

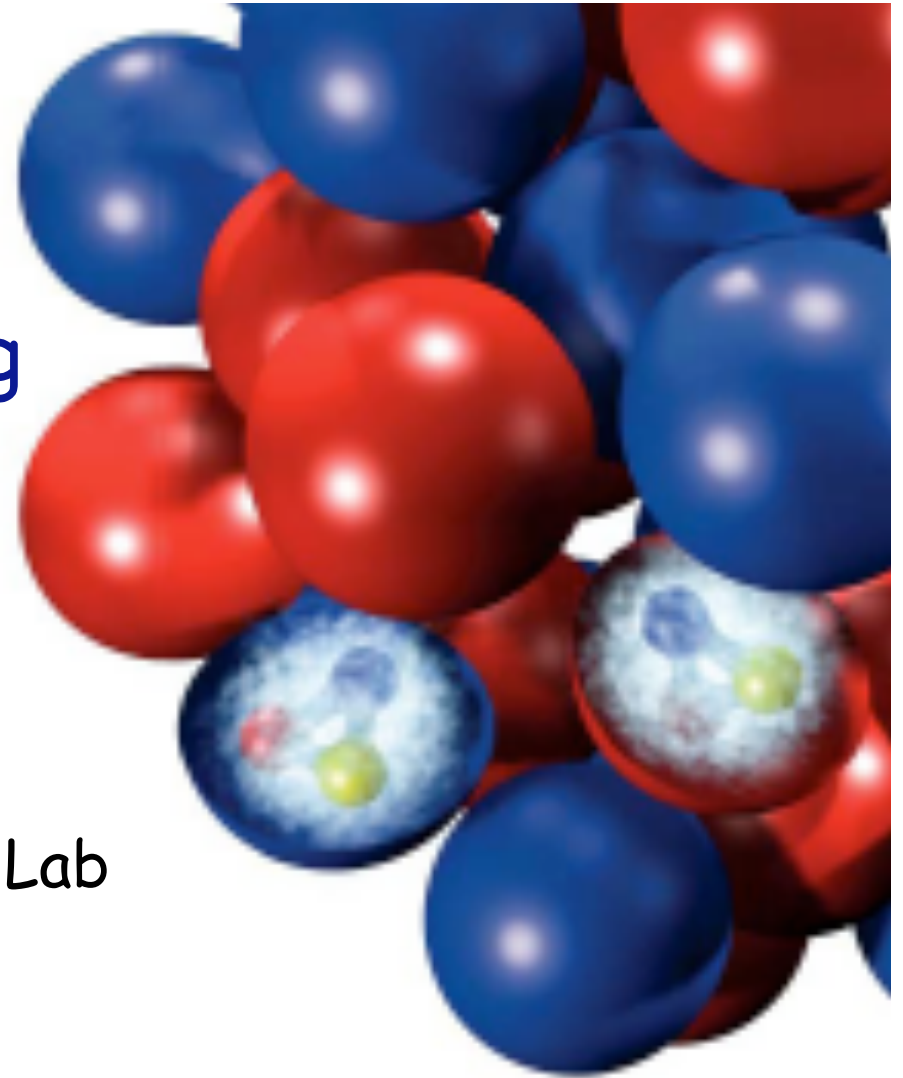
# Deep Inelastic Scattering

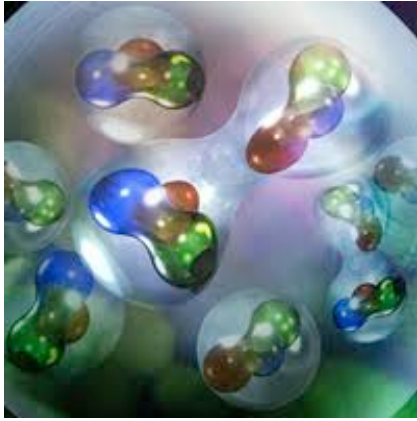
CTEQ Summer School

Madison, WI, July 2011

Cynthia Keppel

Hampton University / Jefferson Lab

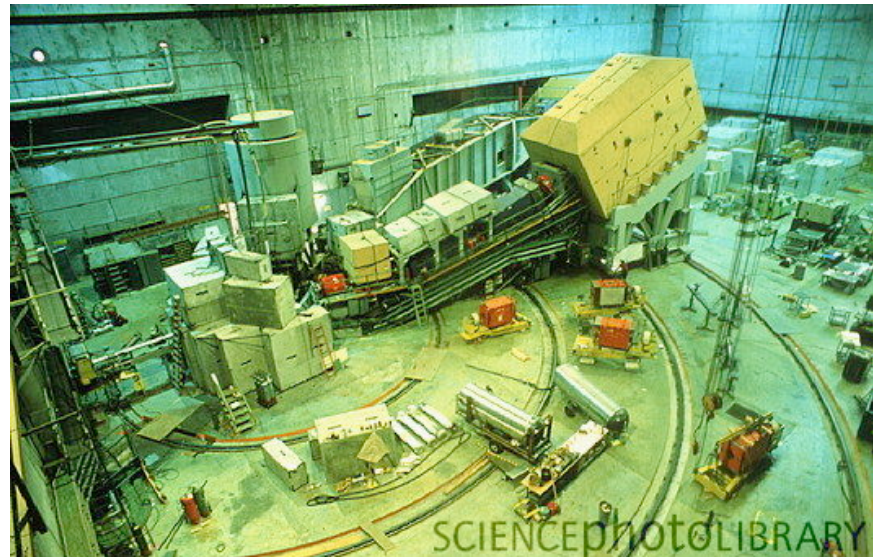




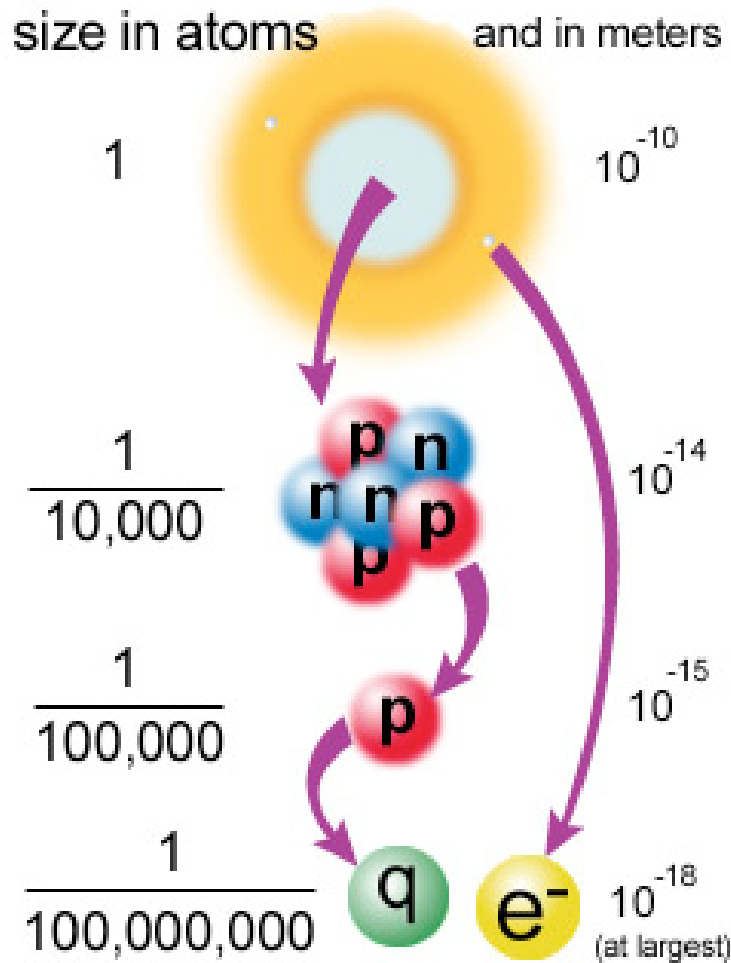
40 years of physics  
Maybe 100 experiments



...in an hour....



# How to probe the nucleon / quarks?



large momentum  $\rightarrow$  short distance  
(Uncertainty Principle at work!)

- Scatter high-energy lepton off a proton:

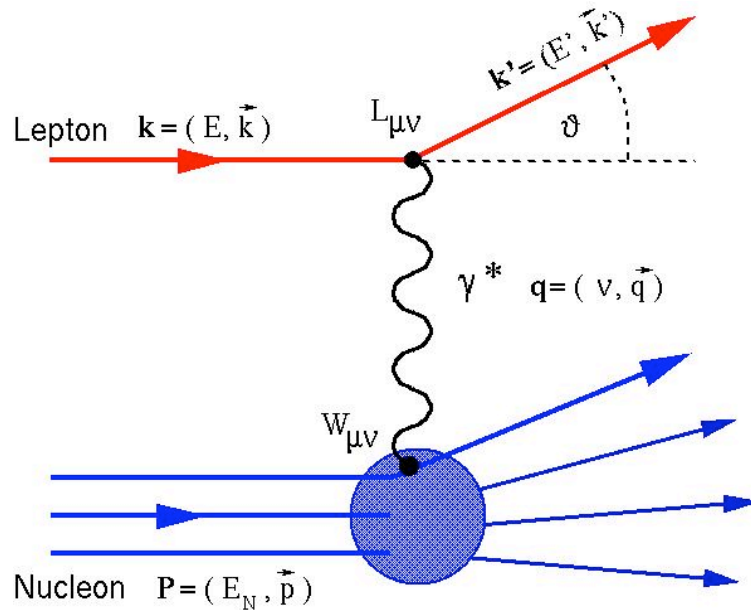
*Deep-Inelastic Scattering (DIS)*

- In DIS experiments point-like leptons + EM interactions which are well understood are used to probe hadronic structure (which isn't).

- Relevant scales:

$$d_{probed} \propto \hat{\lambda} = \frac{\hbar}{p} \approx 10^{-18} \text{ m}$$

# DIS Kinematics



$L_{\mu\nu}$  : lepton tensor

$W_{\mu\nu}$  : hadron tensor

*a virtual photon of four-momentum  $q$  is able to resolve structures of the order  $\hbar/\sqrt{q^2}$*

- Four-momentum transfer:

$$\begin{aligned}
 q^2 &= (E - E')^2 - (\vec{k} - \vec{k}') \cdot (\vec{k} - \vec{k}') = \\
 &= m_e^2 + m_e^2 - 2(EE' - |\vec{k}| |\vec{k}'| \cos \theta) = \\
 &\approx -4EE' \sin^2 \frac{\theta}{2} \equiv -Q^2
 \end{aligned}$$

- Mott Cross Section ( $\hbar c=1$ ):

$$\begin{aligned}
 \left(\frac{d\sigma}{d\Omega}\right)_{Mott} &= \frac{4\alpha^2 E'^2}{Q^4} \cos^2 \frac{\theta}{2} \cdot \frac{E'}{E} \\
 &= \frac{4\alpha^2 E'^2}{16E^2 E'^2 \sin^4 \frac{\theta}{2}} \cos^2 \frac{\theta}{2} \cdot \frac{1}{1 + \frac{E}{M}(1 - \cos \theta)} \\
 &= \frac{\alpha^2 \cos^2 \frac{\theta}{2}}{4E^2 \sin^4 \frac{\theta}{2}} \cdot \frac{1}{1 + \frac{E}{M}(2 \sin^2 \frac{\theta}{2})}
 \end{aligned}$$

Electron scattering of a spinless point particle

# Electron-Proton Scattering

- Effect of proton spin:

- Mott cross section:

$$\sigma_{Mott} = \frac{4\alpha^2 E'^2}{Q^4} \cos^2 \frac{\theta}{2} \cdot \frac{E'}{E} \equiv \sigma_{Ruth} \cos^2 \frac{\theta}{2}$$

- Effect proton spin  $\Rightarrow$

- helicity conservation
- 0 deg.:  $\sigma_{ep}(\text{magnetic}) \rightarrow 0$
- 180 deg.: spin-flip!

$$\begin{aligned} \sigma_{\text{magn}} &\sim \sigma_{\text{Ruth}} \sin^2(\theta/2) \\ &\sim \sigma_{\text{Mott}} \tan^2(\theta/2) \end{aligned}$$

$$\sigma_{e\text{-spin-}\frac{1}{2}} \propto \sigma_{\text{Mott}} \cdot \left[1 + 2\tau \tan^2 \frac{\theta}{2}\right]$$

- with  $\tau = \frac{Q^2}{4M^2 c^2}$

Mass of target = proton

- Nucleon form factors:

$$\sigma_{ep} = \sigma_{\text{Mott}} \left[ A(Q^2) + B(Q^2) \tan^2 \frac{\theta}{2} \right]$$

with:

$$A(Q^2) = \frac{G_E^2 + \tau G_M^2}{1 + \tau} \quad \text{and} \quad B(Q^2) = 2\tau G_M^2$$

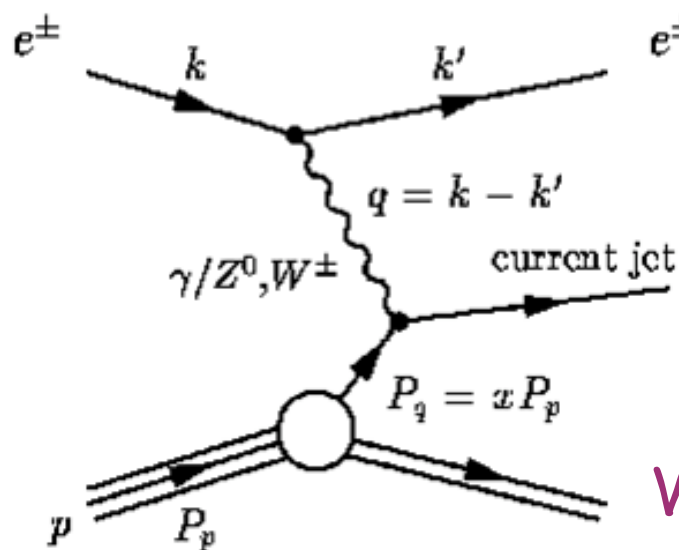
$$G_E^p(0) = 1 \quad \text{and} \quad G_M^p(0) = \frac{g_p}{2} \mu_N = 2.79 \mu_N$$

$$G_E^n(0) = 0 \quad \text{and} \quad G_M^n(0) = \frac{g_n}{2} \mu_N = -1.91 \mu_N$$

- The proton form factors have a substantial  $Q^2$  dependence.

# Measurement kinematics...

ep collision



Final electron energy

Initial electron energy

$$Q^2 = -q^2 = -(k - k')^2 = 2E_e E'_e (1 + \cos \theta_e)$$

Electron scattering angle

$$W^2 = (q + P_p)^2 = M^2 + 2M(E_e - E'_e) - Q^2$$

= invariant mass  
of final state hadronic system

Everything we need can be reconstructed from the measurement of  $E_e$ ,  $E'_e$  and  $\theta_e$ . (in principle) ->  
try a measurement!....

# Excited states of the nucleon

- Scatter 4.9 GeV electrons from a hydrogen target. At 10 degrees, measure ENERGY of scattered electrons
- Evaluate invariant energy of virtual-photon proton system

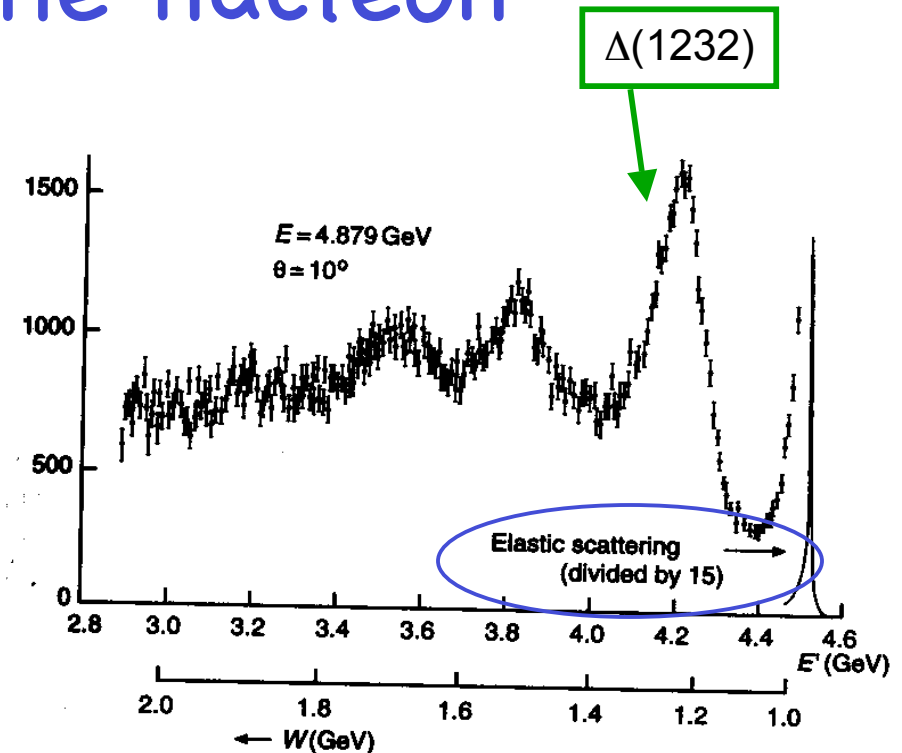
$$W^2 = 10.06 - 2.03E'_e \quad *$$

- In the lab-frame:  $P = (m_p, 0) \rightarrow$

$$W^2 = (P_p + q)^2 = P^2 + 2Pq + q^2$$

$$W^2 = m_p^2 + 2m_p \nu - Q^2$$

\* Convince yourself of this!



