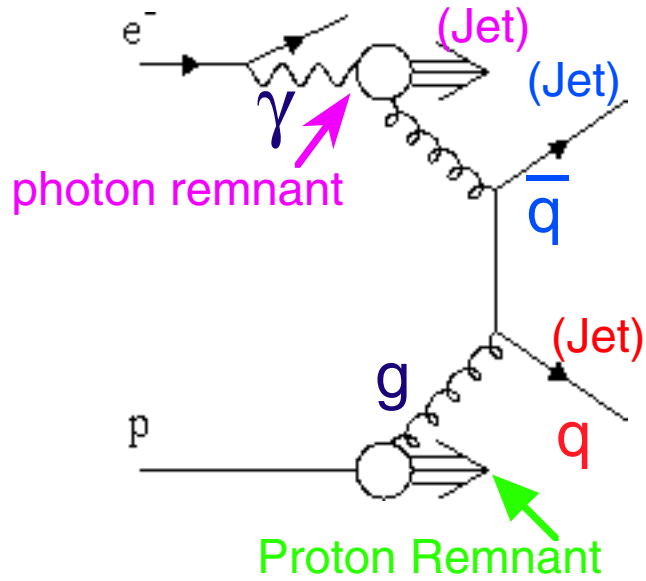
Jet

# Photoproduction

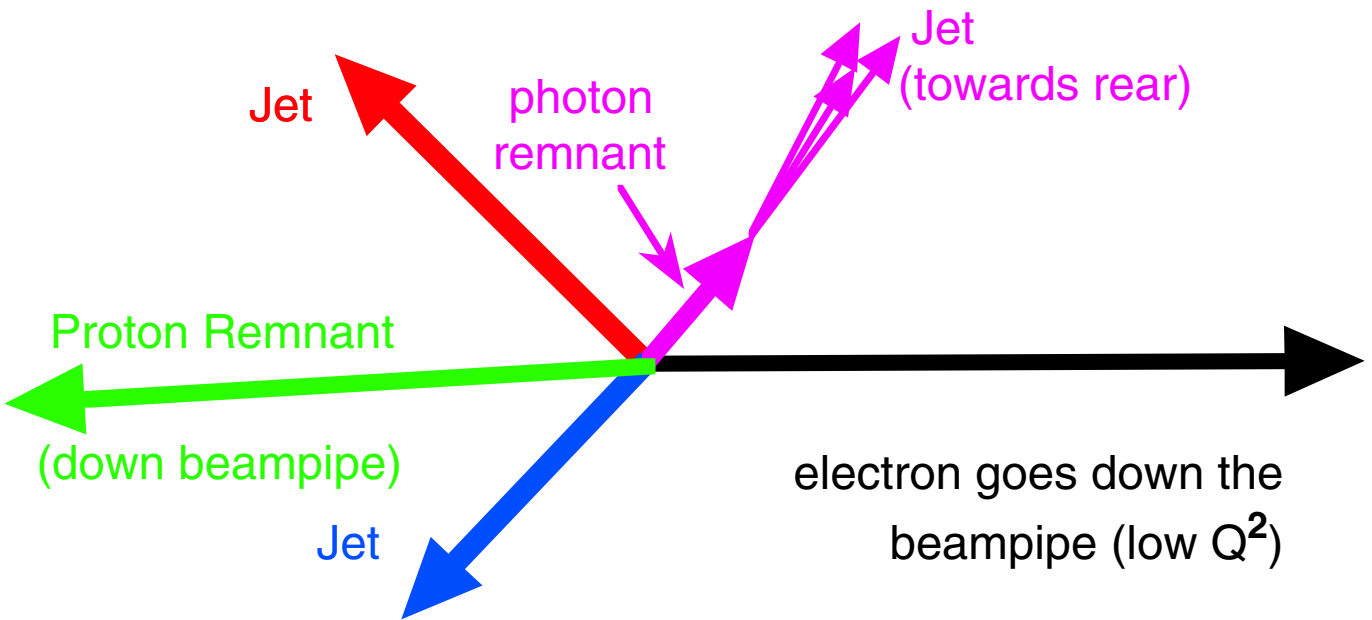
**Direct:**



**Resolved:**



**Almost real photon**



**Background for DIS**

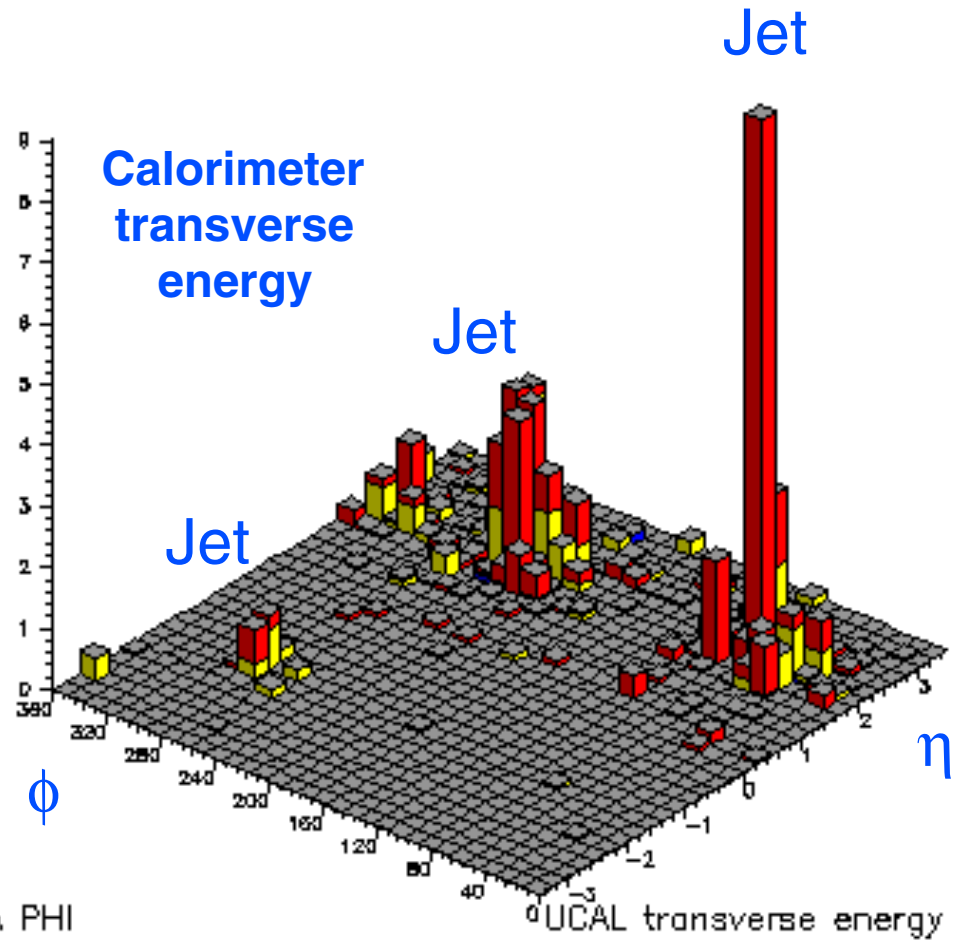
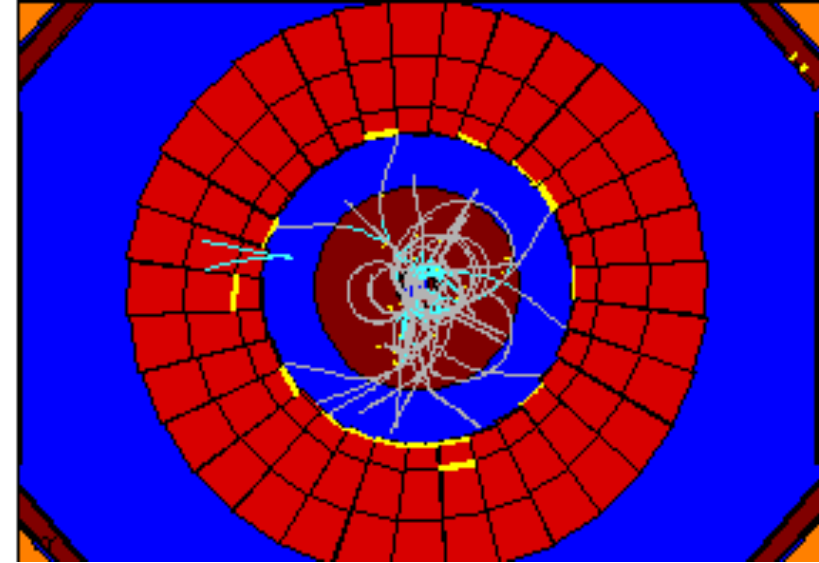
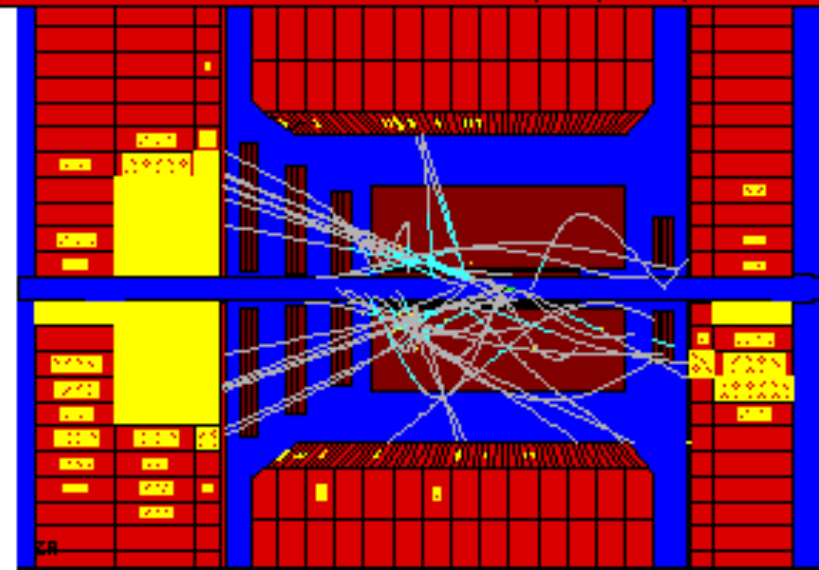
# Photoproduction event



