

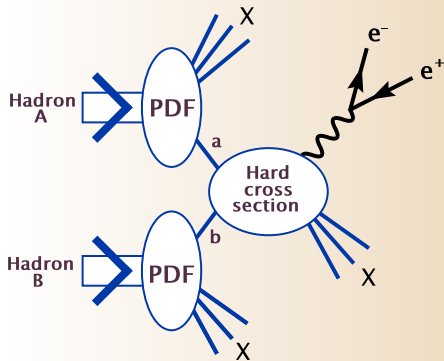
# Vector boson production in hadron-hadron scattering *(Drell-Yan-like processes)*

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July 12, 2011

**DY-like processes:**  $A(p_A)B(p_B) \rightarrow (V(q) \rightarrow v_1v_2\dots)X$



Drell-Yan production of lepton pairs

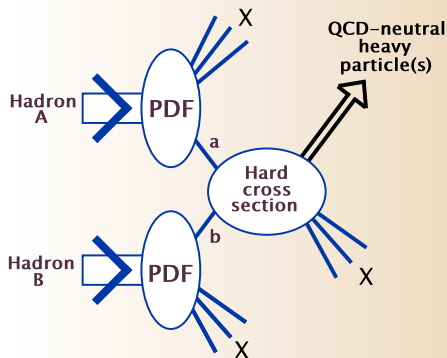
## DY-like processes: $A(p_A)B(p_B) \rightarrow (V(q) \rightarrow v_1 v_2 \dots) X$

### Notations

■  $A, B$  – initial-state hadrons  
( $p, \bar{p}, n$ , nuclei,  $\pi$ , ...)

■  $V$  – a final-state QCD-neutral system  
(a vector boson or boson pair with mass  $Q \gg \Lambda_{QCD}$ )

■  $v_1, v_2$  – observed particles from decay of  $V$  (e.g., leptons)



# DY-like processes: $A(p_A)B(p_B) \rightarrow (V(q) \rightarrow v_1 v_2 \dots)X$

## DY-like processes are ubiquitous

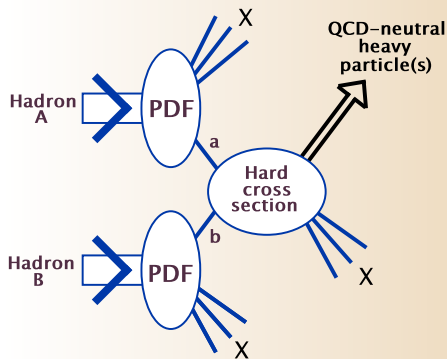
■  $AB \rightarrow (\gamma^*, Z \rightarrow \ell^+ \ell^-)X$   
(with  $\ell = e, \mu$ )

■  $AB \rightarrow (W \rightarrow \ell \nu_\ell)X$

■  $AB \rightarrow VVX$   
(with  $V = \gamma, W, Z, \dots$ )

■  $AB \rightarrow \text{Higgs} + X$  (F. Petriello)

■  $AB \rightarrow V_{BSM}X$   
(with  $V_{BSM} = Z',$   
Randall-Sundrum graviton, etc.)



## DY-like processes: $A(p_A)B(p_B) \rightarrow (V(q) \rightarrow v_1v_2\dots)X$

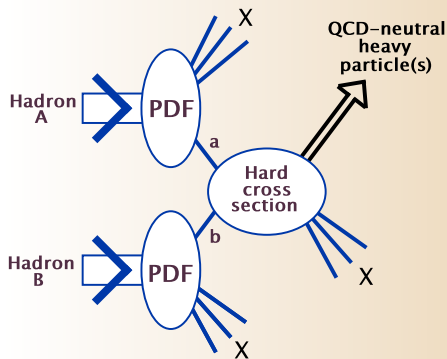
### DY-like processes are "simple"

- $V$  does not interact with final-state hadrons, which are summed over in cross sections

⇒ no dependence on final-state nonperturbative functions

- QCD factorization is **proved** to all orders in  $\alpha_s$  for a number of DY observables