- Observe excited resonance states:

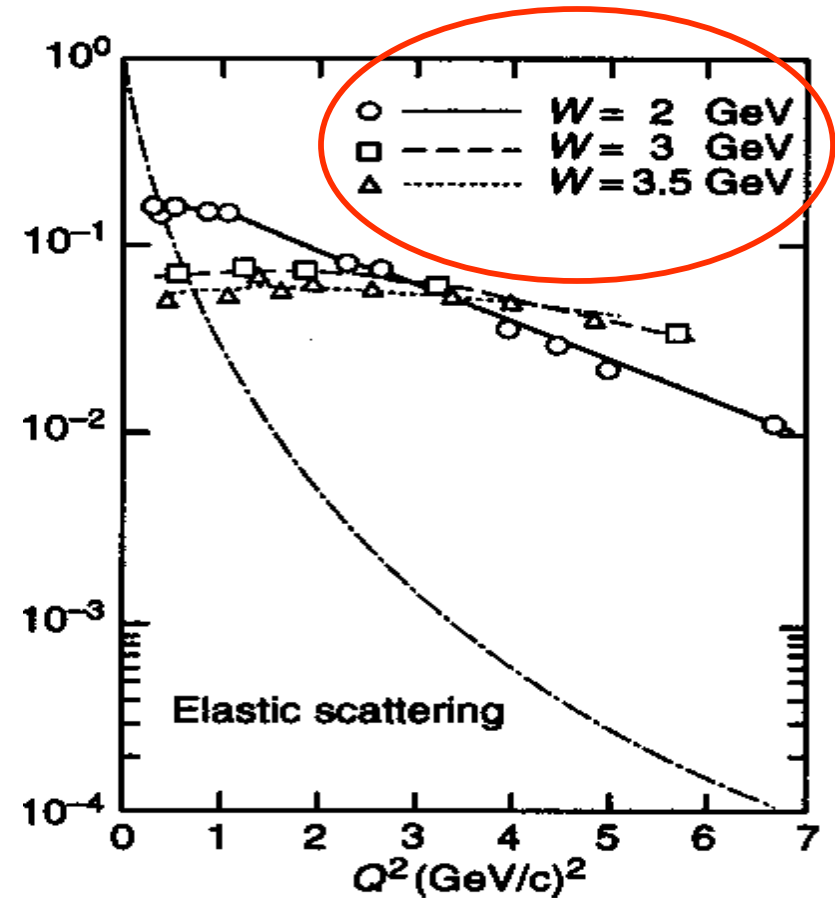
Nucleons are composite

→ What do we see in the data for  $W > 2$  GeV ?

- First SLAC experiment ('69):
  - expected from proton form factor:

$$\frac{d\sigma / dE' d\Omega}{(d\sigma / d\Omega)_{\text{Mott}}} = \left( \frac{1}{(1 + Q^2 / 0.71)^2} \right)^2 \propto Q^{-8}$$

- First data show big surprise:
  - very weak  $Q^2$ -dependence
  - form factor  $\rightarrow 1$ !
  - scattering off point-like objects?

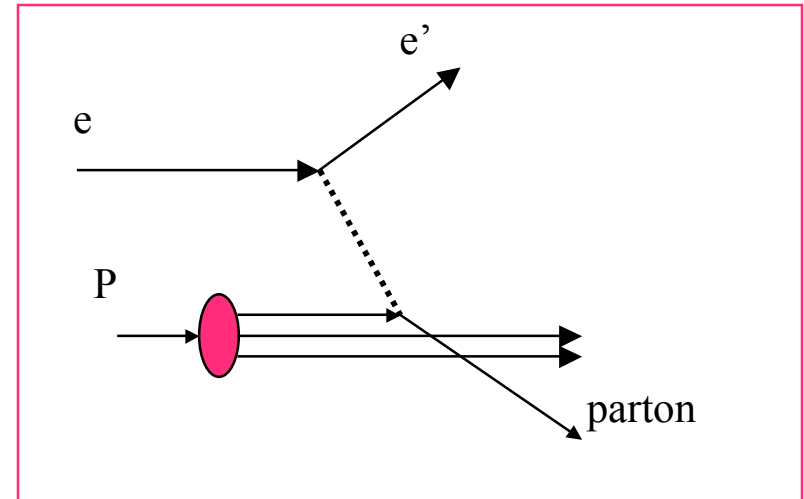


... introduce a clever model!



# The Quark-Parton Model

- Assumptions:
  - Proton constituent = Parton
  - Elastic scattering from a quasi-free spin-1/2 quark in the proton
  - Neglect masses and  $p_T$ 's, “infinite momentum frame”



- Lets assume:  $p_{quark} = xP_{proton}$

$$(xP + q)^2 = p_{quark}^2 = m_{quark}^2 \approx 0$$

- Since  $xP^2 \leq M^2 \ll Q^2$  it follows:

$$2xP \cdot q + q^2 \approx 0 \Rightarrow x = \frac{Q^2}{2Pq} = \frac{Q^2}{2M\nu}$$

$$\nu = (q \cdot p)/M = E_e - E_{e'}$$

*Definition Bjorken scaling variable*

- Check limiting case:

$$W^2 = M_p^2 + 2M_p\nu - Q^2 \xrightarrow{x \rightarrow 1} M_p^2$$

- Therefore:

$x = 1$ : elastic scattering

and  $0 < x < 1$

# Structure Functions $F_1, F_2$

- Introduce dimensionless structure functions:

$$F_1 = MW_1 \text{ and } F_2 = \nu W_2 \Rightarrow \frac{d\sigma}{dE' d\Omega} = \left( \frac{d\sigma}{d\Omega} \right)_M \frac{1}{\nu} \left[ F_2(x) + \frac{2\nu}{M} F_1(x) \tan^2(\theta/2) \right]$$

- Rewrite this in terms of :  $\tau = Q^2 / 4m_{quark}^2$  (elastic  $e$ - $q$  scatt.:  $2m_q \nu = Q^2$ )

$$\frac{d\sigma}{dE' d\Omega} / \left( \frac{d\sigma}{d\Omega} \right)_M = \frac{1}{\nu} \left[ F_2(x) + 2 \frac{Q^2}{4m_q^2} \frac{4m_q^2}{Q^2} \frac{\nu}{M} F_1(x) \tan^2(\theta/2) \right] =$$

$$= \frac{1}{\nu} \left[ F_2(x) + 2\tau \cdot 2xF_1(x) \tan^2(\theta/2) \right]$$

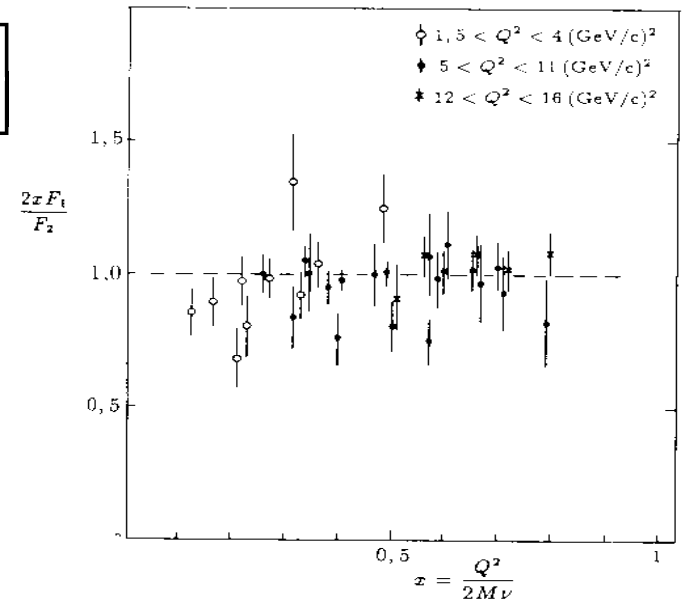
if  $F_2(x) = 2xF_1(x)$

$$= \frac{1}{\nu} F_2(x) \left[ 1 + 2\tau \tan^2(\theta/2) \right]$$

- Experimental data for  $2xF_1(x) / F_2(x)$

→ *quarks have spin 1/2*

(if bosons: no spin-flip  $\Rightarrow F_1(x) = 0$ )

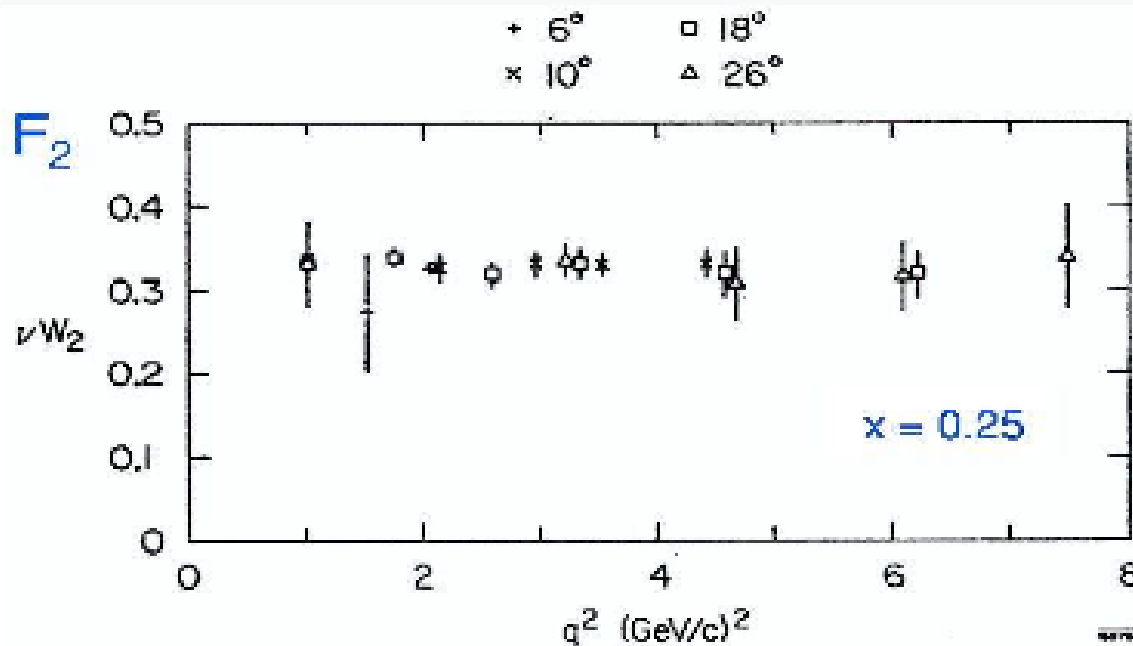


# Interpretation of $F_1(x)$ and $F_2(x)$

- In the quark-parton model:

*Quark momentum  
distribution*

$$F_1(x) = \sum_f \frac{1}{2} z_f^2 [q_f(x) + \bar{q}_f(x)]$$



J. T. Friedman + H. W. Kendall,  
Ann. Rev. Nucl. Sci. **22** (1972) 203

# The quark structure of nucleons

- Quark quantum numbers:

- Spin:  $\frac{1}{2} \Rightarrow S_{p,n} = (\uparrow \uparrow \downarrow) = \frac{1}{2}$
- Isospin:  $\frac{1}{2} \Rightarrow I_{p,n} = (\uparrow \uparrow \downarrow) = \frac{1}{2}$

- Why fractional charges?

- Extreme baryons:  $Z = (-1, +2)$

$$-1 \leq 3z_q \leq +2 \Rightarrow -\frac{1}{3} \leq z_q \leq +\frac{2}{3}$$

- Assign:  $z_{up} = +\frac{2}{3}, z_{down} = -\frac{1}{3}$

- Three families:

$$\begin{pmatrix} u \\ d \end{pmatrix} \begin{pmatrix} c \\ s \end{pmatrix} \begin{pmatrix} t \\ b \end{pmatrix} \Rightarrow z = +\frac{2}{3}; m_u \ll m_c (\approx 1.5 \text{ GeV}) \ll m_t$$

$$\Rightarrow z = -\frac{1}{3}; m_d \ll m_s (\approx 0.3 \text{ GeV}) \ll m_b$$

- $m_{c,b,t} \gg m_{u,d,s}$  : no role in p,n

- Structure functions:

$$F_2^p = x \left[ \frac{1}{9} (d_v^p + d_s^p + \bar{d}_s^p) + \frac{4}{9} (u_v^p + u_s^p + \bar{u}_s^p) + \frac{1}{9} (s_s + \bar{s}_s) \right]$$

$$F_2^n = x \left[ \frac{1}{9} (d_v^n + d_s^n + \bar{d}_s^n) + \frac{4}{9} (u_v^n + u_s^n + \bar{u}_s^n) + \frac{1}{9} (s_s + \bar{s}_s) \right]$$

- Isospin symmetry:

$$u_v^n = d_v^p, d_v^n = u_v^p, \bar{u}_s^n = \bar{d}_s^n = \bar{u}_s^p = \bar{d}_s^p$$

- ‘Average’ nucleon  $F_2(x)$   
with  $q(x) = q_v(x) + q_s(x)$  etc.

$$F_2^N = \frac{1}{2} (F_2^p + F_2^n)$$

$$= \frac{5}{18} x \cdot \sum_{u,d} (q(x) + \bar{q}(x)) + \frac{1}{9} x \cdot [s_s(x) + \bar{s}_s(x)]$$

- Neutrinos:

$$F_2^v = x [(d_v + d_s + \bar{d}_s) + (u_v + u_s + \bar{u}_s) + (s_s + \bar{s}_s)]$$

$$= x [(d + u + s) + (\bar{d}_s + \bar{u}_s + \bar{s}_s)] = x \sum_{u,d,s} (q(x) + \bar{q}(x))$$

# Fractional quark charges

- Neglect strange quarks  $\Rightarrow$

$$\frac{F_2^{e,N}}{F_2^{\nu,N}} \approx \frac{5}{18}$$

- Data confirm factor 5/18:

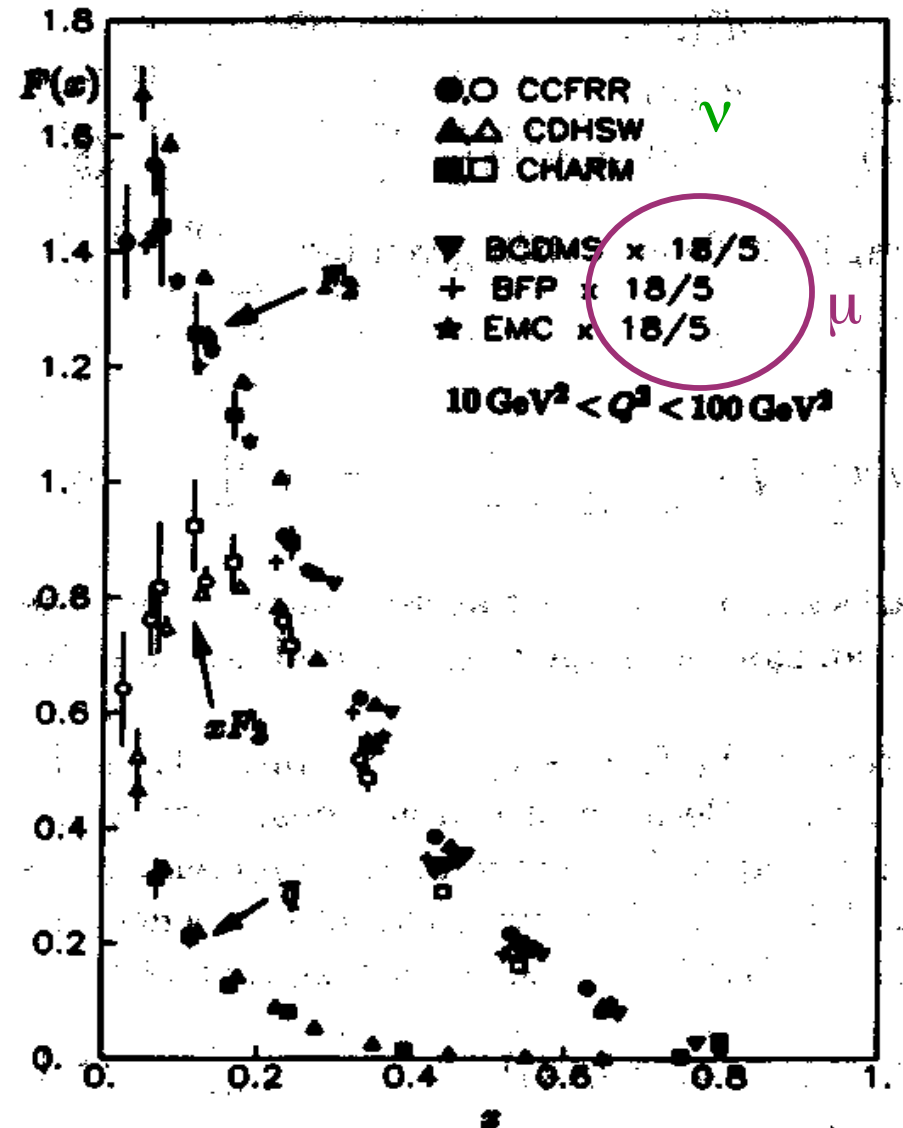
*Evidence for fractional charges*

- Fraction of proton momentum carried by quarks:

$$\int_0^1 F_2^{\nu,N}(x) dx = \frac{18}{5} \int_0^1 F_2^{e,N}(x) dx \approx 0.5$$

- 50% of momentum due to non-electro-weak particles:

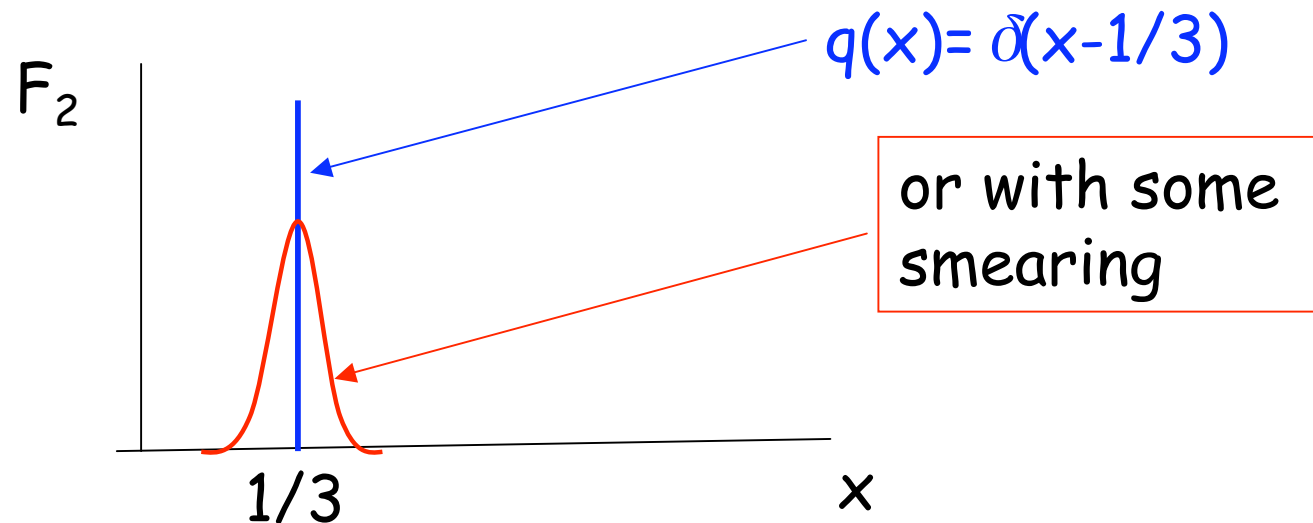
*Evidence for gluons*



**IF**, proton was made of 3 quarks each with 1/3 of proton's momentum:

$$F_2 = x \sum (q(x) + \cancel{q(\bar{x})}) e_q^2$$

no anti-quark!



The partons are point-like and incoherent then  $Q^2$  shouldn't matter.

→ **Bjorken scaling**:  $F_2$  has no  $Q^2$  dependence.

Thus far, we've covered:

- Some history
- Some key results
- Basic predictions of the parton model

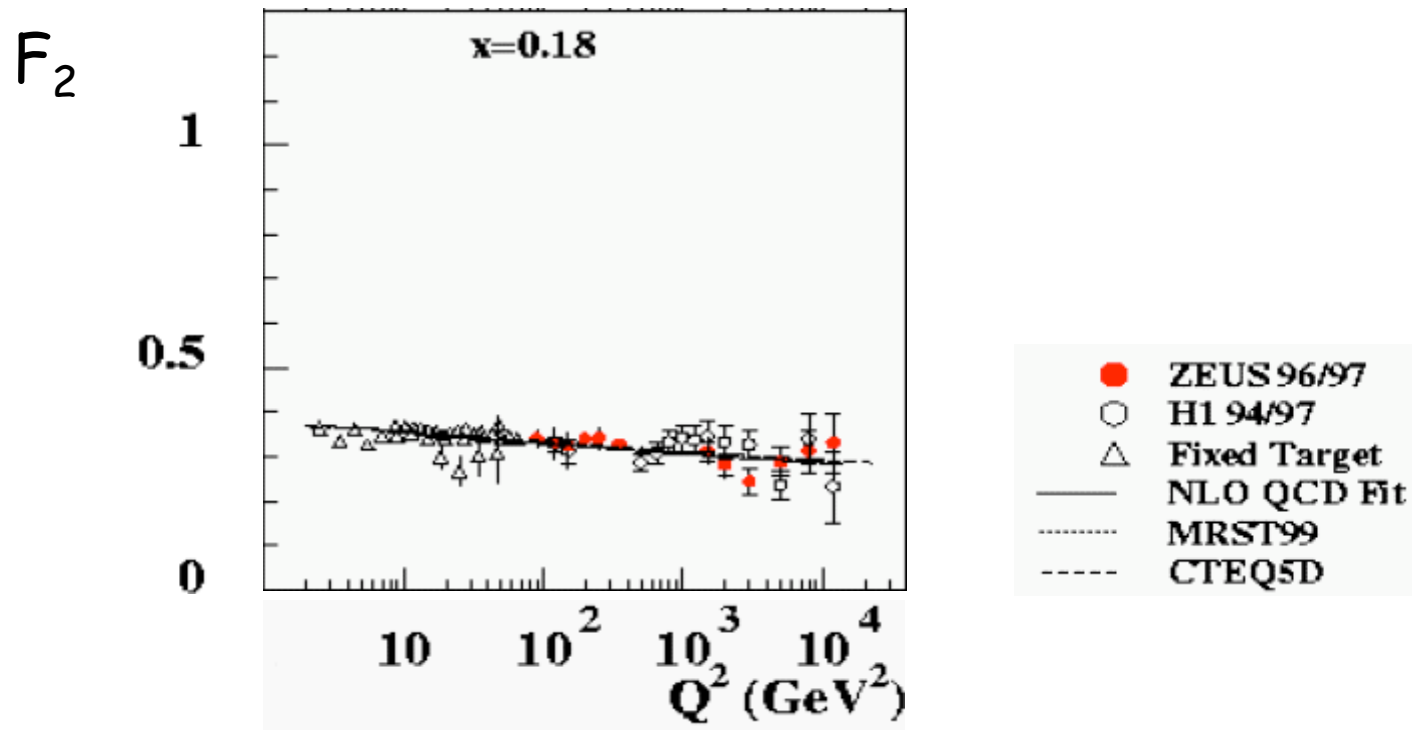
The parton model assumes:

- Non-interacting point-like particles
- Bjorken scaling, i.e.  $F_2(x, Q^2) = F_2(x)$
- Fractional charges (if partons=quarks)
- Spin 1/2
- Valence and sea quark structure (sum rules)

Makes key predictions that can be tested by experiment.....

Let's look at some data→

## Proton Structure Function $F_2$

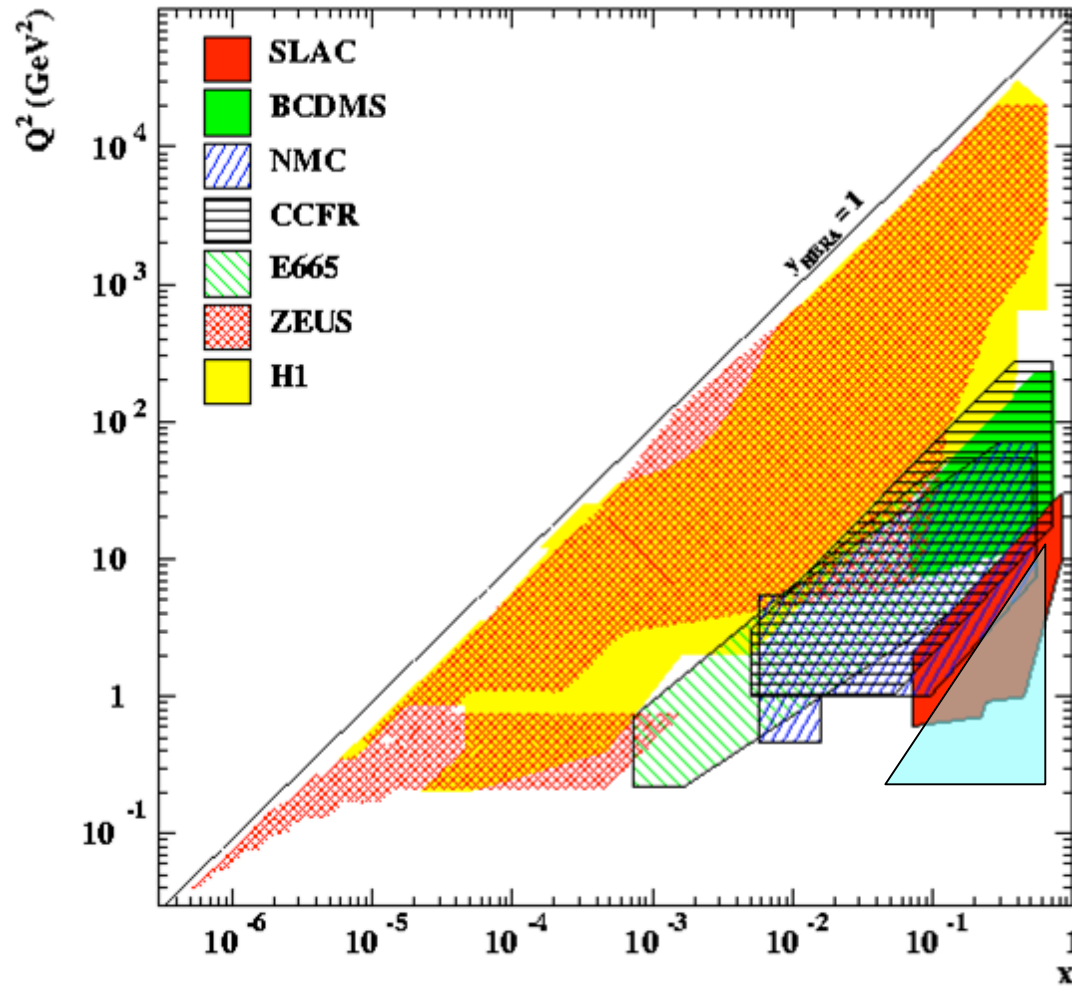


Seems to be.... ..uh oh...

Lovely movies are from R. Yoshida, CTEQ Summer School 2007



# Deep Inelastic Scattering experiments

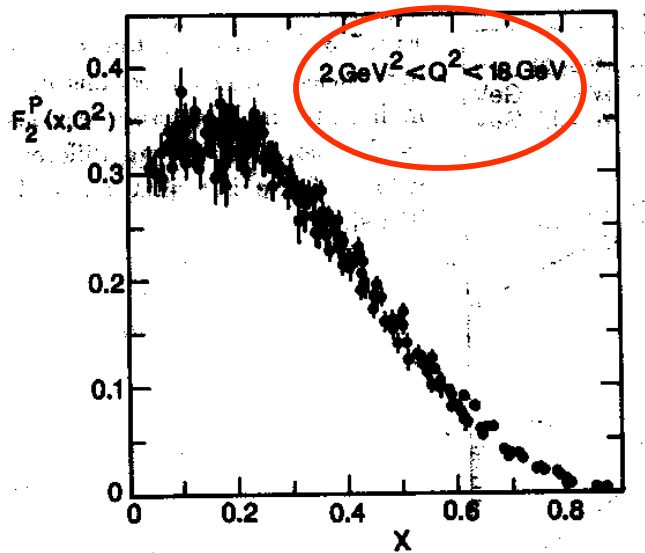


Fixed target DIS at SLAC, FNAL, CERN, HERA collider DIS at SLAC, FNAL, CERN, HERA, 1992-2007  
New JLab

# Modern data

PDG 2002

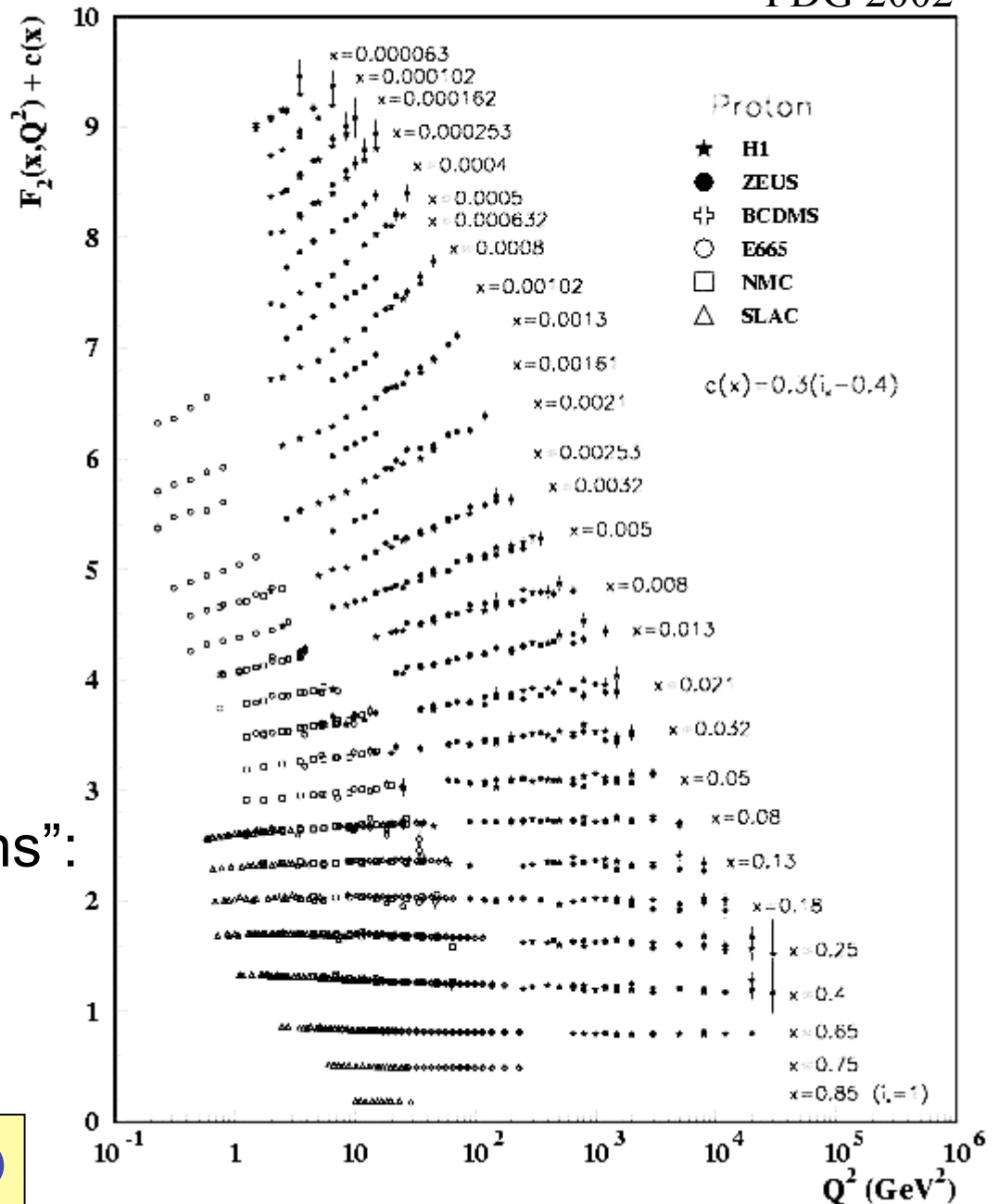
- First data (1980):