$E= 238.5$   $E_t= 59.4$   $p_t= 4.2$   $p_z= 207.0$   $E-p_z= 31.5$   $E_t= 224.3$   $E_b= 2.5$   $E_r= 11.8$   
 $T_f= 0.8$   $T_r= 1.8$   $L_s= 14.3$   $L_r= 0.0$   $FNC= 0$   $BCN=124$   $FLT=808BDDFB$   $D1800000$   
 $z= -0.000$   $y=0.000$   $Q^2= 0$   $DA$   $x=0.000$   $Q^2= 0$   $JB$   $y=0.572$   $phi [ 0.180 ]$

Zeus Run 10064 Event 66075

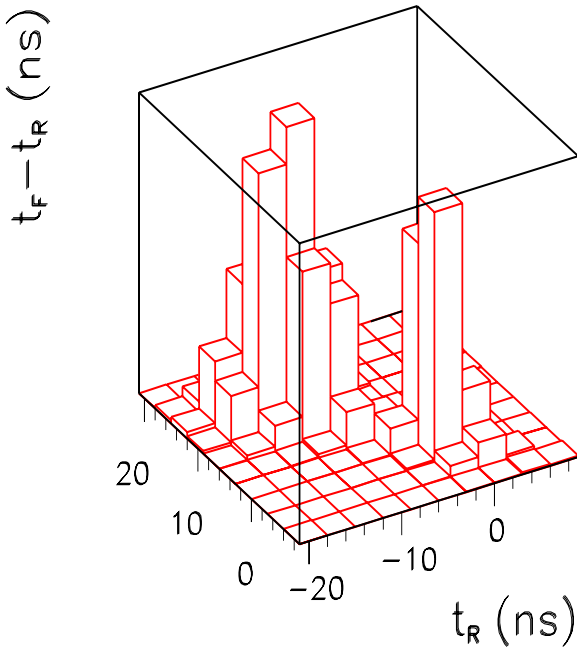
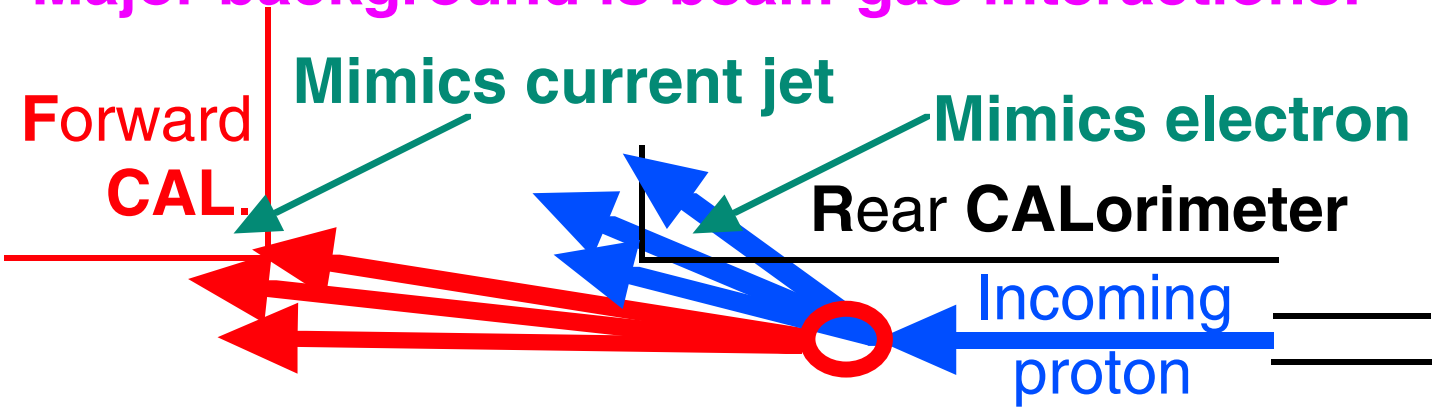
18-Oct-1994 14:48:43.422 File wa/data/min194/r010064.z





# Background rejection

Major background is beam-gas interactions:



reject beam gas

\*vertex cut

\*timing  $\sigma_t \sim 1$  ns

← Cal. timing

$(E - P_z)$  is conserved

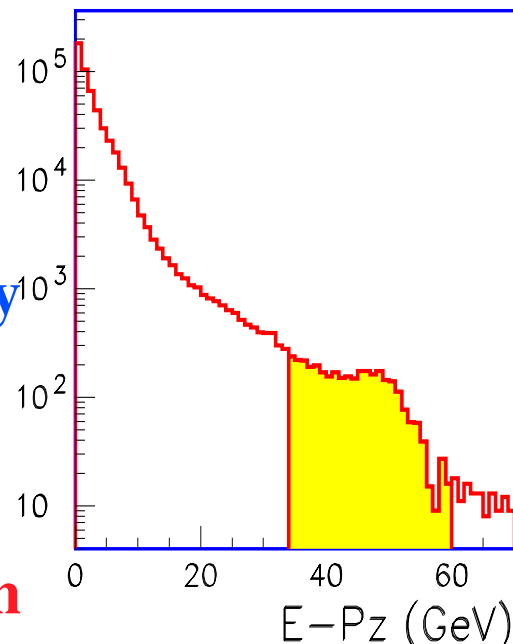
Initially:

$$E_P - P_P + E_e - (-P_e) = 2E_e$$

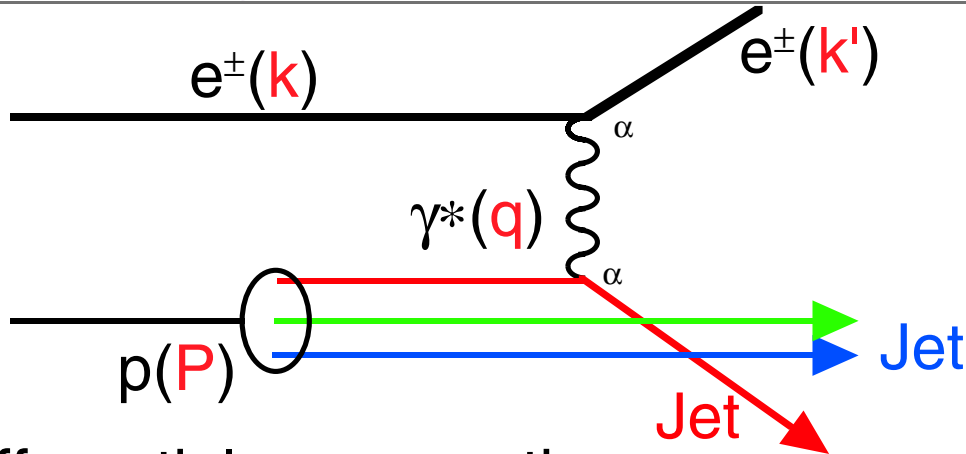
remains same if no energy  
down rear beam pipe.

True for DIS

False for photoproduction



# DIS cross section



DIS differential cross section:

$$\frac{d\sigma^{NC}(e^\pm p)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} Y_\pm \left[ F_2 - \frac{y^2}{Y_+} F_L \mp \frac{Y_-}{Y_+} xF_3 \right]$$

$$Y_\pm = 1 \pm (1-y)^2$$

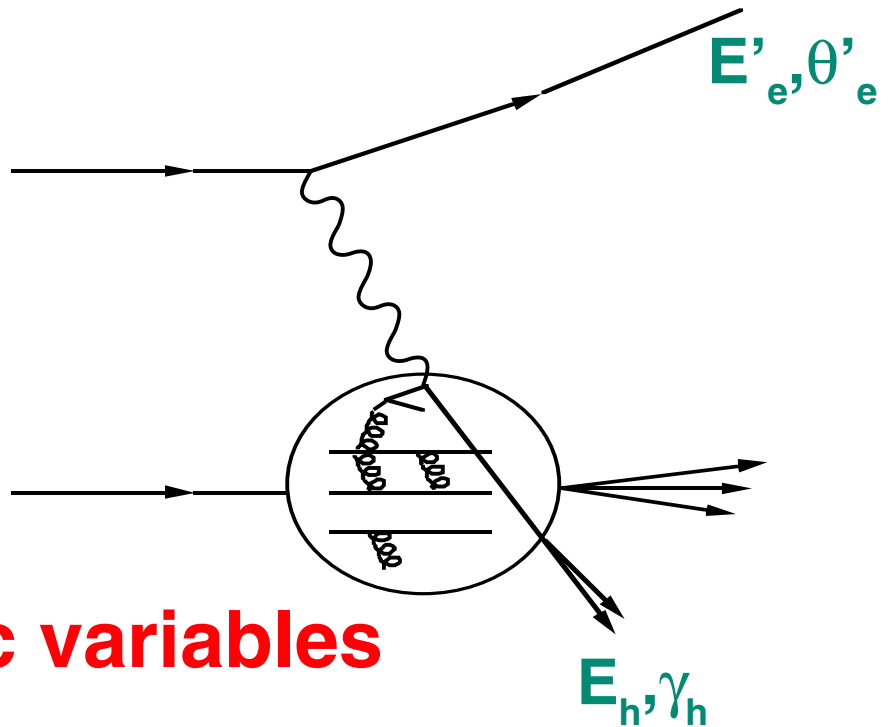
$\gamma^*$  is longitudinally or transversely polarized

$F_2(x, Q^2)$  = Structure function = interaction btw. transversely polarized photons & spin 1/2 partons = charge weighted sum of the quark distributions.