► (In many other processes, factorization is only a **plausible conjecture**)



## DY-like processes: $A(p_A)B(p_B) \rightarrow (V(q) \rightarrow v_1v_2\dots)X$

### Example: factorization for the total cross section

$$\frac{d\sigma}{dQ^2} = \sum_{a,b} \int_{\tau}^1 \frac{d\xi}{\xi} f_{a/A}(\xi, Q) f_{b/B}(\frac{\tau}{\xi}, Q) \frac{d\hat{\sigma}_{ab}}{dQ^2},$$

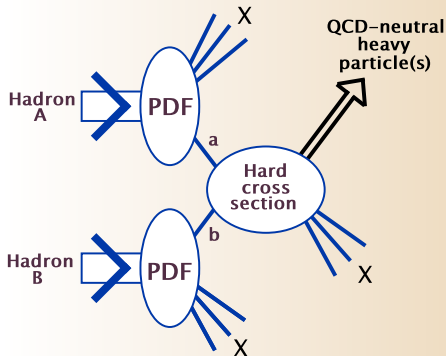
where

$Q$  is the invariant mass of  $V$ ;

$$\tau \equiv Q^2/s;$$

$\hat{\sigma}_{ab}$  is the hard-scattering cross section (calculated as a series in the QCD coupling  $\alpha_s$ );

$f_{a/A}(\xi, \mu)$  and  $f_{b/B}(\tau/\xi, \mu)$  are parton distribution functions

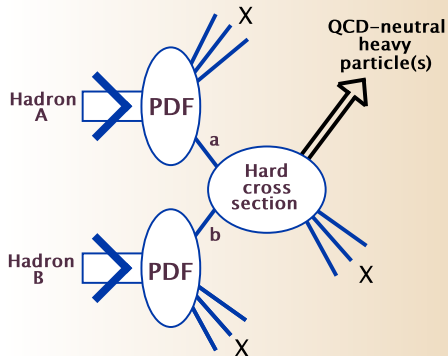


## DY-like processes: $A(p_A)B(p_B) \rightarrow (V(q) \rightarrow v_1v_2\dots)X$

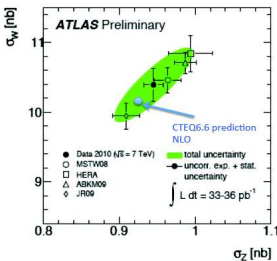
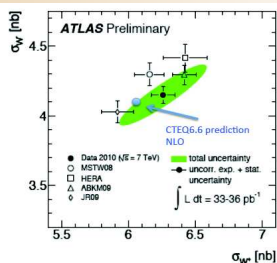
### DY-like processes produced many important discoveries

- early confirmation of the parton model
- discovery of heavy quarks (which ones?)
- discovery of massive carriers of weak force ( $W$  and  $Z$ )

Modern DY experiments provide most precise QCD tests at hadron colliders



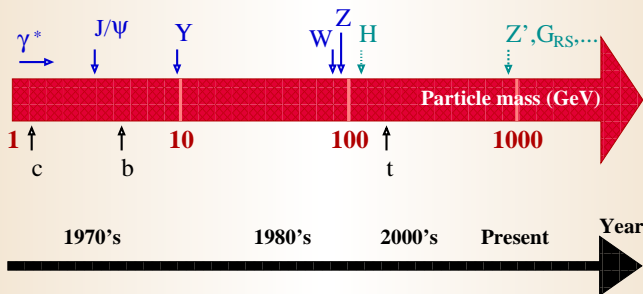
# W and Z cross sections at the LHC



Measurement of  $\sigma_W$  and  $\sigma_Z$  confirms the validity of perturbative QCD at  $\sqrt{s} = 7$  TeV