- Now.. “Scaling violations”:

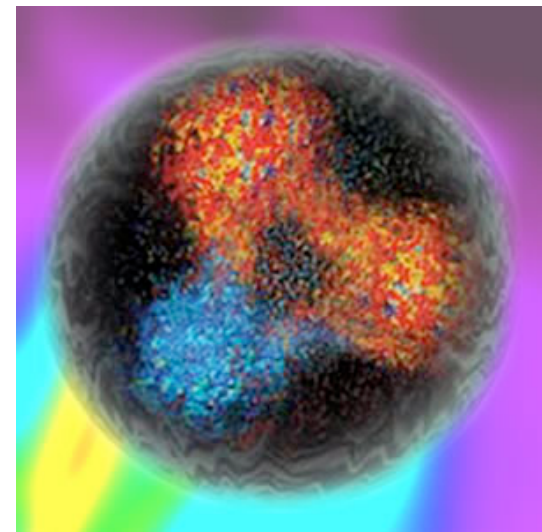
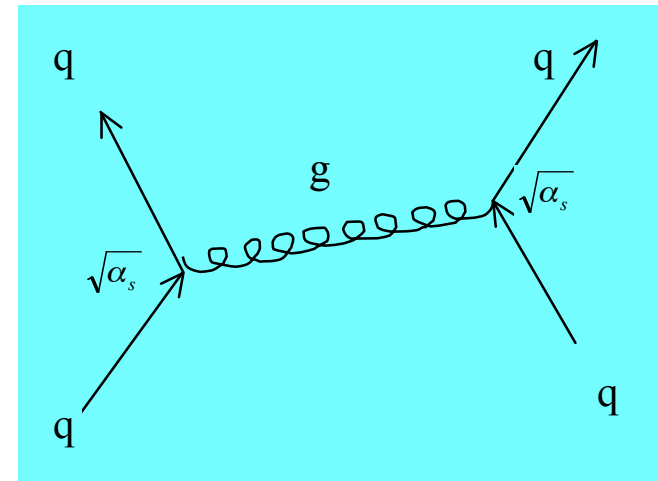
  - weak  $Q^2$  dependence
  - rise at low  $x$
  - what physics??

..... QCD



# Quantum Chromodynamics (QCD)

- Field theory for strong interaction:
  - quarks interact by gluon exchange
  - quarks carry a 'colour' charge
  - exchange bosons (gluons) carry colour  $\Rightarrow$  self-interactions (cf. QED!)
- Hadrons are colour neutral:
  - $R\bar{R}$ ,  $B\bar{B}$ ,  $G\bar{G}$  or  $RGB$
  - leads to confinement:  
 $|q\rangle$ ,  $|qq\rangle$  or  $|qq\bar{q}\rangle$  forbidden
- Effective strength  $\sim$  #gluons exch.
  - low  $Q^2$ : more  $g$ 's: large eff. coupling
  - high  $Q^2$ : few  $g$ 's: small eff. coupling



# The QCD Lagrangian

$$\mathcal{L}_{qcd} = i \sum_q \bar{\psi}_q^j \gamma^\mu (D_\mu)_{jk} \psi_q^k - \sum_q m_q \bar{\psi}_q^j \psi_q^k - \frac{1}{4} G_{\mu\nu}^a G_a^{\mu\nu}$$

( $j, k = 1, 2, 3$  refer to colour;  $q = u, d, s$  refers to flavour;  $a = 1, \dots, 8$  to gluon fields)

Covariant derivative:

$$D_\mu = \partial_\mu + i \frac{1}{2} g_s \lambda_a G_\mu^a$$

Free quarks

$$G_{ii}^a = \underbrace{\partial_\mu G_\nu^a - \partial_\nu G_\mu^a}_{\text{Gluon kinetic energy term}} - \underbrace{g_s f_{abc} G_\mu^a G_\nu^b}_{\text{Gluon self-interaction}}$$

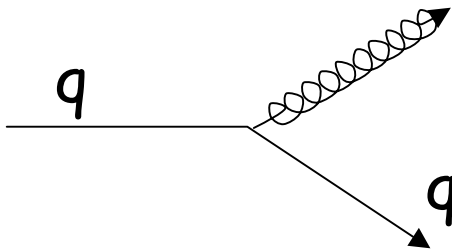
qg-interactions  
SU(3) generators:

$$\lambda_1 = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad \lambda_2 = \begin{pmatrix} 0 & -i & 0 \\ i & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad \lambda_3 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad \lambda_4 = \begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix}$$

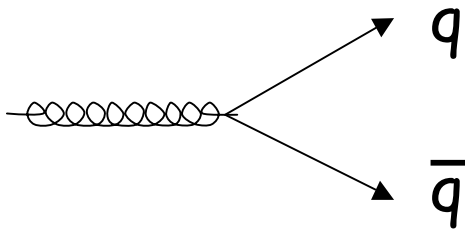
$$([\lambda_a, \lambda_b] = i \frac{1}{2} f_{abc} \lambda_c) \quad \lambda_5 = \begin{pmatrix} 0 & 0 & -i \\ 0 & 0 & 0 \\ i & 0 & 0 \end{pmatrix} \quad \lambda_6 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} \quad \lambda_7 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & -i \\ 0 & i & 0 \end{pmatrix} \quad \lambda_8 = \frac{1}{\sqrt{3}} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix}$$

So what does this mean..?

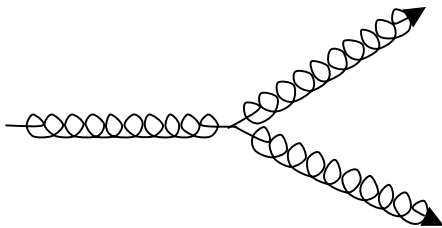
QCD brings new possibilities:



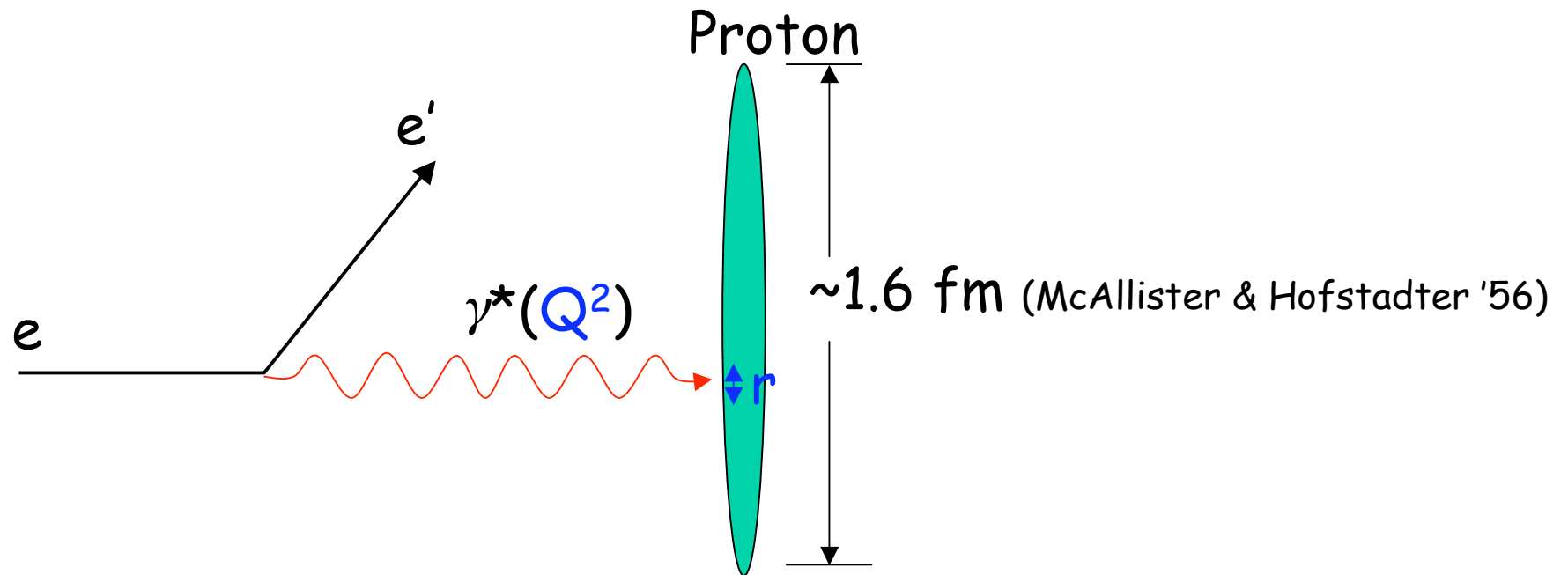
quarks can radiate gluons



gluons can produce  $q\bar{q}$  pairs



gluons can radiate gluons!



Virtuality (4-momentum transfer)  $Q$  gives the distance scale  $r$  at which the proton is probed.

$$r \approx \hbar c / Q = 0.2 \text{ fm} / Q [\text{GeV}]$$

CERN, FNAL fixed target DIS:

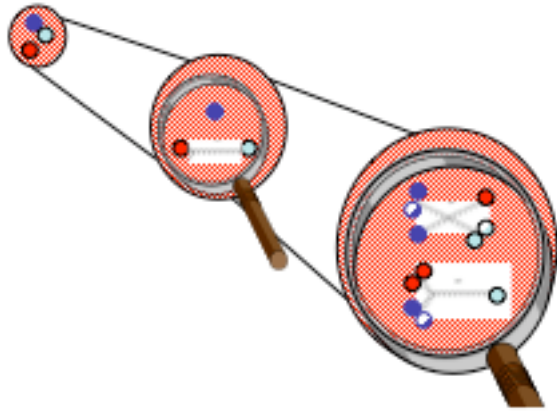
$r_{\min} \approx 1/100$  proton dia.

HERA ep collider DIS:

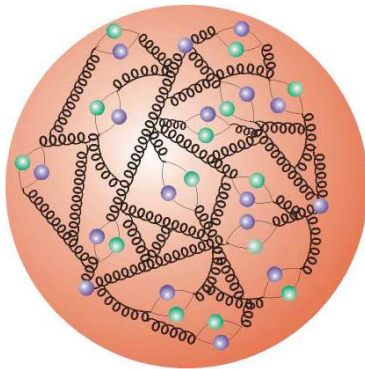
$r_{\min} \approx 1/1000$  proton dia.

HERA:  $E_e = 27.5 \text{ GeV}$ ,  $E_p = 920 \text{ GeV}$

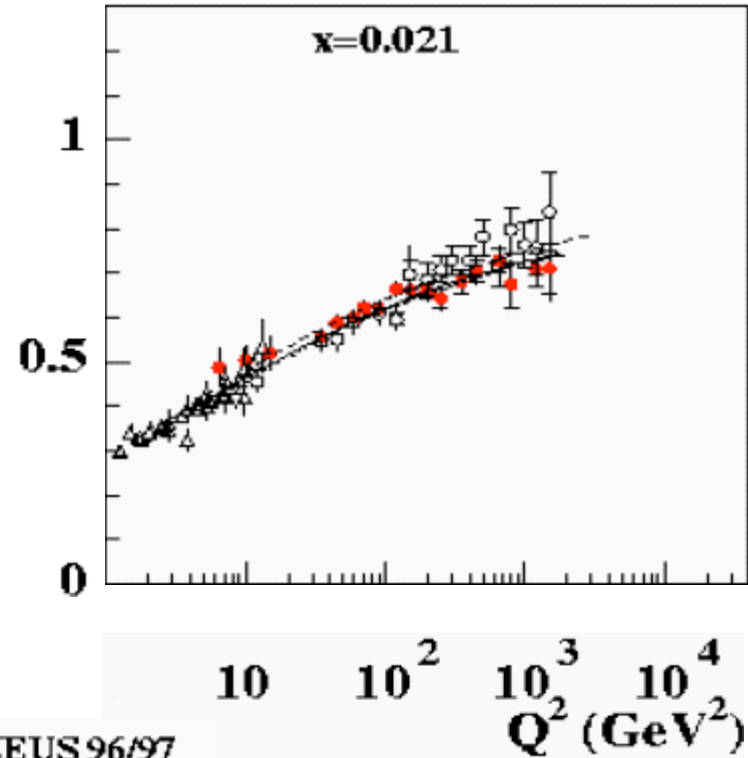
(Uncertainty Principle again)



Higher the resolution  
(i.e. higher the  $Q^2$ )  
more low  $x$  partons we  
"see".

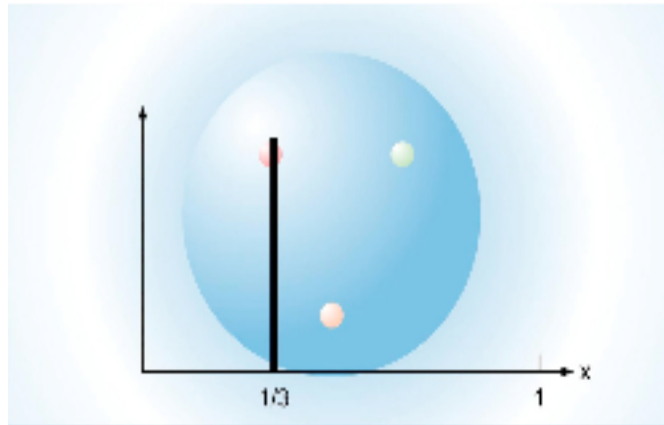
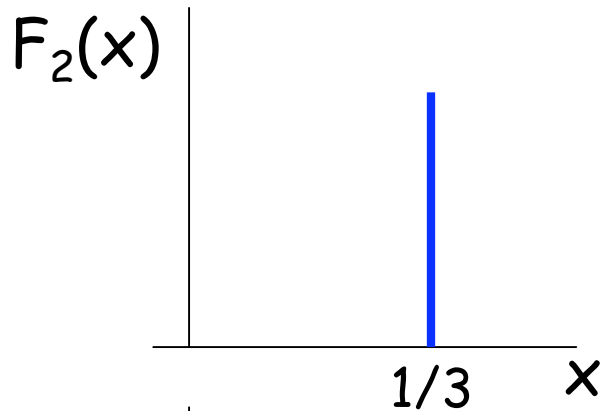


$F_2$

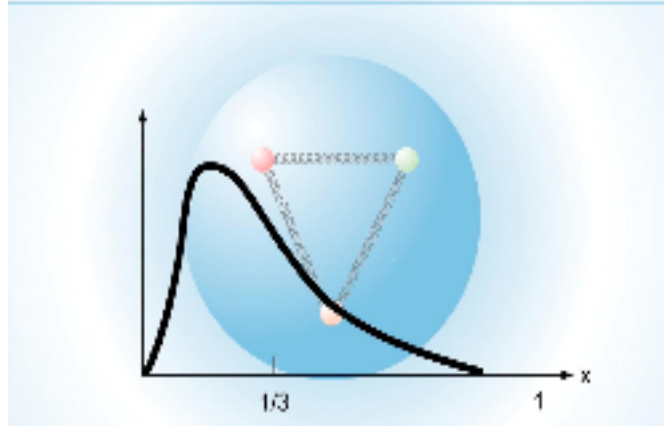
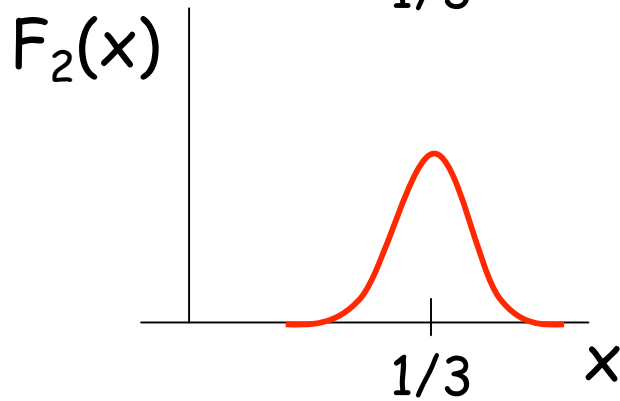


- ZEUS 96/97
- H1 94/97
- △ Fixed Target
- NLO QCD Fit
- ⋯ MRST99
- - - CTEQ5D

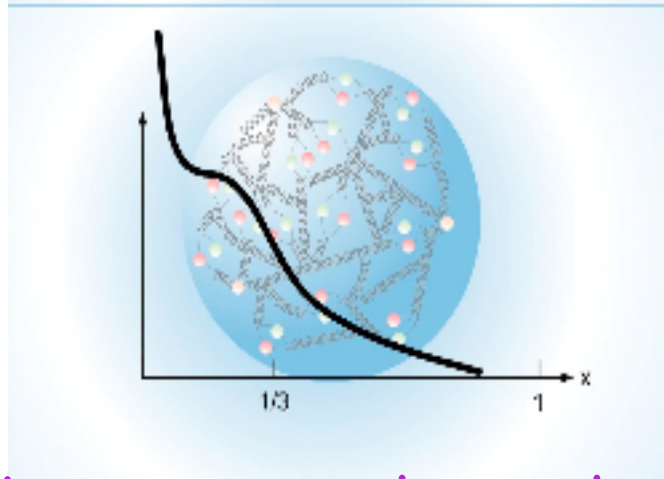
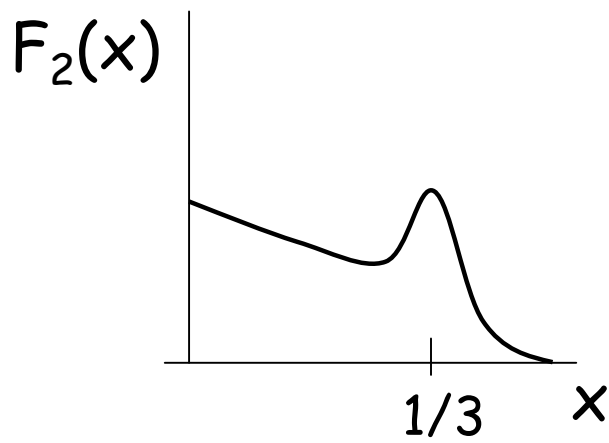
So what do we expect  $F_2$  as a function of  $x$  at  
a fixed  $Q^2$  to look like?