$F_L(x, Q^2)$  = Structure function = cross section due to longitudinally polarized photons that interact with the proton. The partons that interact have transverse momentum. (Important at high  $y$ ).

$F_3(x, Q^2)$  = Parity-violating structure function from  $Z^0$  exchange. (Important at high  $Q^2$ ).

# Kinematic Reconstruction



## 2 kinematic variables

- $x, Q^2$

## 4 measured quantities

- $E'_e, \theta'_e, E_h, \gamma_h$

## Any 2 measured variables can be used to reconstruct $x, Q^2$

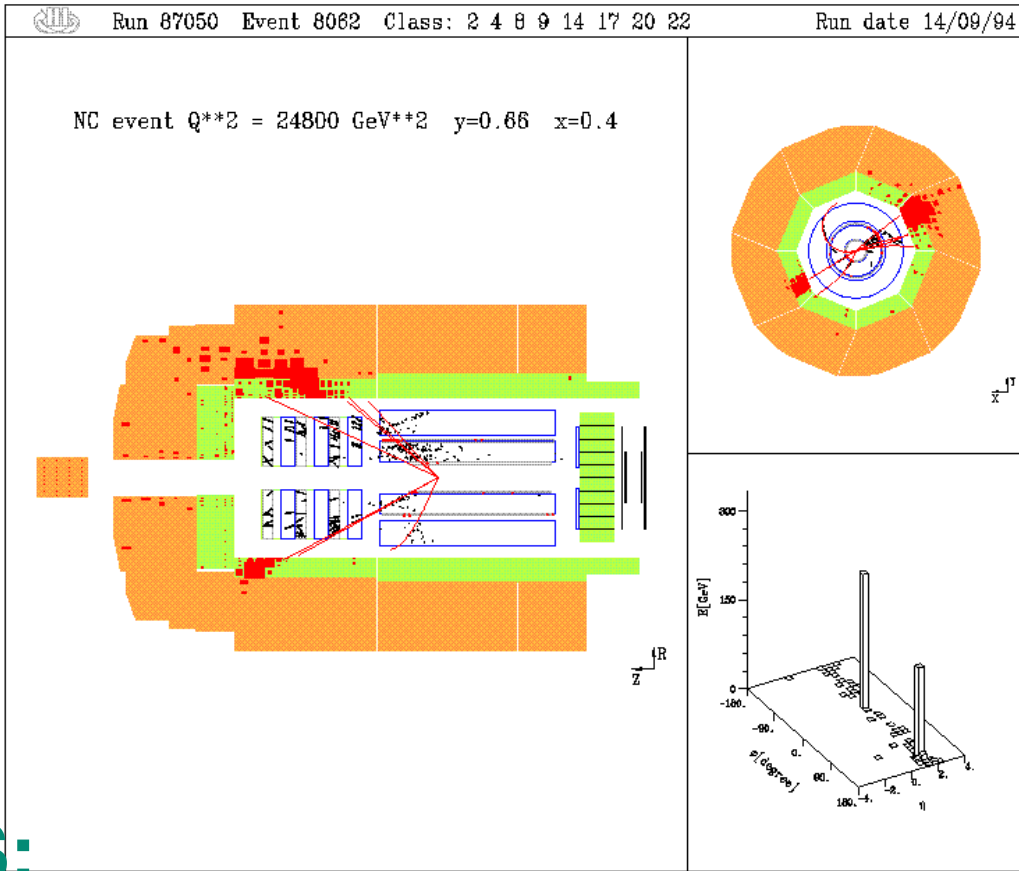
- Reconstruction may not be optimal.

## $P_T$ method

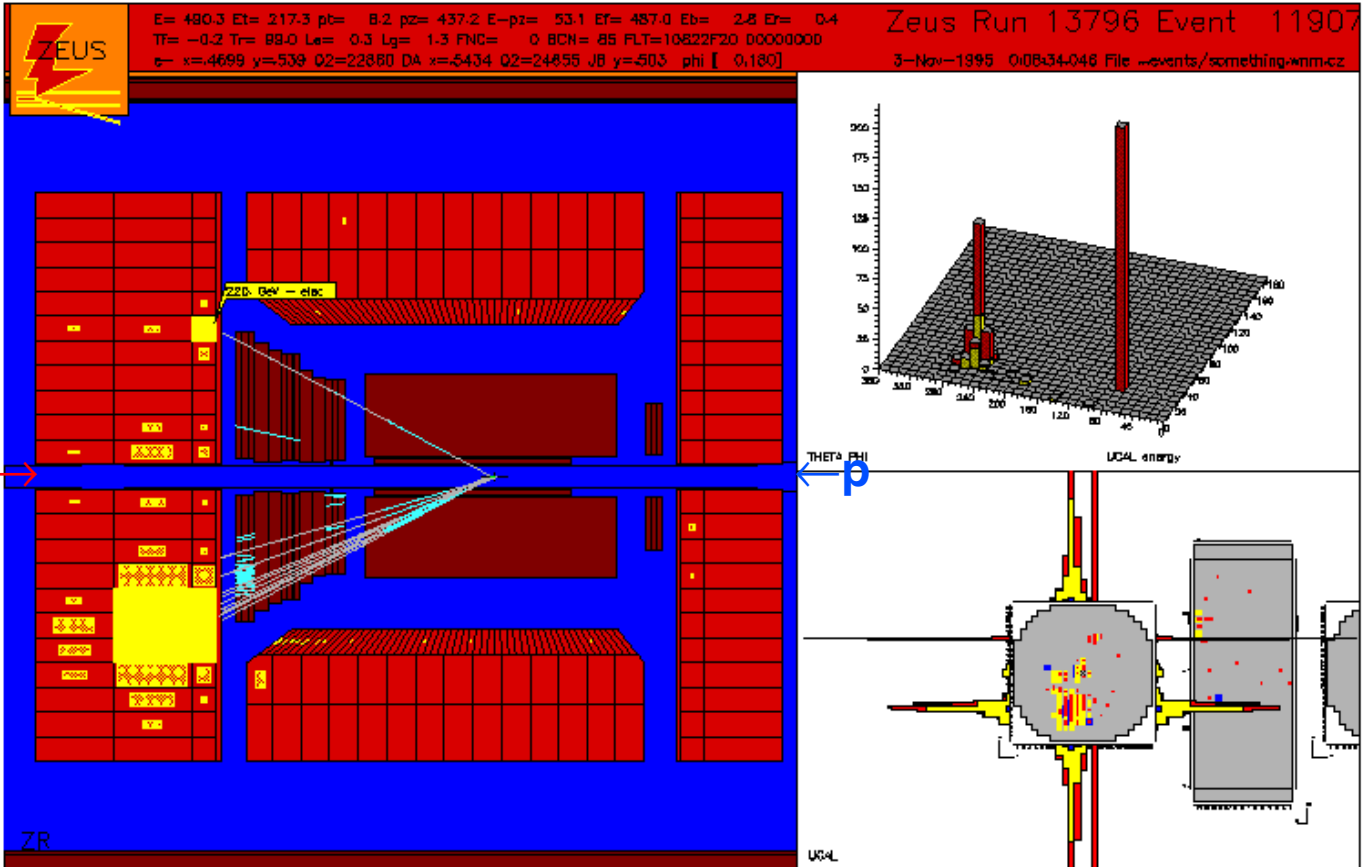
- Best performance for full kinematic range
- Uses  $(E'_e, \theta'_e, E_h, \gamma_h)$ ,  $E-P_z$  conservation, and  $P_T$  balance between the electron and current jet

# Experiments - High $Q^2$

H1:



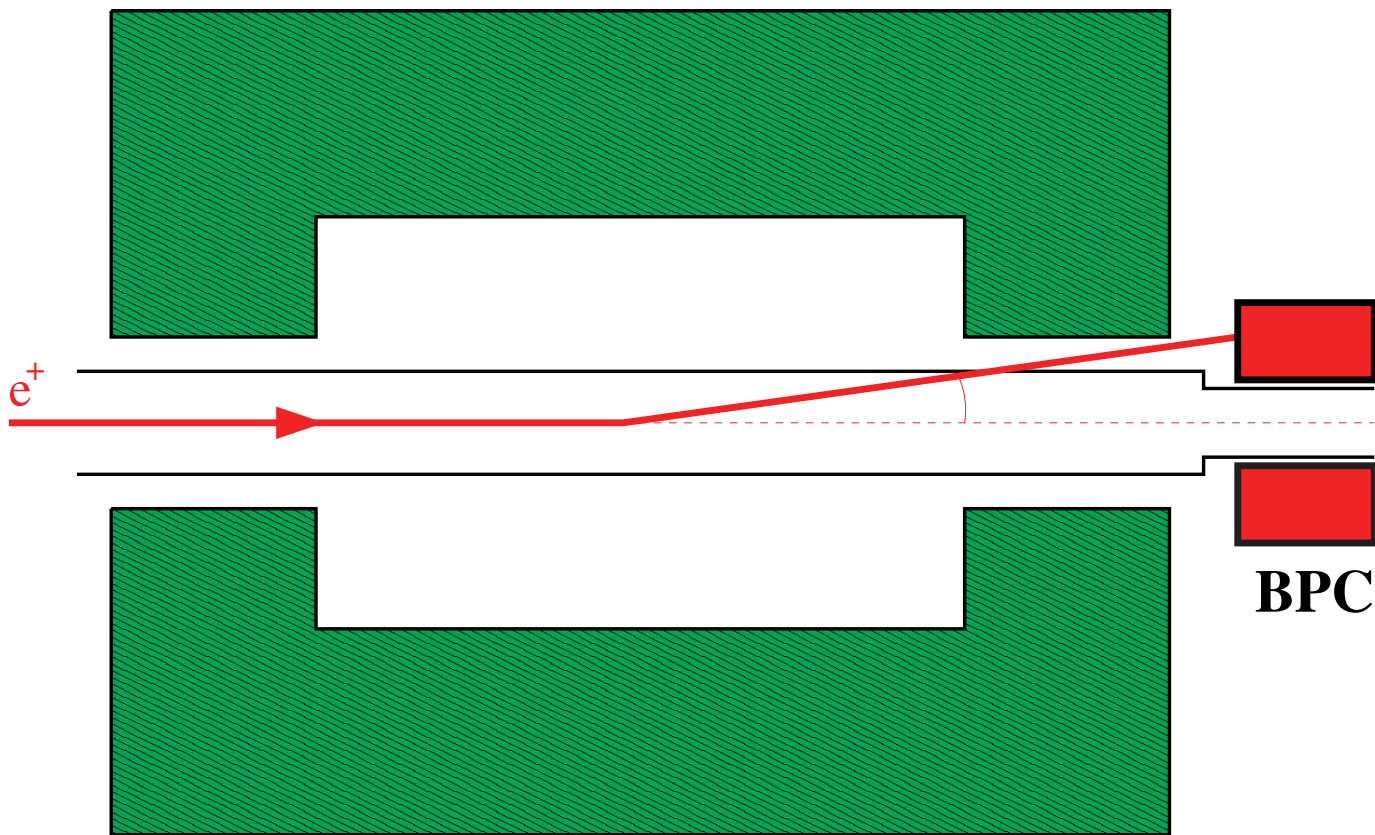
ZEUS:



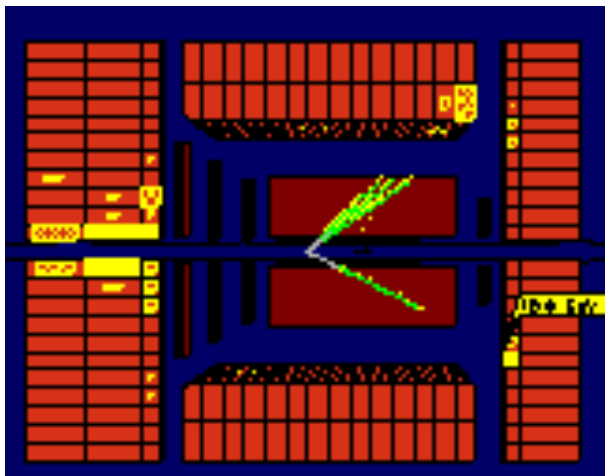
# Experiments - Low $Q^2$

$$Q^2 = 4EE' \cdot \sin^2\left(\frac{\Theta}{2}\right)$$

## Zeus Beampipe Calorimeter:

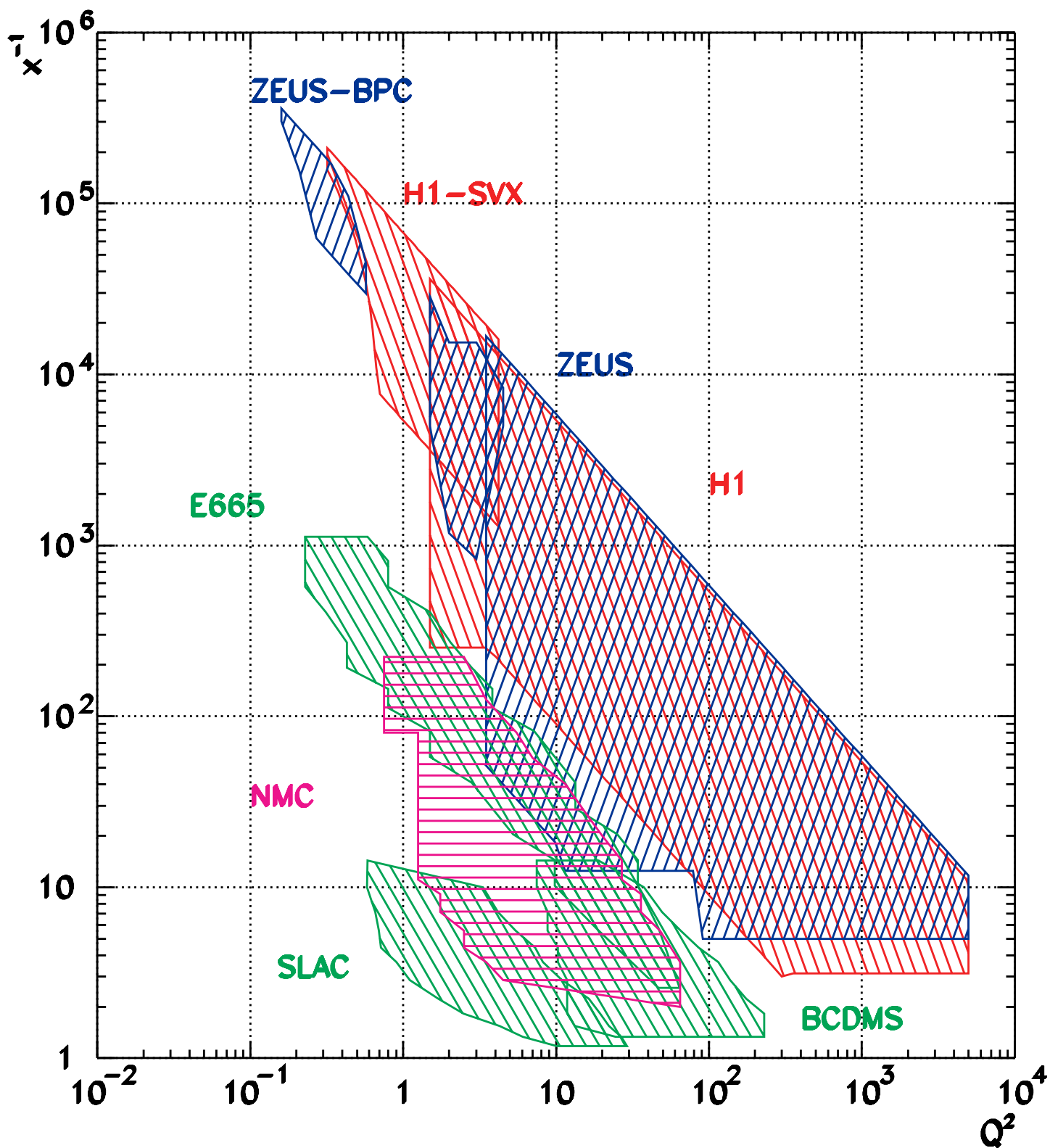


## H1 & Zeus Shifted Vertex:



## H1 & Zeus Initial State Radiation

# Experimental Kinematic Range



# Parton model

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Proton is made up of non-interacting partons.

Bjorken scaling, i.e.,  $Q^2$  independence of structure functions holds. SLAC-MIT experiments observed approximate scaling in data.

Structure function is given by the charge weighted sum of parton momentum densities

$$F_2(x) = \sum_i e_i^2 x f_i(x)$$

For spin-half partons

$$F_L = 0$$

For spin-zero partons

$$F_L = F_2$$

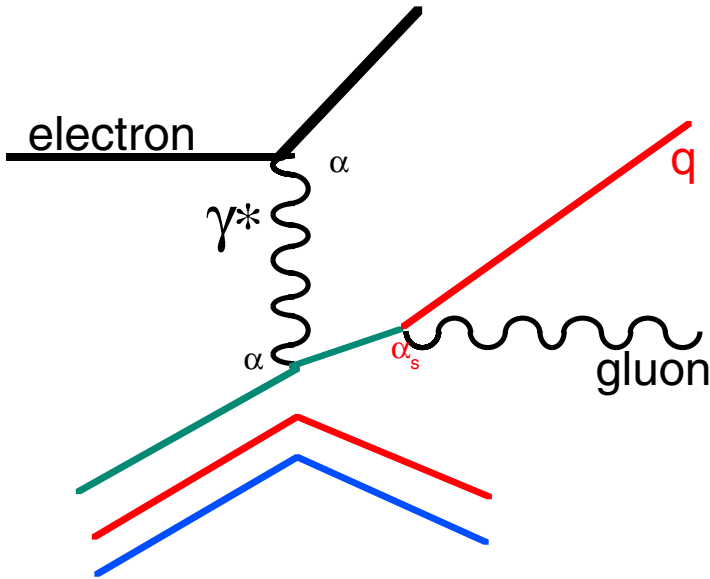
The parton densities  $f_i(x)$  are not calculable in the model and are to be derived from experiment.

Deep inelastic scattering provides a good laboratory for parton density extraction because the electromagnetic probe is well understood.

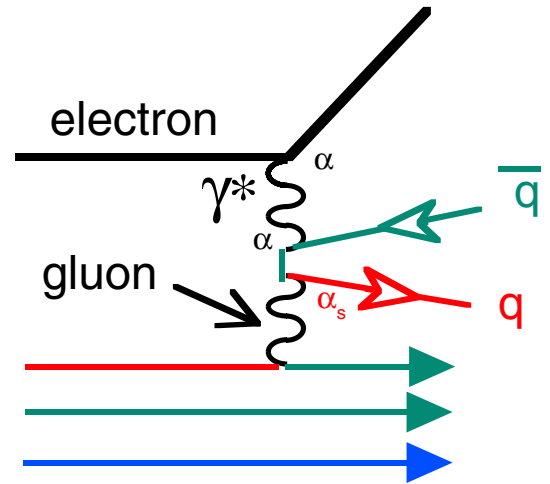
# Scaling violations

Quark transverse momentum from quark-gluon interactions causes scaling violation:  $F_2(x) \rightarrow F_2(x, Q^2)$ .