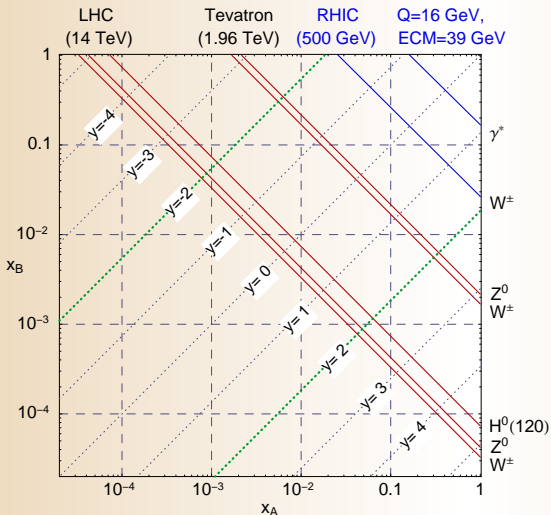
# Final states in DY-like processes



Explore the DY-like processes as a function of  $Q \equiv M_{\ell\ell'}$ , the invariant mass of the heavy EW state

$$\frac{d\sigma}{dQ^2} = \sum_{a,b} \int_{\tau}^1 \frac{d\xi}{\xi} f_{a/A}(\xi, Q) f_{b/B}\left(\frac{\tau}{\xi}, Q\right) \frac{d\hat{\sigma}_{ab}}{dQ^2}$$

# Typical parton momentum fractions



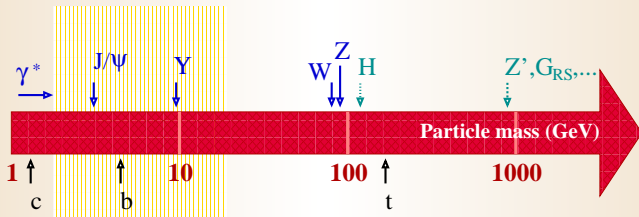
$$x_{A,B} \equiv \frac{Q}{\sqrt{s}} e^{\pm y}$$

Born level:  $p_a^\mu = x_A p_A^\mu$ ,  
 $p_b^\mu = x_B p_B^\mu$

Typical rapidities in the experiment:  $|y| \lesssim 2$

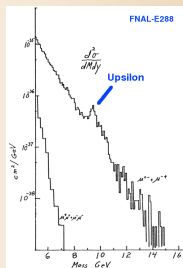
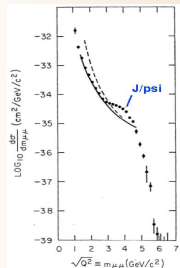
- experiments at higher energies are sensitive to PDF's at smaller  $x$

# Final states in DY-like processes

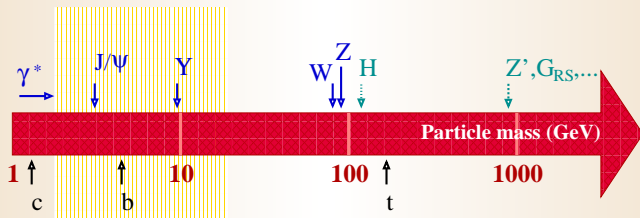


$pN \xrightarrow{\gamma^*} l^+ l^- X$  at  $Q < 20$  GeV

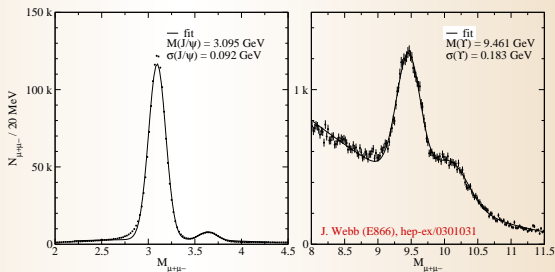
- Continuous  $\gamma^*$  cross section
- Multiple quarkonium resonances (studied by non-relativistic QCD, **not** in the PDF fit)
- ▲  $J/\psi$  ( $c\bar{c}$ )– found in  $e^+e^-$  scattering (1974)
- ▲  $\Upsilon$  ( $b\bar{b}$ )– found in  $pN \rightarrow \mu^+ \mu^- X$  (FNAL-E288, 1977)



# Final states in DY-like processes



$J/\psi, \Upsilon$   
resonances  
shown with  
better  
resolution  
(FNAL-E866)