Three quarks with  $1/3$  of total proton momentum each.



Three quarks with some momentum smearing.



The three quarks radiate partons at low  $x$ .

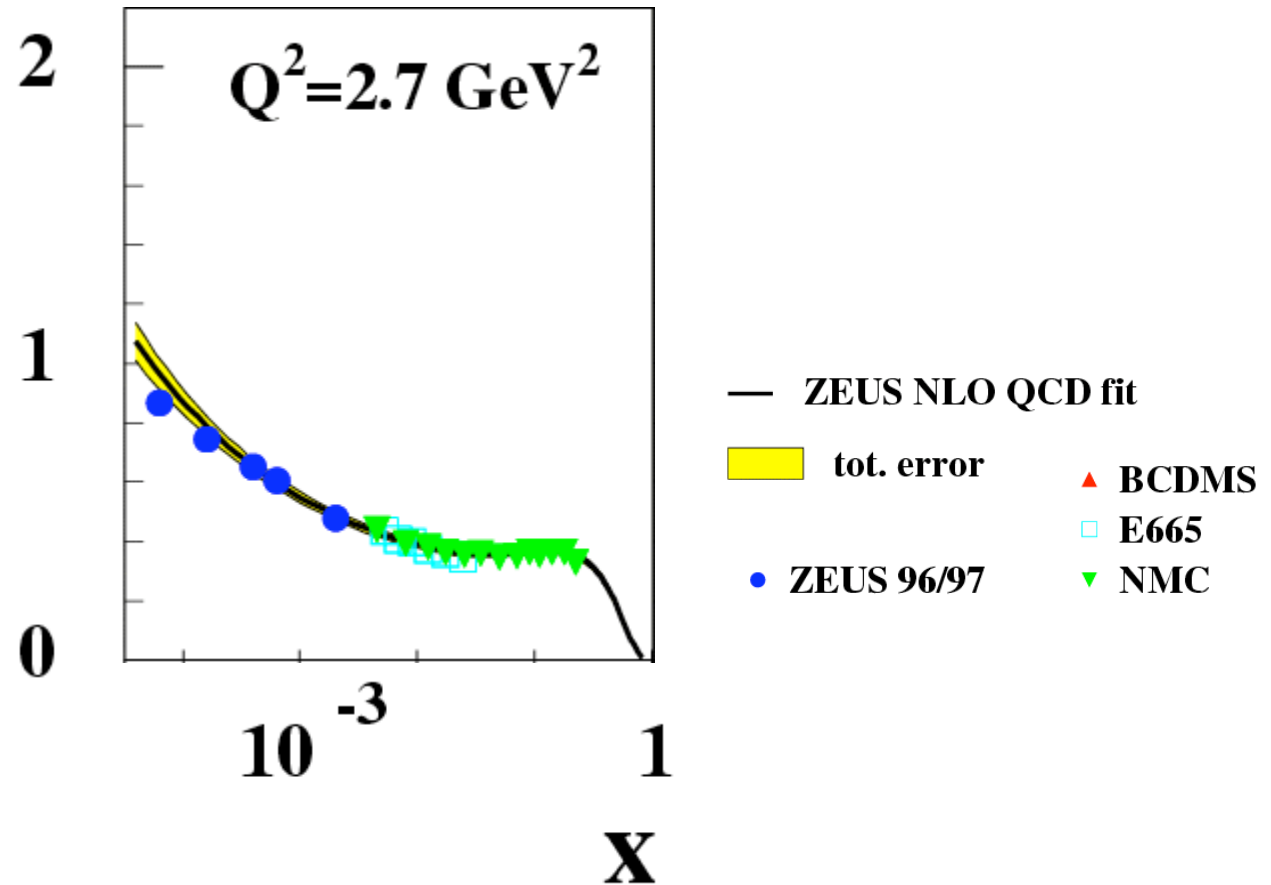
....The answer depends on the  $Q^2$ !



# Proton Structure Function $F_2$

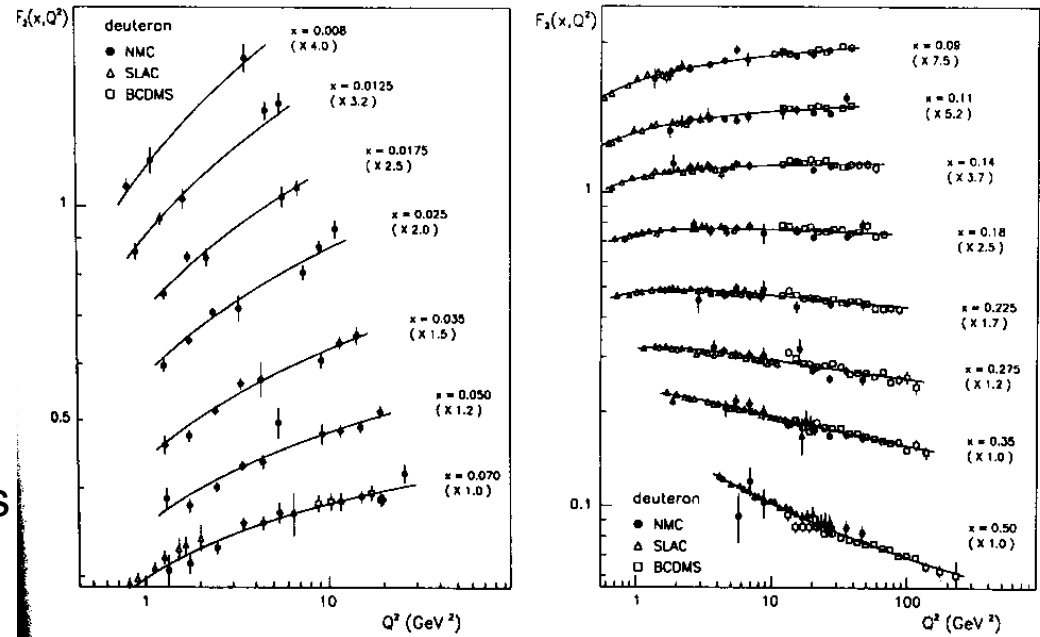
How this change with  $Q^2$  happens quantitatively described by the:

Dokshitzer-Gribov-Lipatov-Altarelli-Parisi (DGLAP) equations



# QCD predictions: scaling violations

- Originally:  $F_2 = F_2(x)$ 
  - but also  $Q^2$ -dependence
- Why scaling violations?
  - if  $Q^2$  increases:
    - $\Rightarrow$  more resolution ( $\sim 1/Q^2$ )
    - $\Rightarrow$  more sea quarks + gluons
- QCD improved QPM:

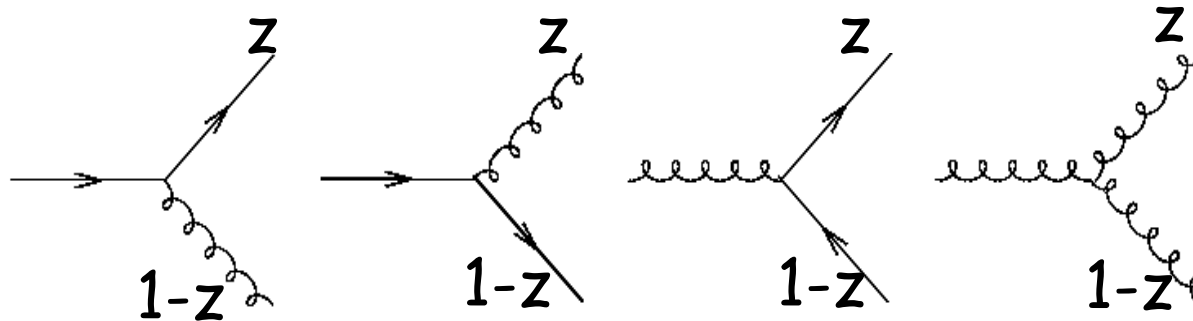


$$\frac{F_2(x, Q^2)}{x} = \left| \begin{array}{c} \text{wavy line} \\ \text{arrow} \end{array} \right|^2 + \left| \begin{array}{c} \text{wavy line} \\ \text{arrow} \\ \text{loop} \end{array} \right|^2 + \left| \begin{array}{c} \text{wavy line} \\ \text{arrow} \\ \text{loop} \end{array} \right|^2$$

- Officially known as: Altarelli-Parisi Equations (“DGLAP”)

DGLAP equations are easy to “understand” intuitively..

First we have four “splitting functions”



$P_{ab}(z)$  : the probability that parton **a** will radiate a parton **b** with the fraction  $z$  of the original momentum carried by **a**.

These additional contributions to  $F_2(x, Q^2)$  can be calculated.

Now DGLAP equations (schematically)

$$\frac{dq_f(x, Q^2)}{d \ln Q^2} = \alpha_s [q_f \otimes P_{qq} + g \otimes P_{gq}]$$

convolution

strong coupling constant

$q_f$  is the quark density summed over all active flavors

Change of quark distribution  $q$  with  $Q^2$  is given by the probability that  $q$  and  $g$  radiate  $q$ .

Same for gluons:

$$\frac{dg(x, Q^2)}{d \ln Q^2} = \alpha_s [\sum q_f \otimes P_{qg} + g \otimes P_{gg}]$$

Violation of Bjorken scaling predicted by QCD - logarithmic dependence, not dramatic

DGLAP fit (or QCD fit) extracts the parton distributions from measurements.

(CTEQ, for instance :)

Basically, this is accomplished in two steps:

Step 1: parametrise the parton momentum density

$f(x)$  at some  $Q^2$ . e.g.  $f(x) = p_1 x^{p_2} (1-x)^{p_3} (1+p_4 \sqrt{x} + p_5 x)$

$u_v(x)$	u-valence	} "The original three quarks"
$d_v(x)$	d-valence	
$g(x)$	gluon	
$S(x)$	"sea" (i.e. non valence) quarks	

Step 2: find the parameters by fitting to DIS (and other) data using DGLAP equations to evolve  $f(x)$  in  $Q^2$ .

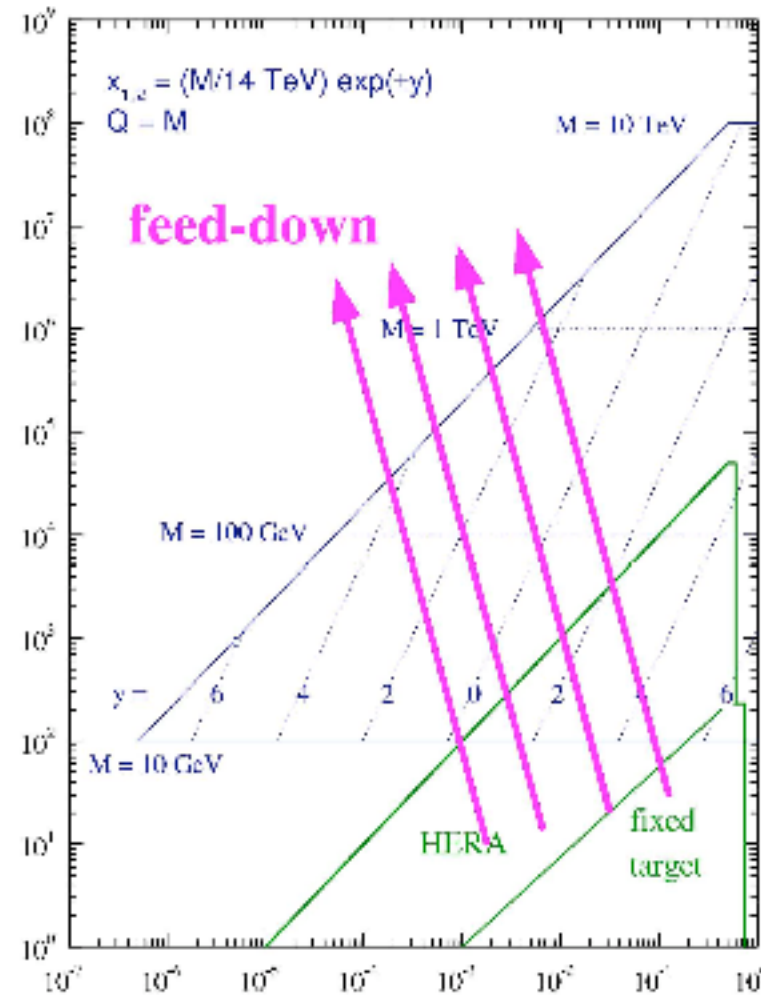
$$\frac{\partial f_q(x, Q^2)}{\partial \log Q^2} = \frac{\alpha_s}{2\pi} \int_x^1 \frac{dy}{y} f_q(y, Q^2) P_{qq}\left(\frac{x}{y}\right) + \frac{\alpha_s}{2\pi} \int_x^1 \frac{dy}{y} g(y, Q^2) P_{gq}\left(\frac{x}{y}\right)$$

$$\frac{\partial g(x, Q^2)}{\partial \log Q^2} = \frac{\alpha_s}{2\pi} \int_x^1 \frac{dy}{y} f_q(y, Q^2) P_{gq}\left(\frac{x}{y}\right) + \frac{\alpha_s}{2\pi} \int_x^1 \frac{dy}{y} g(y, Q^2) P_{gg}\left(\frac{x}{y}\right)$$