QCD Compton

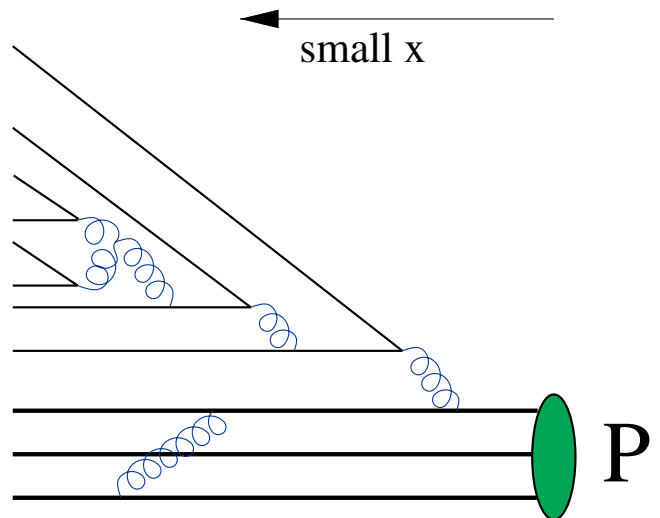
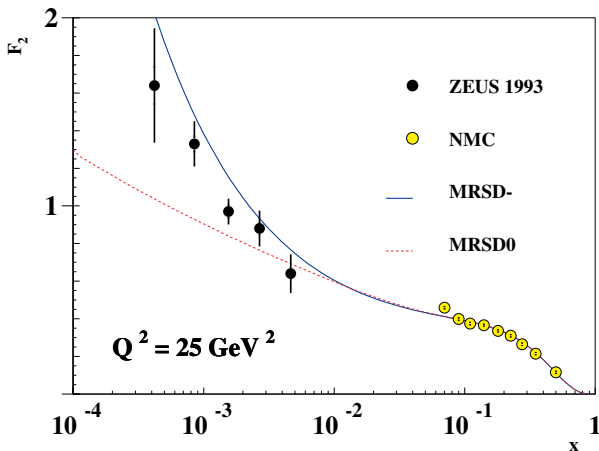


Boson-Gluon Fusion



Splitting functions, probabilities for these interactions, are calculated in 2nd order perturbative QCD.

These interactions drive  $F_2(x)$  to grow with decreasing  $x$ :





# Perturbative QCD

Given an empirical parameterization for parton densities at  $Q^2=Q_0^2$ , e.g.:

$$xg(x) = A_g x^{\delta_g} (1-x)^{\eta_g} (1 + \gamma_g x)$$

Dokshitzer-Gribov-Lipatov-Altarelli-Parisi equations describe evolution of parton densities to higher  $Q^2$

$$\frac{dq_i(x, Q^2)}{d \ln Q^2} = \frac{\alpha_s(Q^2)}{2\pi} \int_x^1 \frac{dw}{w} \left[ q_i(w, Q^2) P_{qq} \left( \frac{x}{w} \right) + g(w, Q^2) P_{qg} \left( \frac{x}{w} \right) \right]$$

$$\frac{dg(x, Q^2)}{d \ln Q^2} = \frac{\alpha_s(Q^2)}{2\pi} \int_x^1 \frac{dw}{w} \left[ \sum_i q_i(w, Q^2) P_{gq} \left( \frac{x}{w} \right) + g(w, Q^2) P_{gg} \left( \frac{x}{w} \right) \right]$$

Next-to-leading order splitting functions,  $P$ , are now available.

The structure function  $F_2$  is given by,

$$F_2(x, Q^2) = \sum_i e_i^2 x q_i(x, Q^2)$$

Calculation of DIS cross section requires  $F_L$ :

$$F_L(x, Q^2) = \frac{\alpha_s(Q^2)}{\pi} \int_x^1 \frac{dw}{w} \left( \frac{x}{w} \right)^2 \left\{ \frac{4}{3} F_2(w, Q^2) + 2 \sum_i e_i^2 \left( 1 - \frac{x}{w} \right) w g(w, Q^2) \right\}$$

Parameterization of gluon density can be determined by fitting QCD evolution to DIS data.

# Expected low- $x$ behavior of $F_2$

## • Regge Approach

### • Donnachie-Landshoff (DL)

since :  $F_2 = \frac{Q^2}{4\pi\alpha^2} \sigma(\gamma * p)$

but at  $Q^2 = 0$  :  $\sigma(\gamma * p) = C(W^2)^{-0.08}$

and at low  $x$  :  $W^2 = \frac{Q^2}{x} \rightarrow \sigma(\gamma * p) = C'(Q^2)X^{-0.08}$

Therefore :  $\lim_{Q^2 \rightarrow 0} F_2(x, Q^2) = f(Q^2)x^{-0.08}$

### • Martin-Roberts-Stirling (MRS)

- Assume  $g(x, Q_0^2) \sim x^{\gamma_1}$  &  $F_2(x, Q_0^2) \sim x^{\gamma_2}$

- Evolve in  $Q^2$  according to QCD

### • Gluck-Reya-Vogt (GRV)

- Use "valence-like" distributions at low  $Q^2$

- Evolve in  $Q^2$  according to QCD

- Empirically produces  $\gamma \ll -0.08$

### • Balitsky-Fadin-Kuraev-Lipatov (BFKL)

- Summation of many QCD graphs in powers of  $\ln(1/x)$

$$g(x, Q_0^2) \sim x^\gamma \text{ and } \gamma = -\frac{12 \ln(2)}{\pi} \alpha_s \sim -0.5$$

# $F_2$ Results

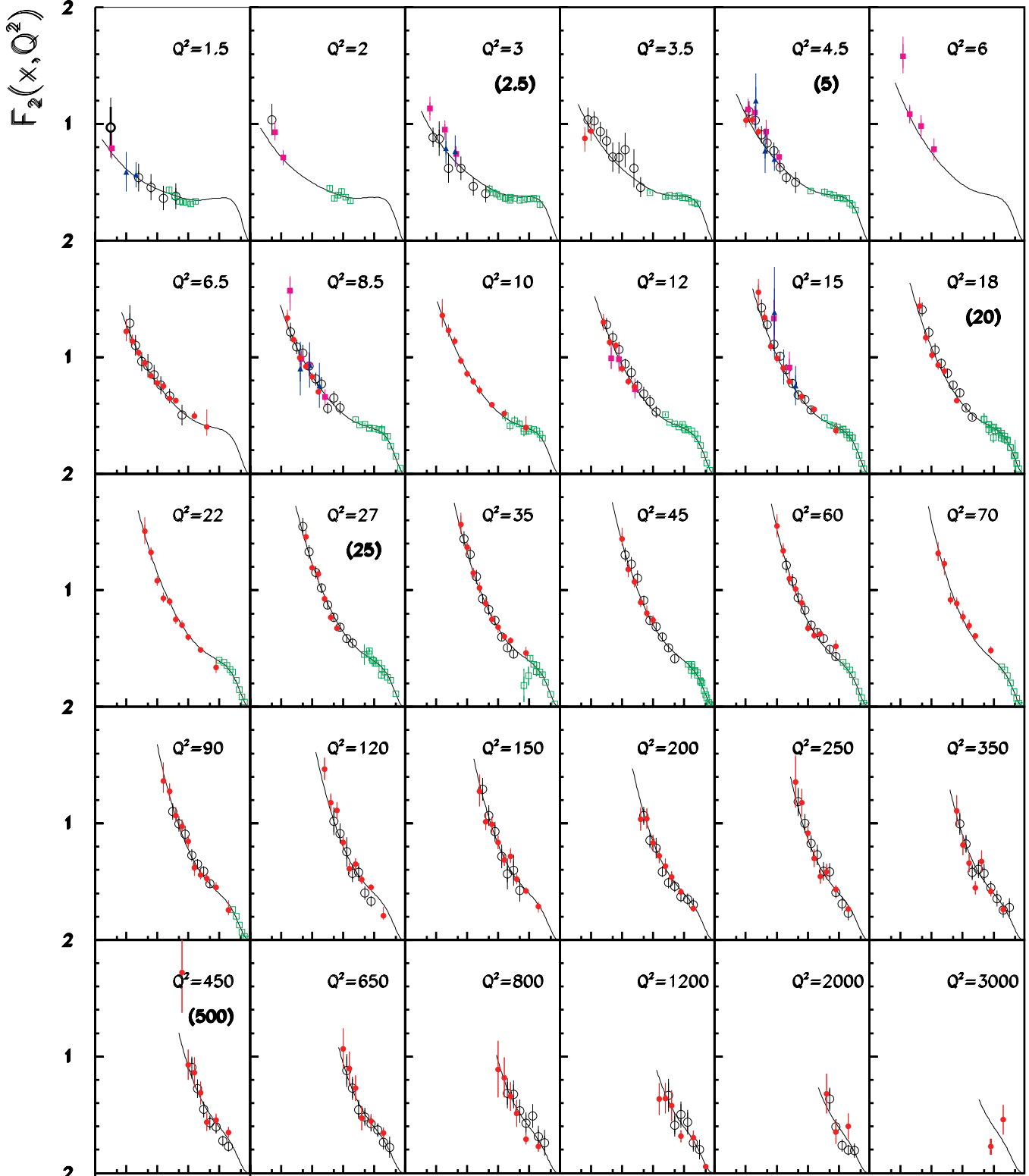
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## Extraction:

- Bin data in  $x$ ,  $Q^2$
- Subtract background
- Cross section multiplied by QCD  $F_L$  calculation using parameterizations of  $q(x, Q^2)$  and  $G(x, Q^2)$
- Acceptance estimated from Monte Carlo
- $F_2$  unfolded iteratively until MC matches data
- Estimate Systematic Error

## Issues:

- Does rise at low  $x$  continue?
- Over what kinematic range is rise observed?
- Agreement with fixed target experiments?