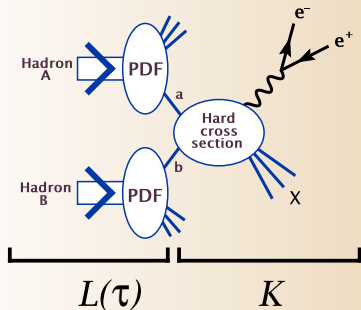


# Scaling of the continuum cross section

S. Drell, T. M. Yan, 1970

$$s \frac{d\sigma}{dQ^2} \approx \mathcal{L}_{ab}(\tau) \cdot \text{const}$$

■  $\mathcal{L}_{ab}(\tau)$  is the “parton luminosity”, originally derived from DIS functions; depends only on  $\tau$  if the  $\ln Q$  dependence is neglected



# Scaling of the continuum cross section

S. Drell, T. M. Yan, 1970

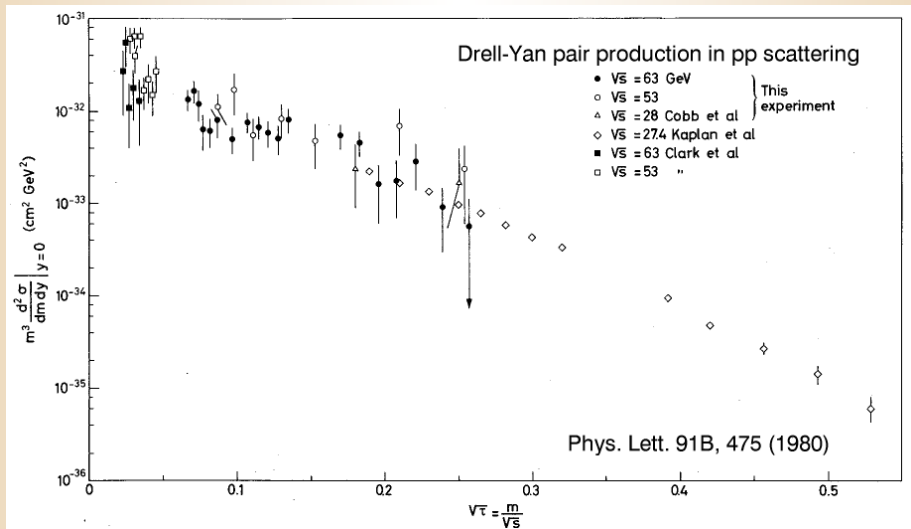
$$s \frac{d\sigma}{dQ^2} \approx \mathcal{L}_{ab}(\tau) \cdot \text{const}$$

- Compare to the Born cross section:

$$\left( \frac{d\sigma}{dQ^2} \right)_{LO} = \frac{4\pi\alpha_{EM}^2}{3N_c Q^2 s} \times \underbrace{\sum_{i=u,d,s,\dots} e_i^2 \int_{\tau}^1 \frac{d\xi}{\xi} \left[ f_{q_i/A}(\xi, Q) f_{\bar{q}_i/B}\left(\frac{\tau}{\xi}, Q\right) + f_{\bar{q}_i/A}(\xi, Q) f_{q_i/B}\left(\frac{\tau}{\xi}, Q\right) \right]}_{\mathcal{L}(\tau)},$$

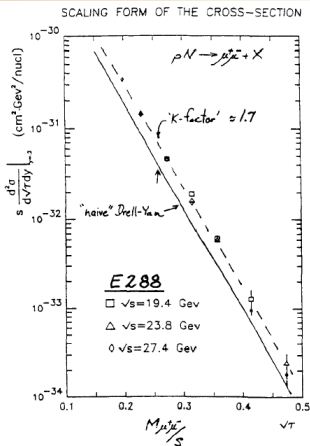
with  $N_c = 3$ ,  $\alpha_{EM} \equiv e^2/(4\pi)$ ,  $ee_i$  is the fractional quark charge