QCD fits  
of  $F_2(x, Q^2)$   
data

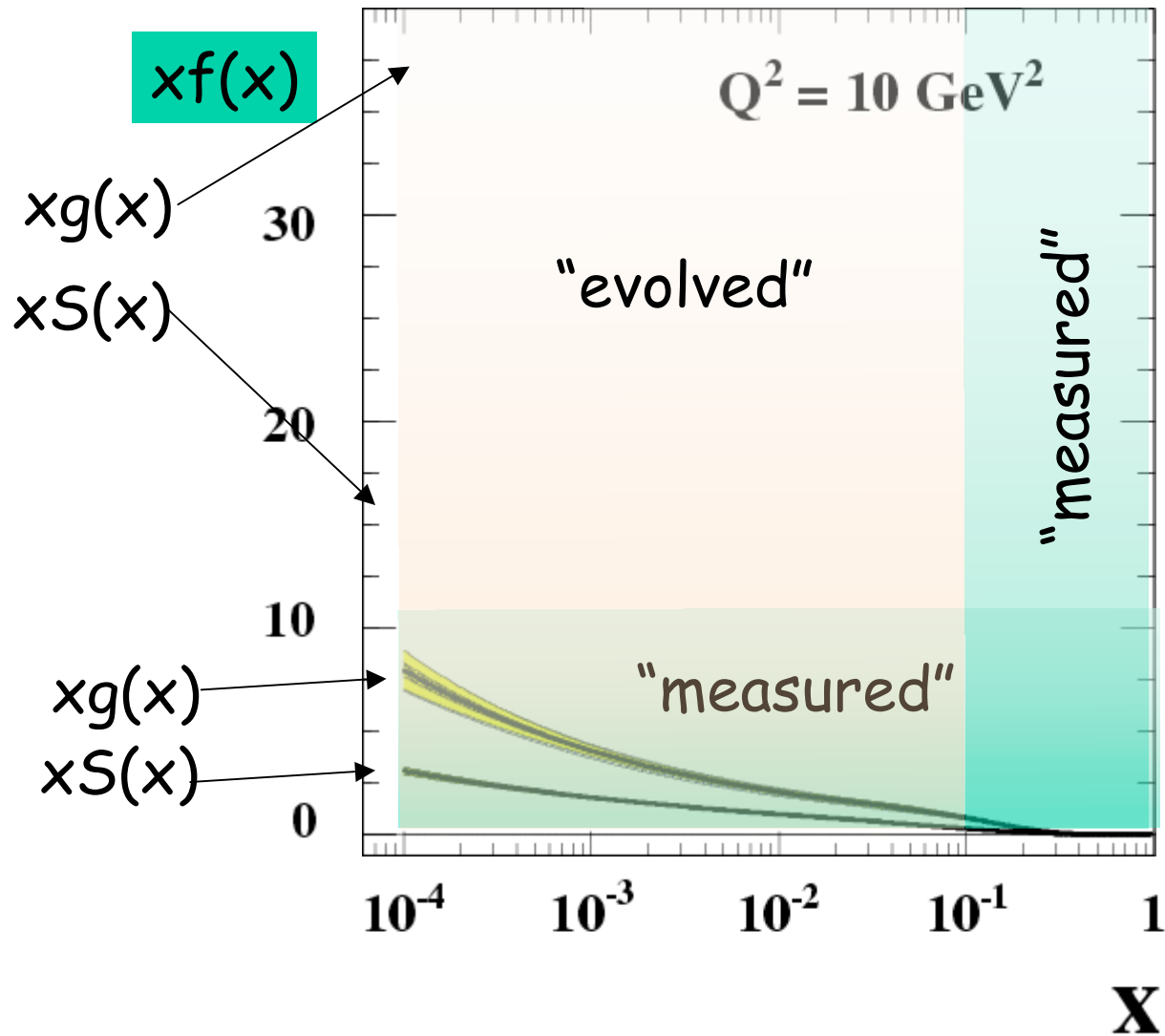
The DGLAP evolution equations are extremely useful as they allow structure functions measured by one experiment to be compared to other measurements - and to be extrapolated to predict what will happen in regions where no measurements exist, e.g. LHC.

$Q^2$

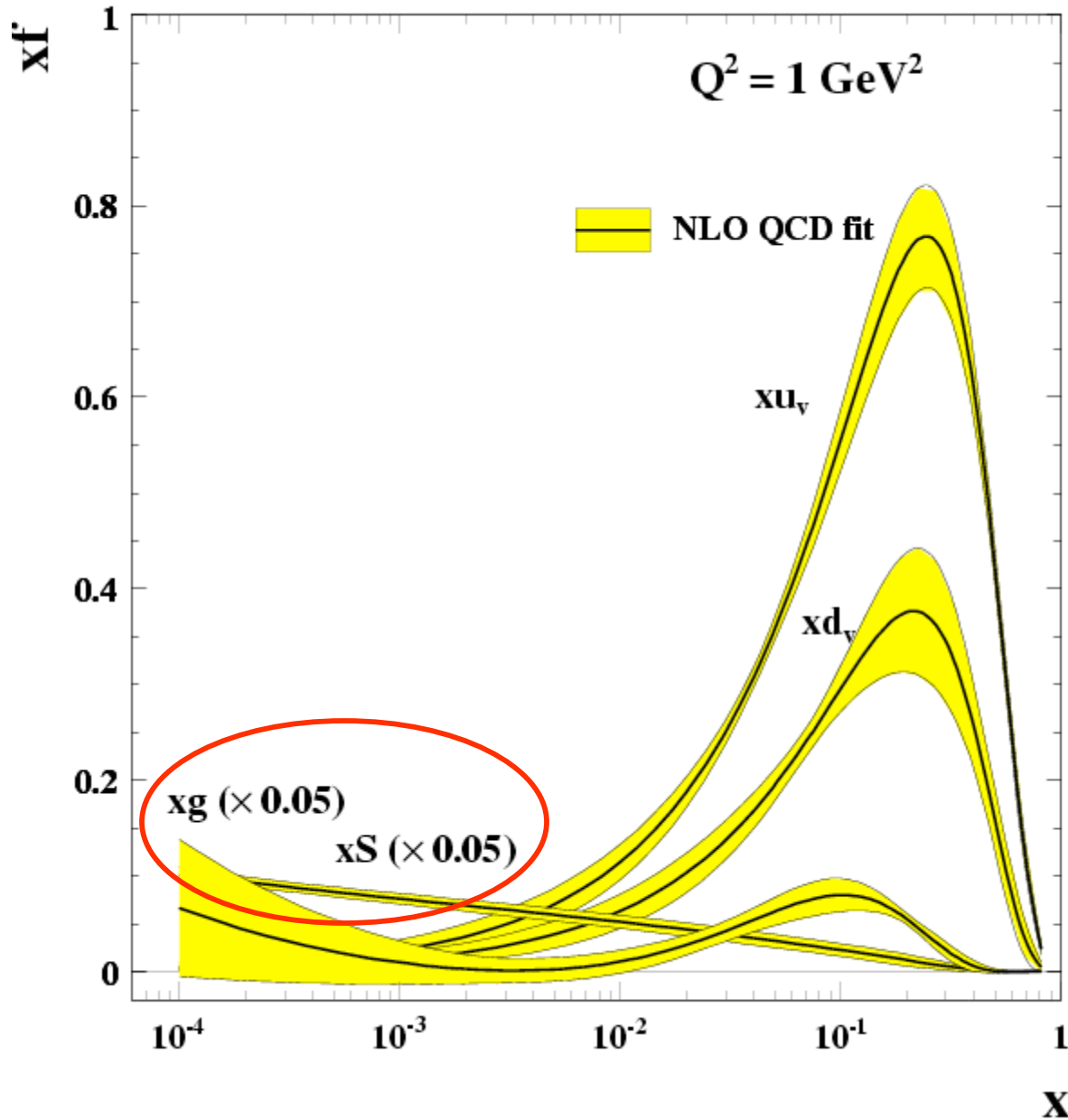


x

# Evolving PDFs up to $M_{W,Z}$ scale



Finally...



Valence quarks  
maximum around  
 $x=0.2$ ;  $q(x) \rightarrow 0$  for  
 $x \rightarrow 1$  and  $x \rightarrow 0$

Sea quarks  
and gluons -  
contribute at  
low values of  
 $x$



# QCD predictions: the running of $\alpha_s$

- pQCD valid if  $\alpha_s \ll 1$ :

$$\Rightarrow Q^2 > 1.0 \text{ (GeV/c)}^2$$

- pQCD calculation:

$$\alpha_s(Q^2) = \frac{12\pi}{(33 - 2n_f) \cdot \ln(Q^2 / \Lambda^2)}$$

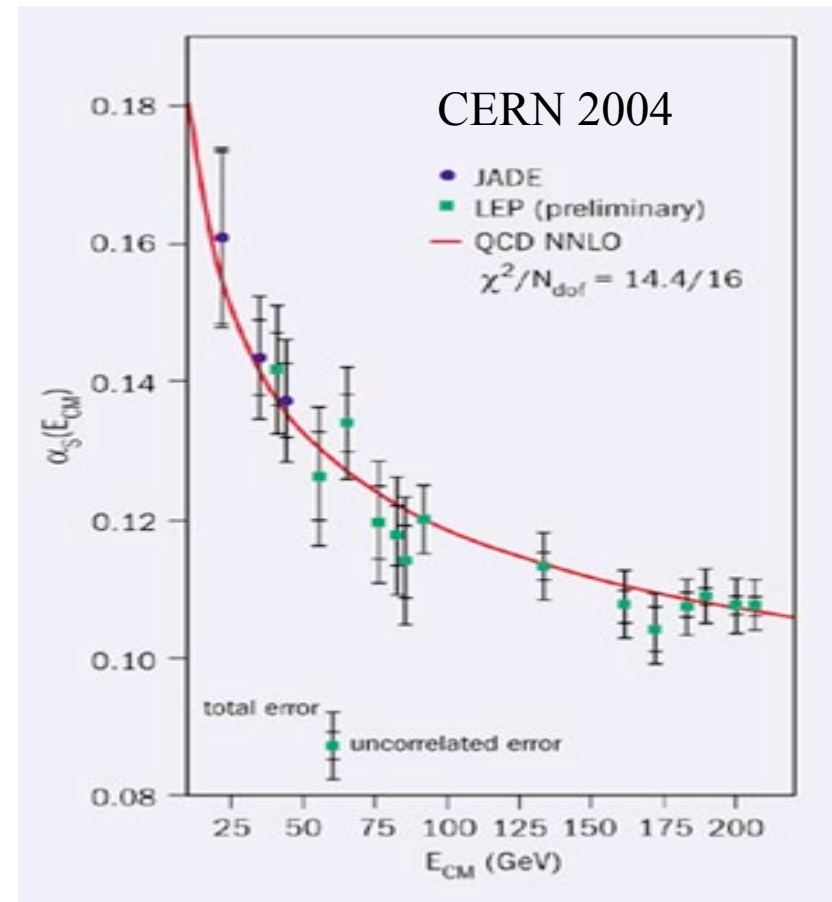
– with  $\Lambda_{\text{exp}} = 250 \text{ MeV/c}$ :

$$Q^2 \rightarrow \infty \Rightarrow \alpha_s \rightarrow 0$$

$\Rightarrow$  asymptotic freedom

$$Q^2 \rightarrow 0 \Rightarrow \alpha_s \rightarrow \infty$$

$\Rightarrow$  confinement



Running coupling constant is quantitative test of QCD.

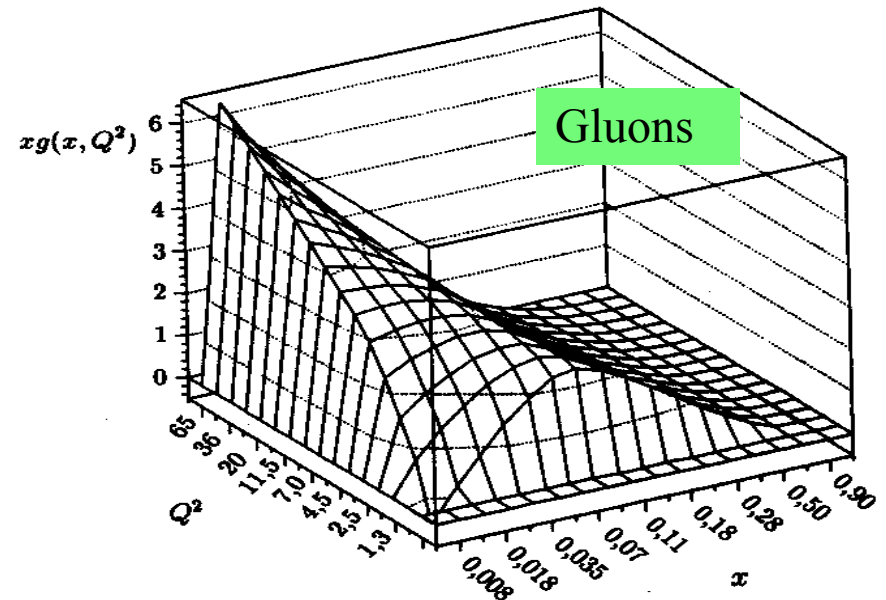
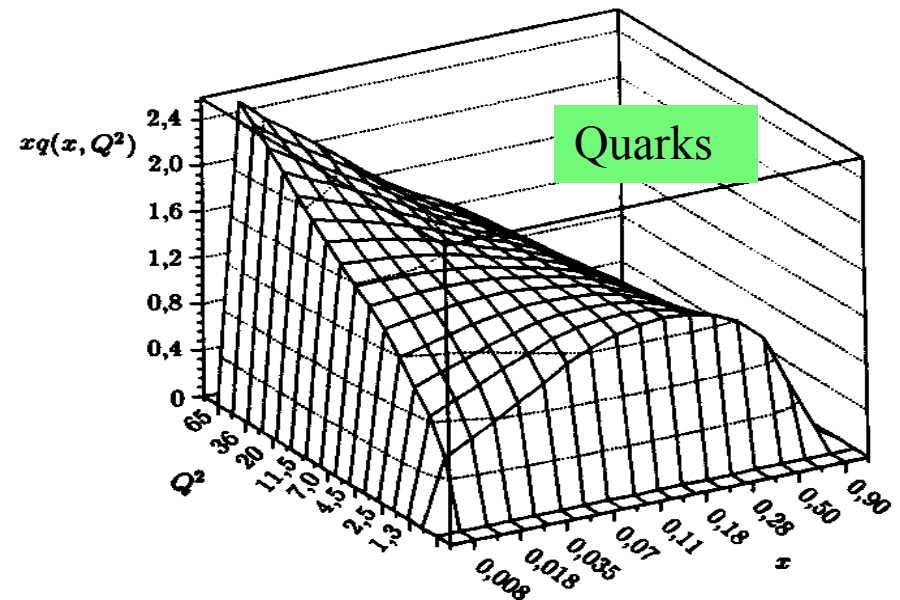
# QCD fits of $F_2(x, Q^2)$ data

- Free parameters:
  - coupling constant:

$$\alpha_s = \frac{12\pi}{(33 - n_f) \ln(Q^2 / \Lambda^2)} \approx 0.16$$

- quark distribution  $q(x, Q^2)$
  - gluon distribution  $g(x, Q^2)$
- Successful fit:

*Corner stone of QCD*



What's still to do?