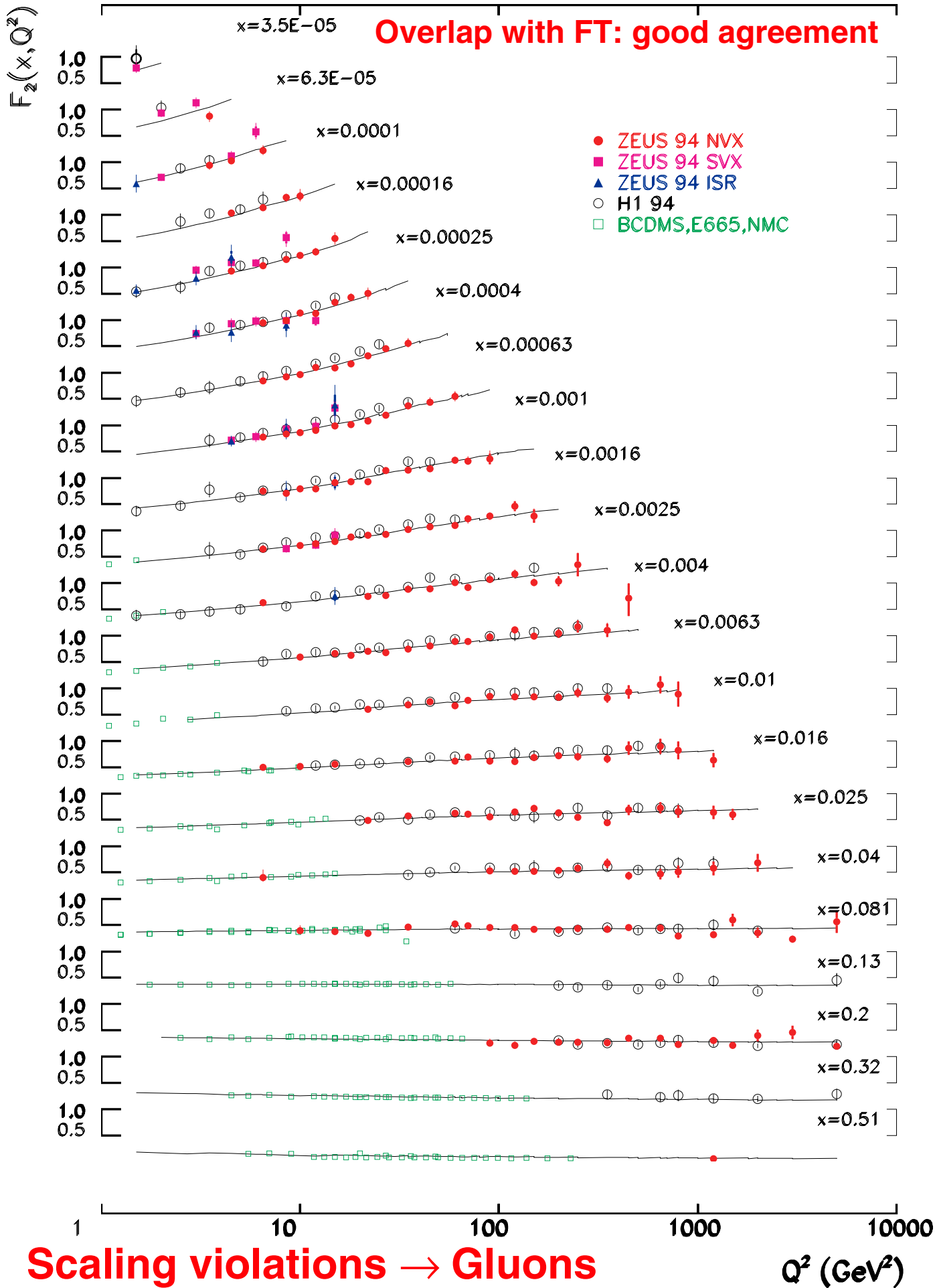
$10^{-4}$   $10^{-3}$   $10^{-2}$   $10^{-1}$  1     $10^{-4}$   $10^{-3}$   $10^{-2}$   $10^{-1}$  1     $10^{-4}$   $10^{-3}$   $10^{-2}$   $10^{-1}$  1     $10^{-4}$   $10^{-3}$   $10^{-2}$   $10^{-1}$  1     $10^{-4}$   $10^{-3}$   $10^{-2}$   $10^{-1}$  1     $10^{-4}$   $10^{-3}$   $10^{-2}$   $10^{-1}$  1     $\times$

- ZEUS 94 NVX
- ZEUS 94 SVX
- ▲ ZEUS 94 ISR
- H1 94 ( $Q^2$  in paren. where different)
- BCDMS, NMC, E665
- ZEUS QCDNLO fit

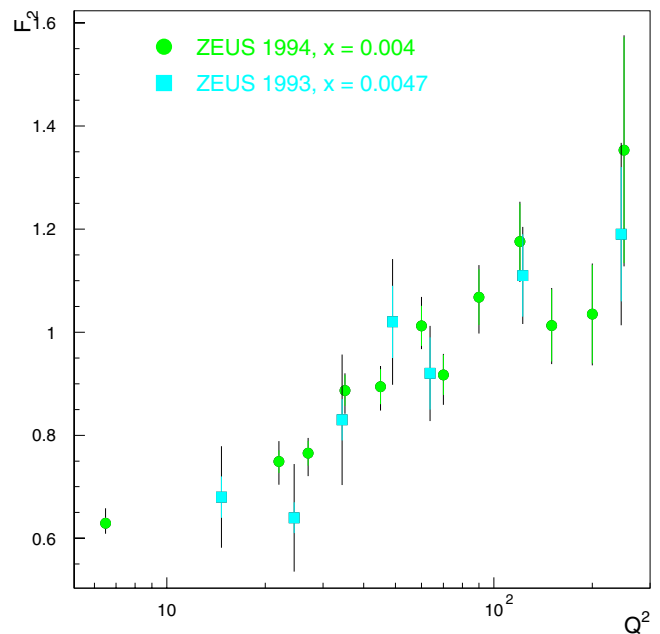
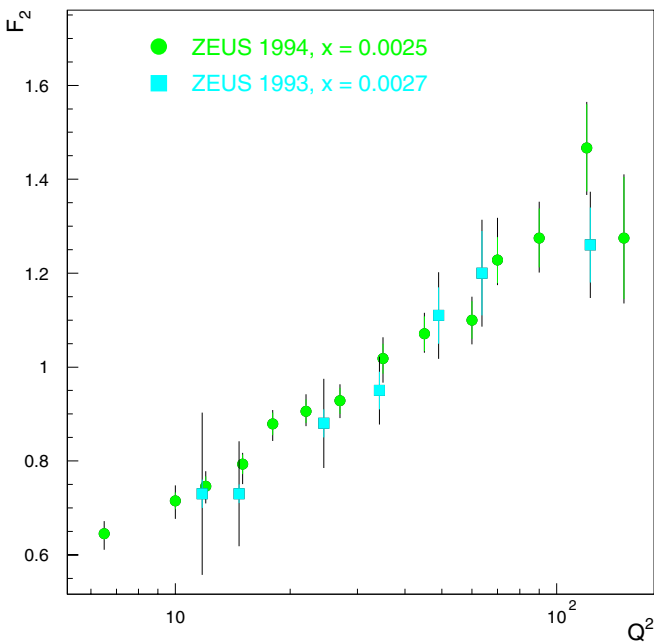
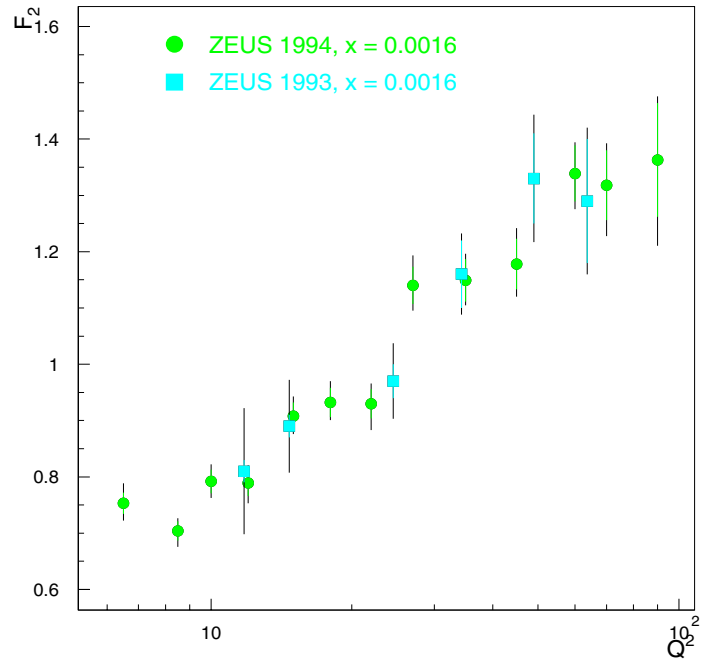
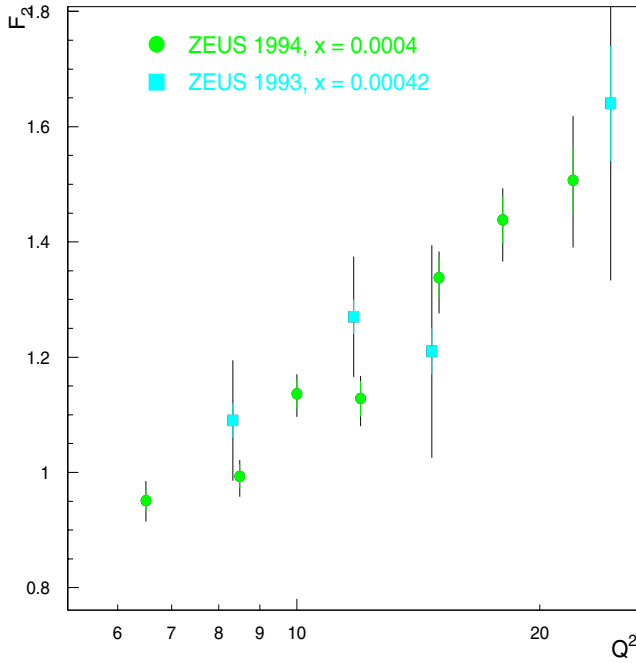
**DGLAP describes down to  $x \sim 10^{-4}$ ,  $Q^2 \sim 1.5 \text{ GeV}^2$**

**No need to resum  $\ln(1/x)$  terms (BFKL)**

$10^{-4}$   $10^{-3}$   $10^{-2}$   $10^{-1}$  1



# Scaling Violation - Gluon sensitivity



Sensitivity to the gluon distribution is in the slope of  $F_2$  versus  $\log Q^2$  plots. 1994 and 1993 ZEUS  $F_2$  data is shown above. It is seen that 94 data constrains  $dF_2/d\log Q^2$  with high precision.