# Scaling of the low-Q data



# NLO corrections and the K-factor

Tau-scaling works because radiative corrections to  $q\bar{q} \rightarrow VX$  are relatively constant at  $x \sim 0.1$



## A useful estimate

$$\frac{d\sigma}{dQ^2} \approx \left( \frac{d\sigma}{dQ^2} \right)_{LO}(\tau) \cdot K_{NLO}(Q),$$

where  $K_{NLO} = 1 + \kappa\alpha_s(Q)$  with  $\kappa = 3 \pm 1$

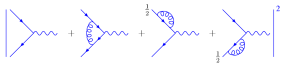
(also applies to  $W, Z, \dots$  production)

**Exercise: show that  $K \approx 1.65$  (1.35) at  $Q = 5$  (90) GeV**



# NLO cross section

- NLO:  $(\alpha_s^{(1)})$  virtual corrections  $(q\bar{q})_{virt}$



- NLO:  $(\alpha_s^{(1)})$  real emission diagrams  $(q\bar{q})_{real}$



- NLO:  $(\alpha_s^{(1)})$  real emission diagrams  $(qG)_{real}$



- NLO:  $(\alpha_s^{(1)})$  real emission diagrams  $(G\bar{q})_{real}$



## Virtual contributions

The dominant contribution to  $\sigma_{tot}$ , if  $x$  is moderate

$$\begin{aligned}\sigma_{tot}^{NLO} &\sim \left[ 1 + \frac{\alpha_s}{2\pi} C_F \left( 1 + \frac{4\pi^2}{3} \right) \right] \sigma_{tot}^{LO} \\ &\sim [1 + 3.005\alpha_s] \sigma_{tot}^{LO}\end{aligned}$$

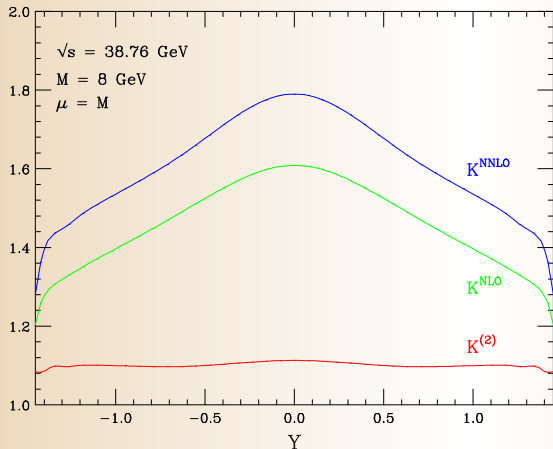
At  $x \rightarrow 0$  or  $1$ ,  $\ln(x)$  or  $\ln^p(1-x)/(1-x)_+$  terms are enhanced; the NLO factor is not constant!

## 2 $\rightarrow$ 3 contributions

Generate  $Q_T \neq 0$ , non-trivial  $\theta_*, \varphi_*$  dependence

# NNLO cross sections for low- $Q$ DY process

Anastasiou, Dixon, Melnikov, Petriello, 2003-05



$$K^{\text{NLO}} \approx 1.6 \text{ at } y = 0$$

$$K^{\text{NLO}} \approx 1.4 \text{ at } y = 1$$

Compare with  $1 + 3\alpha_s(8) \approx 1.56$

$K^{(2)} = \sigma_{\text{NNLO}}/\sigma_{\text{NLO}}$  – uniform enhancement over NLO by  $\sim 8\%$

# Classical measurements in low- $Q$ DY process

1. Sea quark PDFs  $\bar{q}_i(x, Q)$  from rapidity ( $y$ ) distributions
2. Spins of  $\gamma^*$  and quarks from angular distributions of decay leptons

# 1. Constraints on quark sea from $pN \rightarrow \ell^+ \ell^- X$

( $N = p, d, Fe, Cu, \dots$ )

$$\frac{d\sigma_{pp}}{dQ^2 dy} \sim \left(\frac{2}{3}\right)^2 [u_A \bar{u}_B + \bar{u}_A u_B] + \left(-\frac{1}{3}\right)^2 [d_A \bar{d}_B + \bar{d}_A d_B] + \text{smaller terms}$$