# LOTS still to do!

- Large pdf uncertainties still at **large x**, low x
- **pdfs in nuclei**
- $F_L$  structure function - unique sensitivity to the glue

EIC

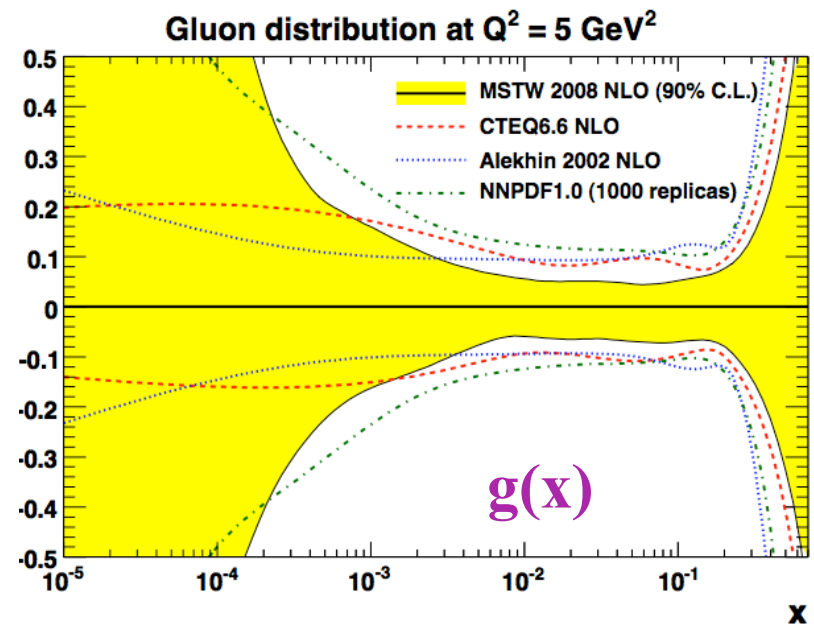
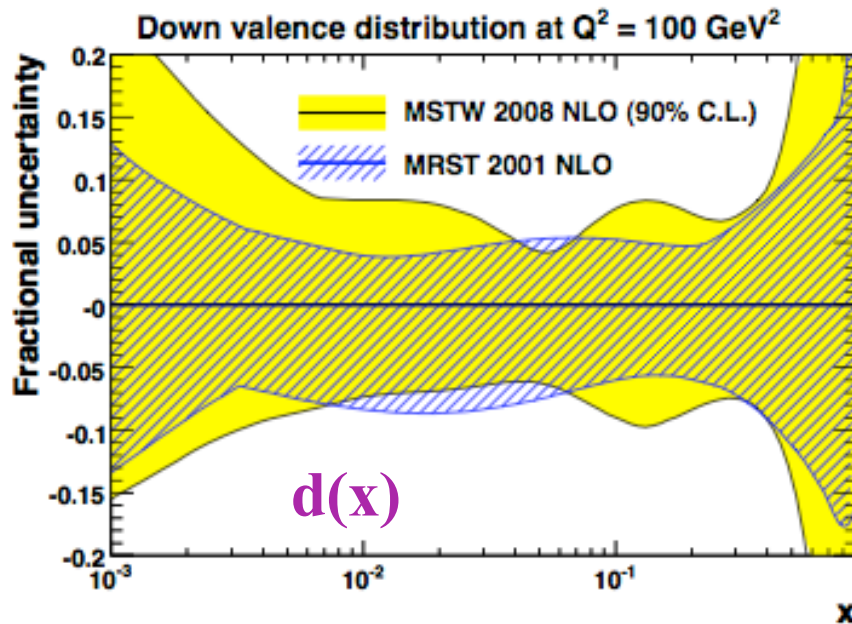
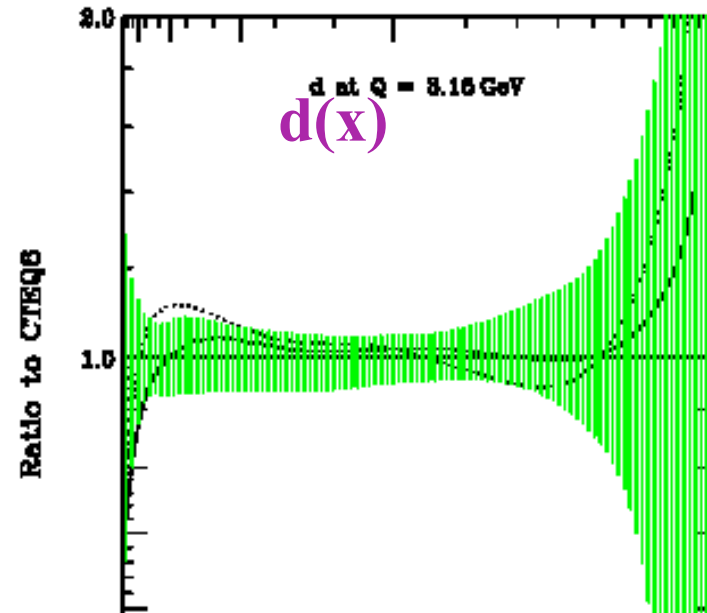
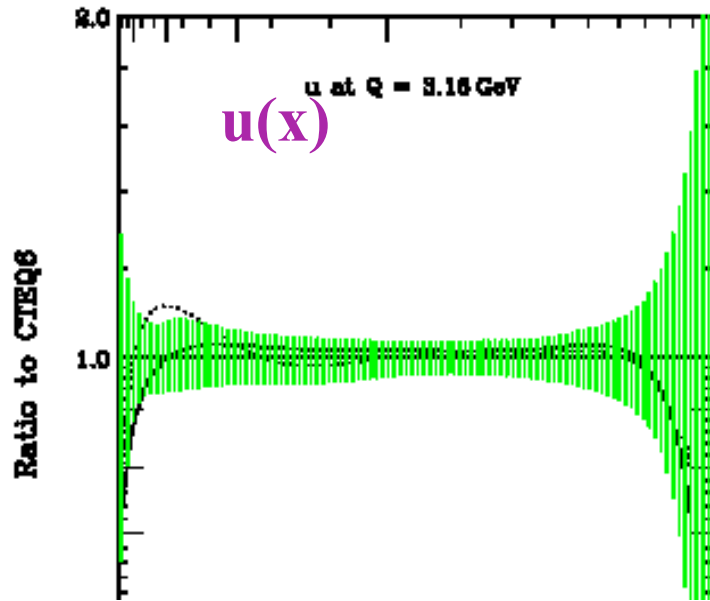


$$\int_0^1 dx F_L(x, Q^2) = \frac{\alpha_s(Q^2)}{4\pi} \left( \frac{4}{9} \int_0^1 dx F_2(x, Q^2) + \frac{2 \sum e_q^2}{12} \int_0^1 dx x \underline{G(x, Q^2)} \right)$$

( $F_2 = 2xF_1$  only true at leading order)

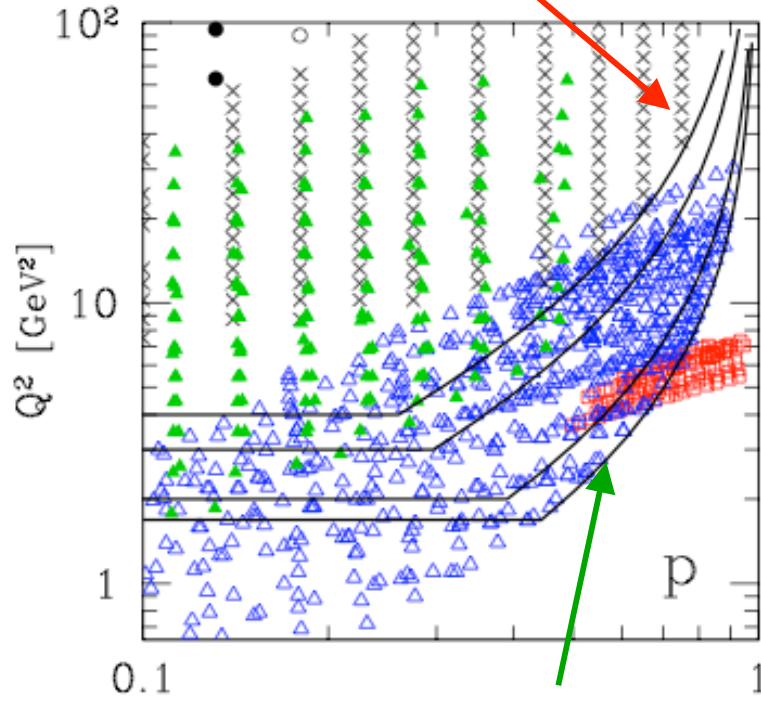
- Spin-dependent structure functions and transversity
- **Generalized parton distributions**
- **Quark-hadron duality, transition to pQCD**
- Neutrino measurements - nuclear effects different?  $F_3$  structure function (Dave Schmitz talks next week)
- Parity violation, charged current,....
- NLO, NNLO, and beyond
- Semi-inclusive (flavor tagging)
- BFKL evolution, Renormalization

# Large $x$ ( $x > 0.1$ ) $\rightarrow$ Large PDF Uncertainties

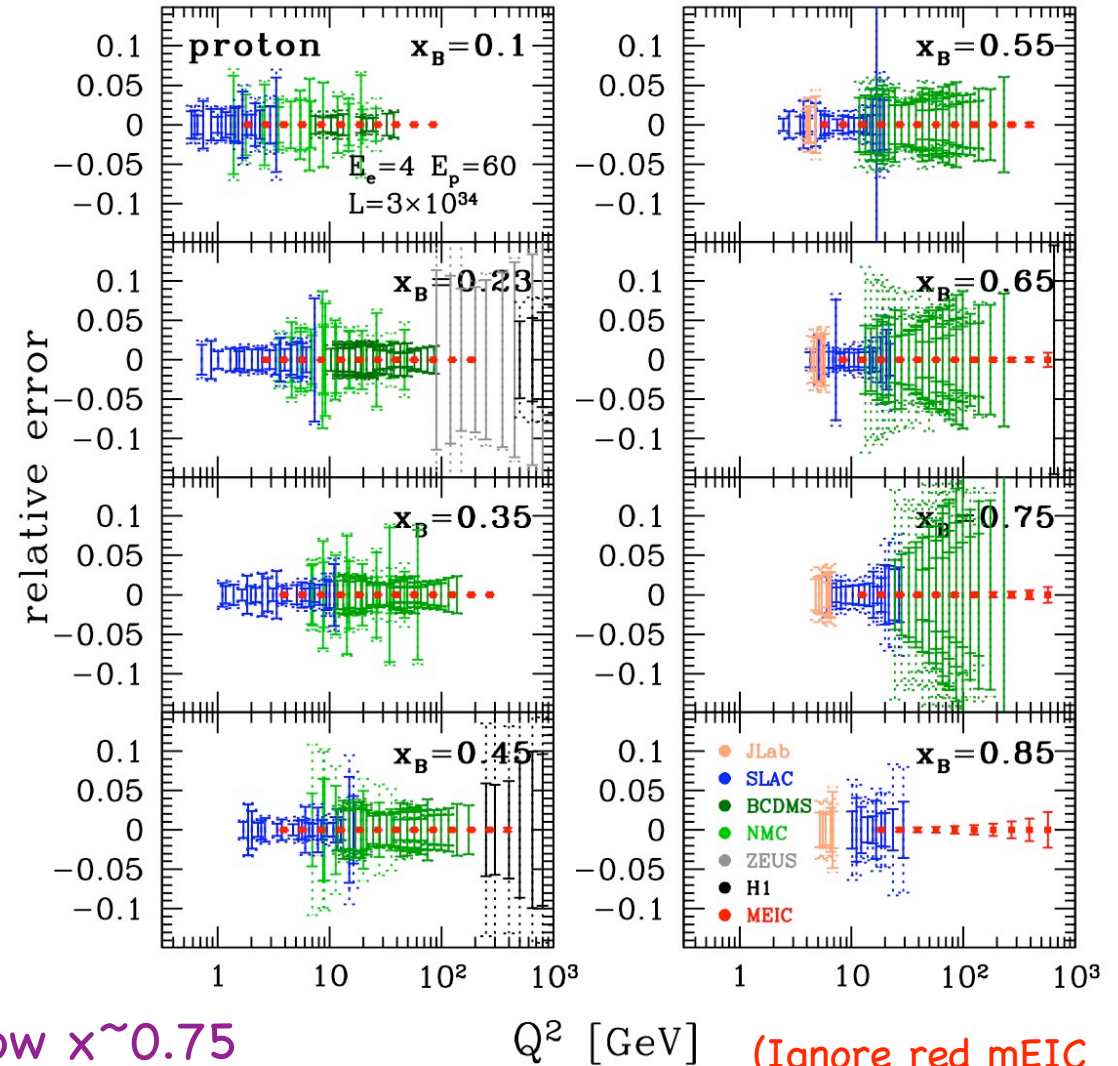


# Typical $W$ , $Q$ cuts are **VERY** restrictive...

Current  $Q^2 > 4 \text{ GeV}^2$ ,  $W^2 > 12.25 \text{ GeV}^2$ , cuts



Recent CTEQ-Jlab effort to reduce cuts



Essentially leave no data below  $x \sim 0.75$

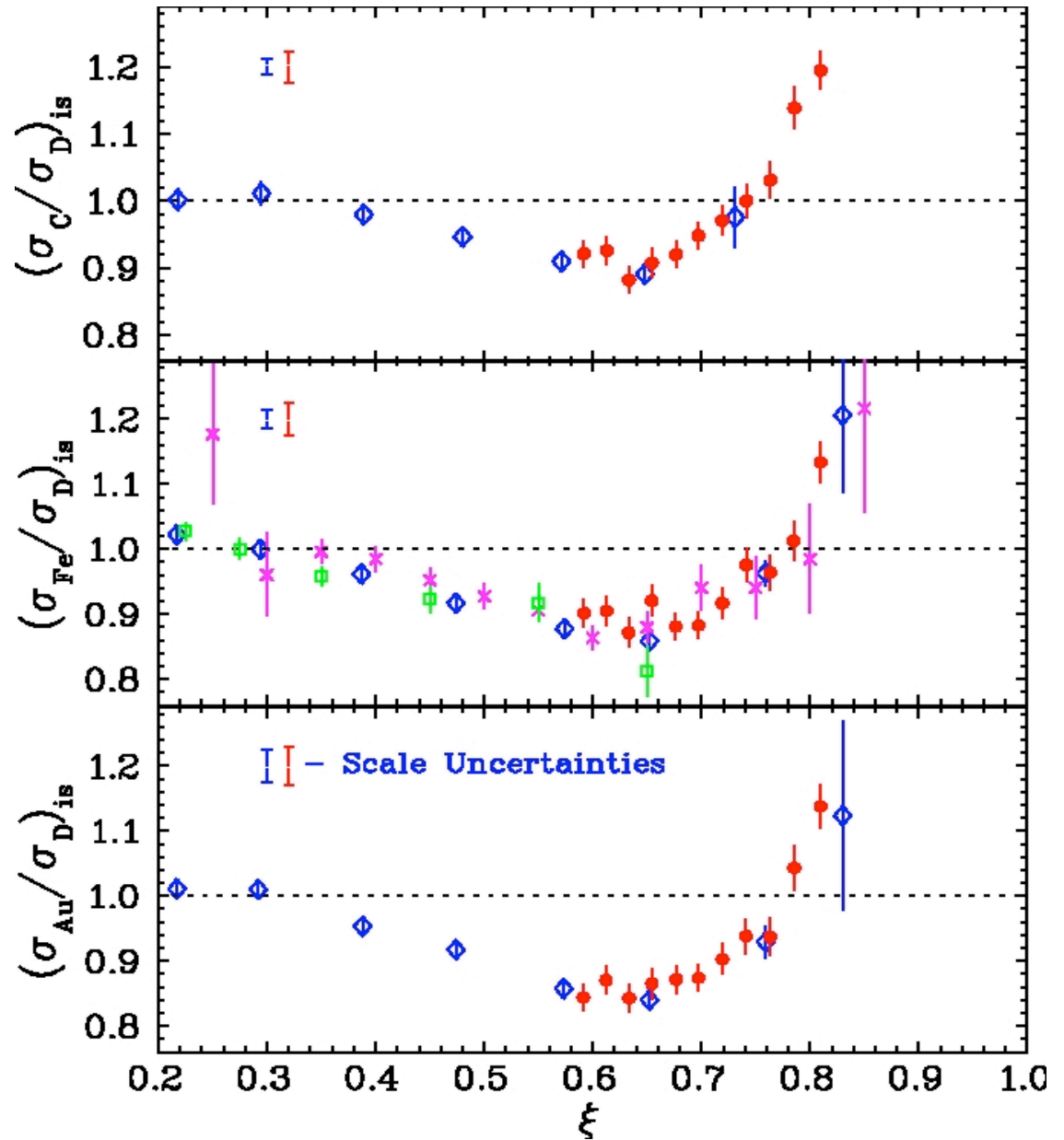
What large  $x$  data there is has large uncertainty

(Ignore red mEIC proposed data points.)