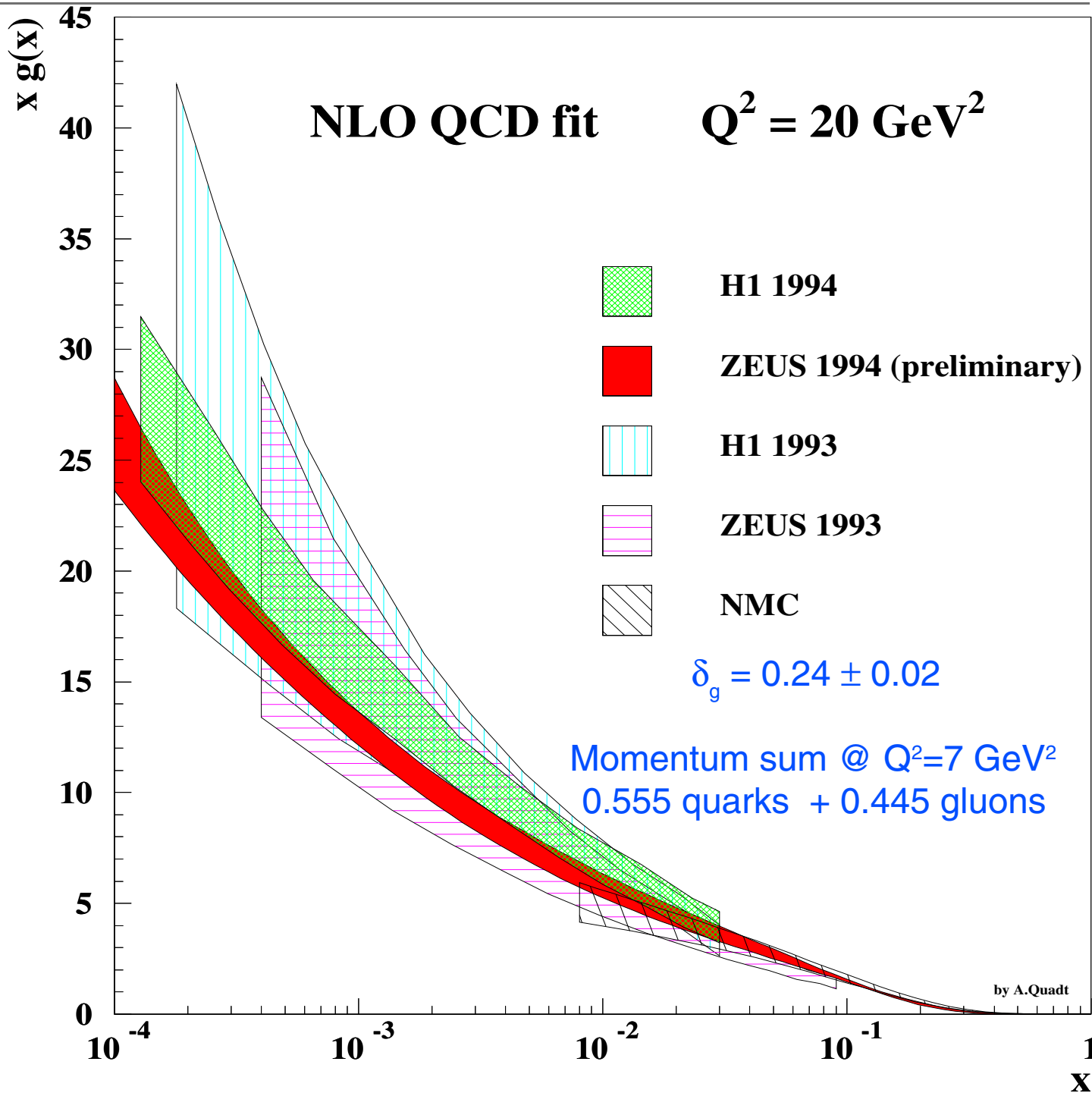
# *Extraction of gluon density*

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## **Example: fit to ZEUS 1994 $F_2$ data:**

- Used NMC data to constrain fit at larger values of  $x$ .
- Assumed momentum sum rule to constrain gluon density.
- Assumed quark and gluon density functional forms.
- Assumed (SLAC/BCDMS)  $\alpha_s(M_Z^2)=0.113$  and evolved to higher  $Q^2$ .
- Evolved the distributions using GLAP eq'ns to measured  $Q^2$  bins to calculate  $F_2$ .
- In computation of  $\chi^2$  for agreement with the fit only the statistical errors were included.
- Performed nonlinear minimization of  $\chi^2$  to find fit parameters for assumed functional forms of quarks and gluons.
- Systematic uncertainty estimated separately by varying each of the 31 different systematic effects individually and performing a new fit.

# Gluon results



A significant improvement in the uncertainty and in the validity range in kinematic plane is seen in the gluon density extracted from the 1994 H1 and ZEUS DIS data. Agreement with 1993 extraction is remarkable.



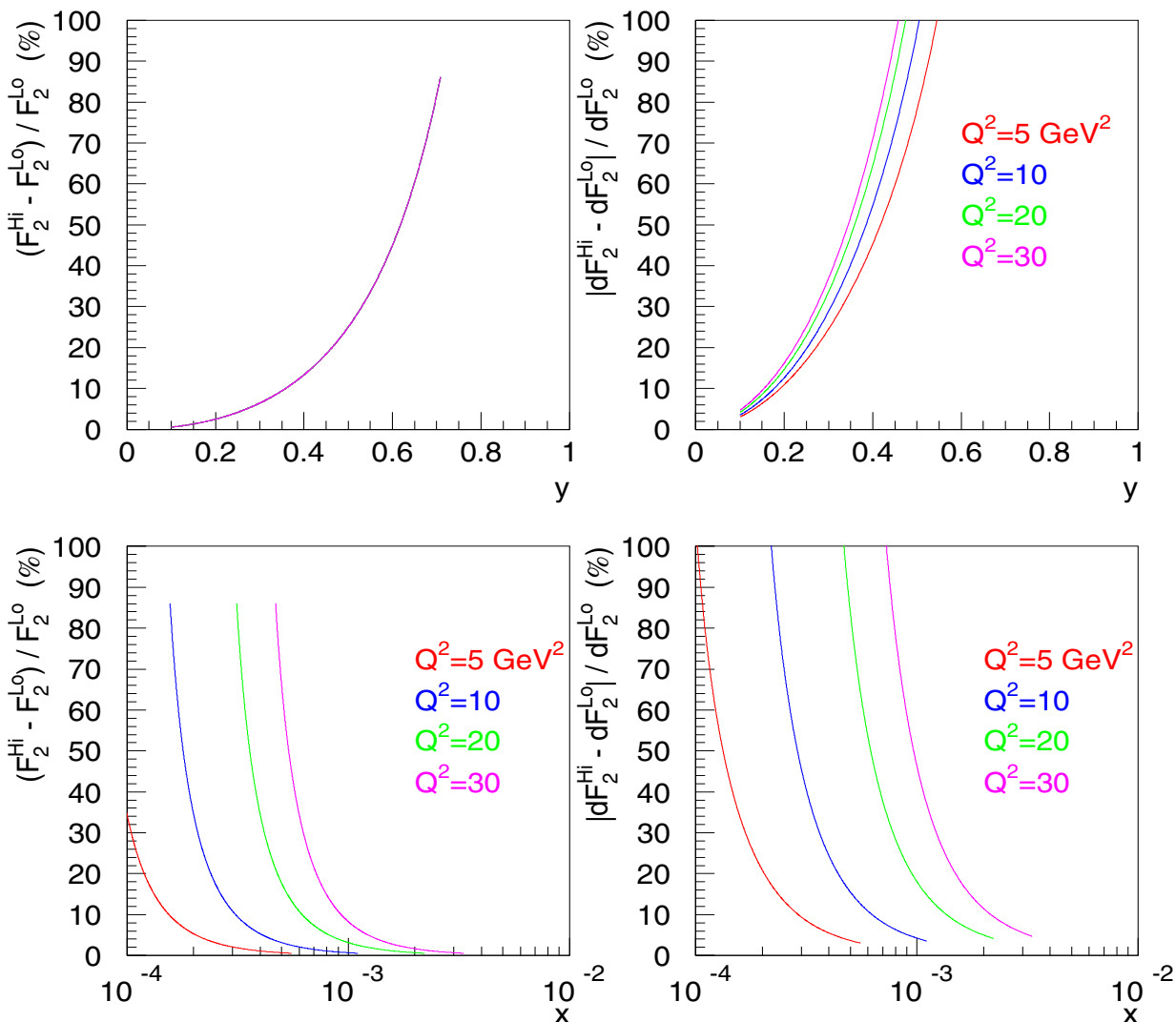
# Caveats on $F_2$ & Gluons

ZEUS  $F_2$  extraction, as is true with most world  $F_2$  data, involved a priori assumptions for  $\alpha_s$  and quark-gluon parameterizations in computing  $F_L$  and  $F_3$  corrections for DIS cross section.

The extracted  $F_2$  is sensitive to these assumptions, particularly for high  $y$  kinematic range data, which is sensitive to the gluon. Therefore, an assumption independent analysis needs to be done by fitting directly to the cross section data.

The results of such analysis can yield consistent values for  $\alpha_s$ , quark and gluon parameterizations.

Impact of  $F_L$  uncertainty ( $F_L: 0 \rightarrow F_2$ ) on  $F_2$  and  $dF_2/d\ln Q^2$



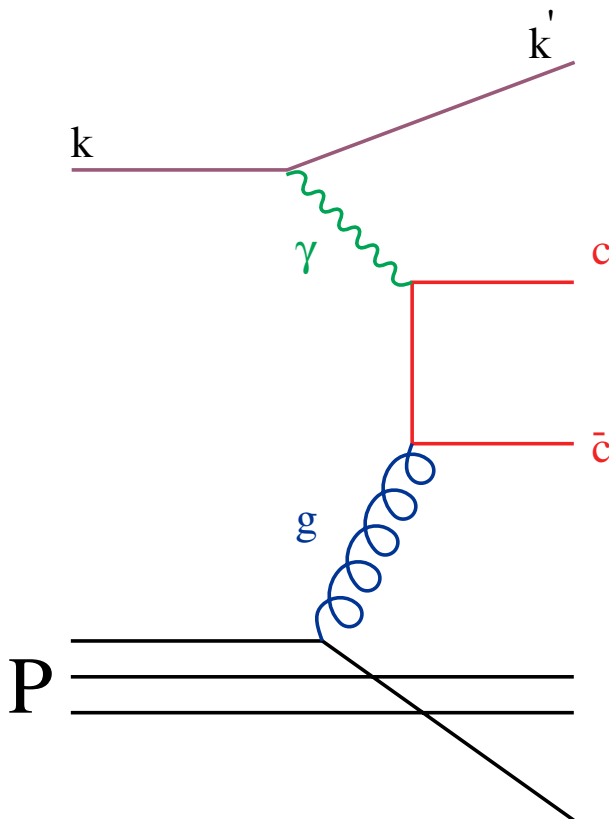
# Charm $F_2$

## Analyze components of $F_2$

- Identify Flavor in the final state
- Justify NLO QCD assumptions
- Further understand the rise in  $F_2$

## Evolution of charm from the sea:

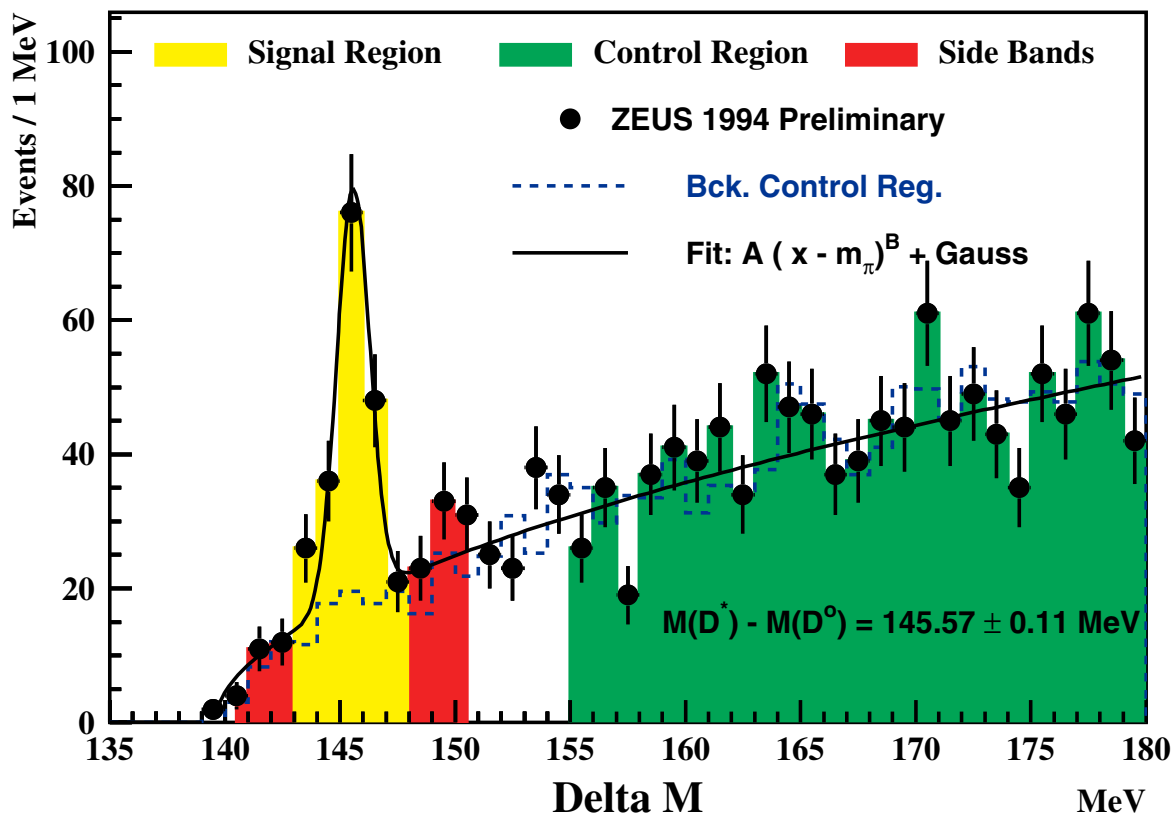
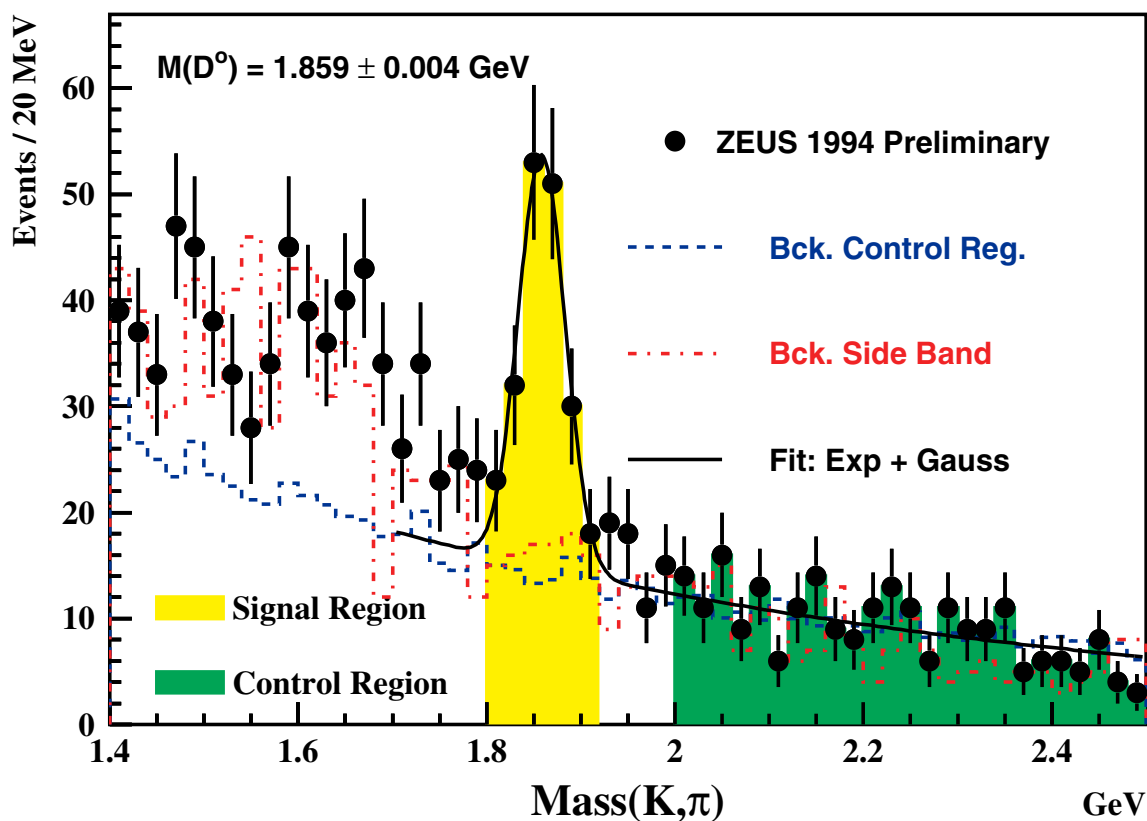
- Boson Gluon Fusion:



- Small Contribution from fragmentation
- Higher sensitivity to gluon density than  $F_2$

# Identifying open charm/ $D^*$ signals

$D^* \rightarrow (K \pi) \pi_S$  in DIS



# $F_2^{c\bar{c}}$ versus $x$

## H1 Result:

- $\frac{d^2\sigma^{c\bar{c}}}{dx dQ^2} = \frac{4\pi\alpha^2}{xQ^4}(1 + (1 - y)^2) F_2^{c\bar{c}}(x, Q^2)$
- Range extended by 1/100 in  $x$  with respect to EMC
- Steep rise in  $F_2^{c\bar{c}}$  at small  $x$
- In agreement with NLO calculations BUT currently statistics too poor to draw any conclusions
- Eventually alternative handle on the gluon