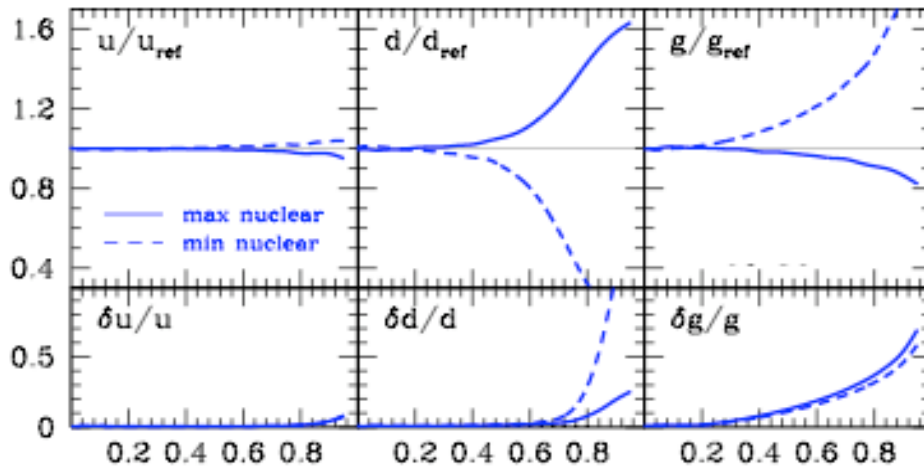
# Nuclear medium modifications, pdfs



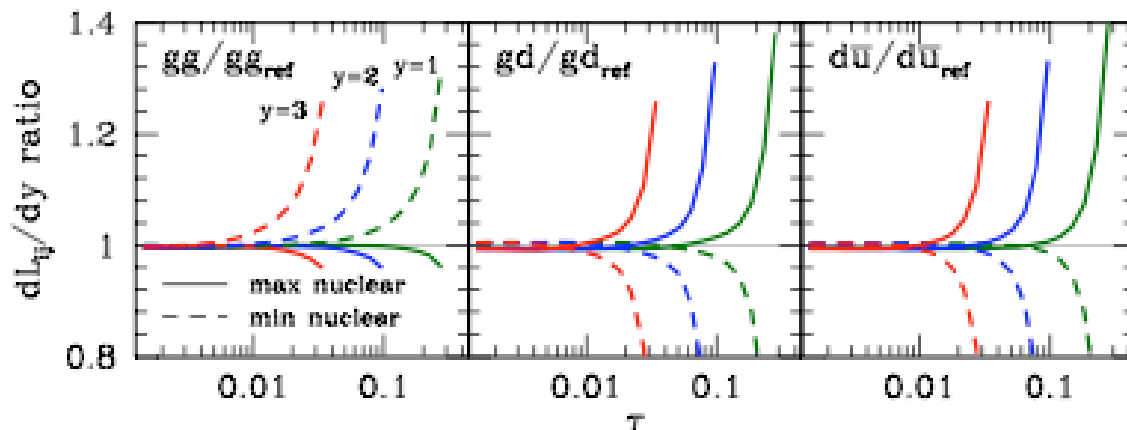
The moon at nuclear densities  
( $A_{\text{moon}} \approx 5 \times 10^{49}$ )



# The deuteron is a nucleus, and corrections at large x matter...



The extremes of variation of the u,d, gluon PDFs, relative to reference PDFs using different deuterium nuclear corrections

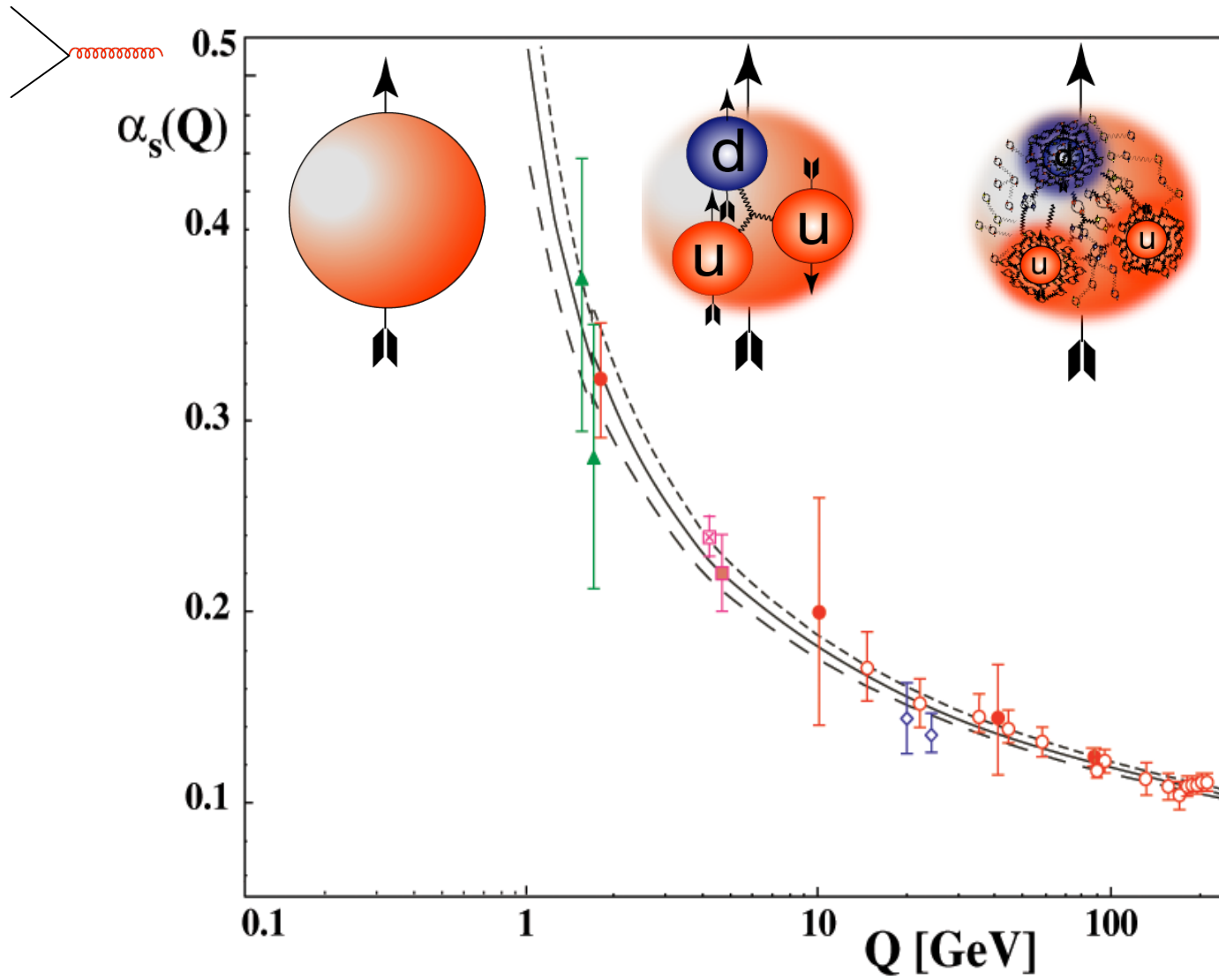


Differential parton luminosities for fixed rapidity  $y = 1, 2, 3$ , as a function of  $\tau = Q^2/S$ , variations due to the choice of deuterium nucleon corrections.

The  $gg$ ,  $gd$ ,  $d\bar{u}$  luminosities control the “standard candle” cross section for Higgs, jet  $W^-$  production, respectively.



# QCD and the Parton-Hadron Transition



**Hadrons**  
**Nucleons**  
**Quarks and Gluons**

# Quark-Hadron Duality

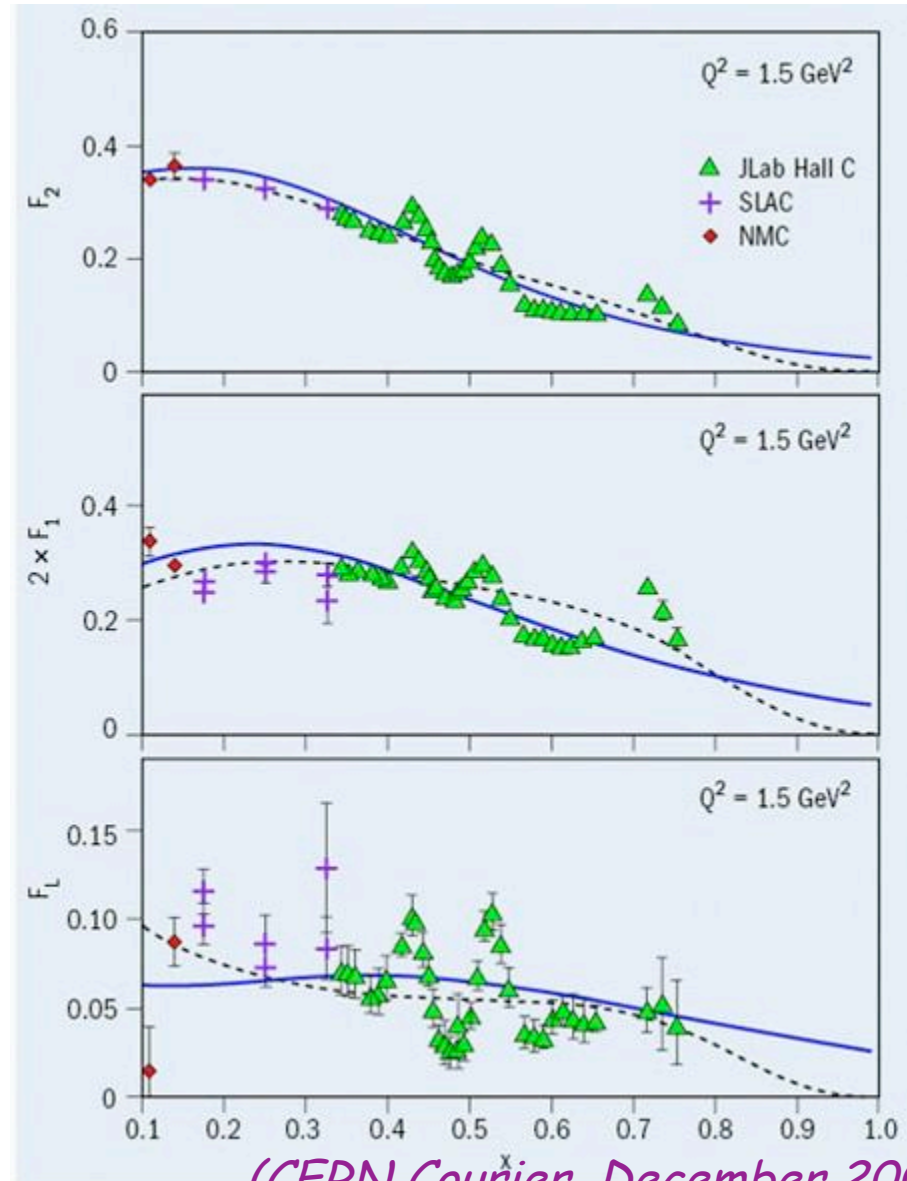
- At high energies: interactions between quarks and gluons become weak  
(“asymptotic freedom”)
  - efficient description of phenomena afforded in terms of quarks
- At low energies: effects of confinement make strongly-coupled QCD highly non-perturbative
  - collective degrees of freedom (mesons and baryons) more efficient
- Duality between quark and hadron descriptions
  - reflects relationship between *confinement* and *asymptotic freedom*
  - intimately related to nature and transition from *non-perturbative* to *perturbative* QCD

Duality defines the transition from soft to hard QCD.

# Duality observed (but not understood) in inelastic (DIS) structure functions

*First observed in  $F_2$  ~1970 by Bloom and Gilman at SLAC*

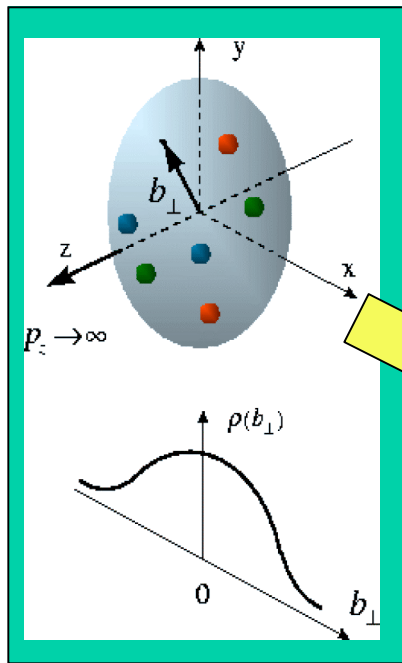
- Bjorken Limit:  $Q^2, \nu \rightarrow \infty$
- Empirically, DIS region is where logarithmic scaling is observed:  $Q^2 > 5 \text{ GeV}^2$ ,  $W^2 > 4 \text{ GeV}^2$
- Duality: Averaged over  $W$ , logarithmic scaling observed to work also for  $Q^2 > 0.5 \text{ GeV}^2$ ,  $W^2 < 4 \text{ GeV}^2$ , resonance regime



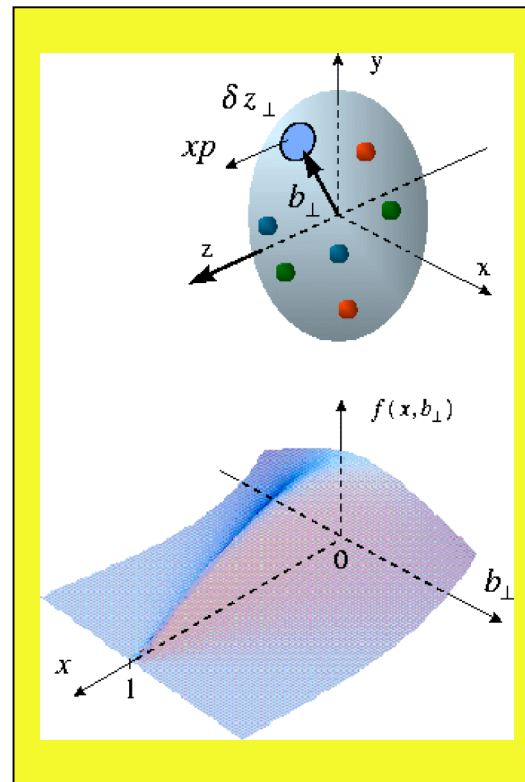
*(CERN Courier, December 2004)*

# Beyond form factors and quark distributions - Generalized Parton Distributions (GPDs)

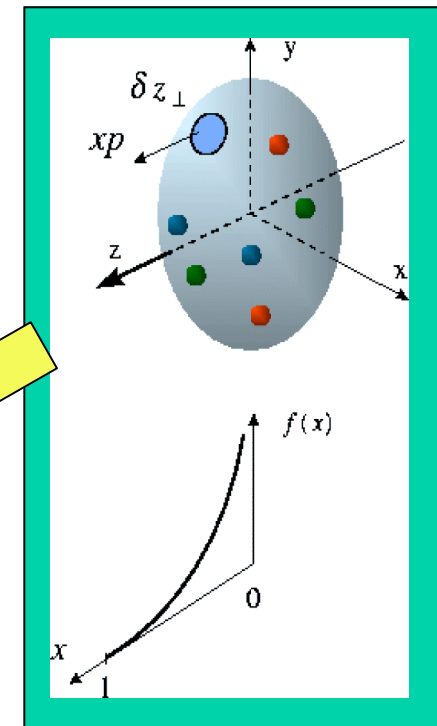
X. Ji, D. Mueller, A. Radyushkin (1994-1997)



Proton form factors, **transverse** charge & current densities



**Correlated** quark momentum and helicity distributions in **transverse space** - **GPDs**



Structure functions, quark **longitudinal** momentum & helicity distributions

# Again, LOTS still to do!

- Large pdf uncertainties still at **large x**, low x
- **pdfs in nuclei**
- $F_L$  structure function - unique sensitivity to the glue

EIC

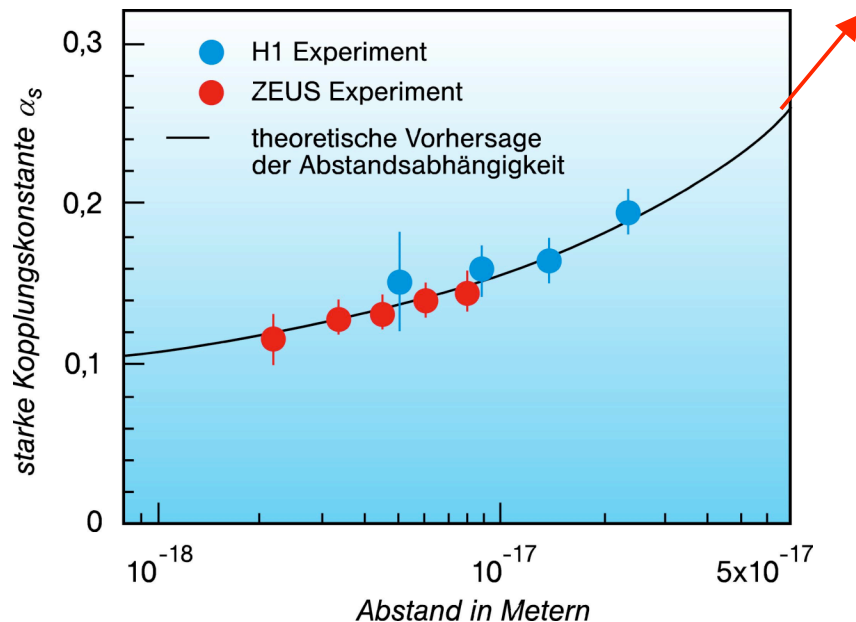
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( $F_2 = 2xF_1$  only true at leading order)

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# More challenges....

- Extrapolate  $\alpha_s$  to the size of the proton,  $10^{-15}$  m:



- If  $\alpha_s > 1$  perturbative expansions fail...

→ *Non-perturbative QCD:*

- Proton structure & spin
- Confinement
- Nucleon-Nucleon forces
- Higher twist effects
- Target mass corrections

$$l \rightarrow r_{proton} \Rightarrow \alpha_s > 1$$