$\Rightarrow$  sensitivity to  $\bar{q}(x, Q)$

Assuming charge symmetry between protons and neutrons

( $u_p = d_n, u_n = d_p$ ):

$$\frac{d\sigma_{pn}}{dQ^2 dy} \sim \left(\frac{2}{3}\right)^2 [u_A \bar{d}_B + \bar{u}_A d_B] + \left(-\frac{1}{3}\right)^2 [d_A \bar{u}_B + \bar{d}_A u_B] + \text{smaller terms}$$

If deuterium binding corrections are neglected:

$$q_d(x) \approx q_p(x) + q_n(x)$$

At  $x_A \gg x_B$  (large  $y$ ):  $\bar{q}(x_A) \sim 0$  and  $4u(x_A) \gg d(x_A)$

$$\frac{\sigma_{pd}}{2\sigma_{pp}} \approx \frac{1}{2} \frac{(1 + \frac{d_A}{4u_A})[1+r]}{(1 + \frac{d_A}{4u_A}r)} \approx \frac{1}{2}(1+r), \text{ where } r \equiv \bar{d}(x_B)/\bar{u}(x_B)$$

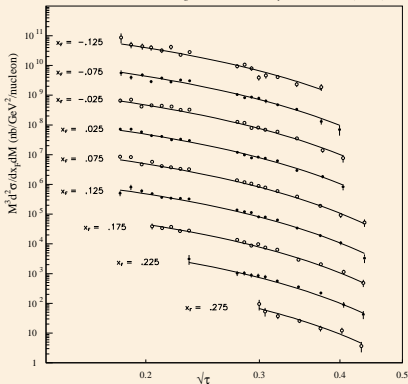
$\therefore \sigma_{pd}/(2\sigma_{pp})$  constrains  $\bar{d}(x, Q)/\bar{u}(x, Q)$  at moderate  $x$

# Theory vs. experiment

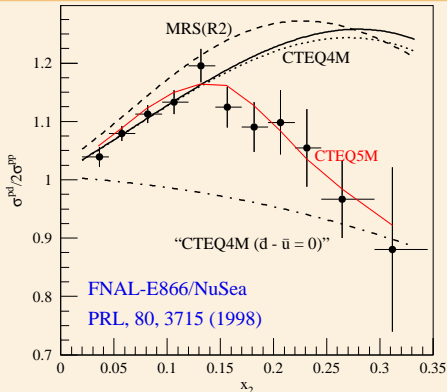
## Cross section at $Q = 4 - 17 \text{ GeV}$

E605 (p Cu  $\rightarrow \mu^+ \mu^- X$ )  $P_{\text{LAB}} = 800 \text{ GeV}$

Martin, Roberts, Stirling, Thorne, *Eur. Phys. J., C4, 463 (1998)*



## $\sigma_{pd}/(2\sigma_{pp})$ at large $x_F = x_A - x_B$



Theory curves reflect different assumptions about  $\bar{d}/\bar{u}$

PDF fits (e.g., CTEQ5M) quantitatively account for the violation of  $SU(2)$  symmetry in the quark sea

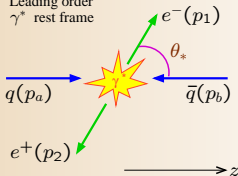
## 2. Lepton distributions in the rest frame of $\gamma^*$

The Born cross section for  $q_j \bar{q}_{\bar{k}} \rightarrow V \rightarrow \ell \bar{\ell}'$  is derived tomorrow:

$$\frac{d\sigma}{dQ^2 dy d\Omega} \propto \sum_{j, \bar{k}=u, \bar{u}, d, \bar{d}, \dots} \left\{ (f_R^2 + f_L^2)(g_{L,j\bar{k}}^2 + g_{R,j\bar{k}}^2)(1 + \cos^2 \theta_*) [q_j(x_A) \bar{q}_{\bar{k}}(x_B) + \bar{q}_{\bar{k}}(x_A) q_j(x_B)] \right. \\ \left. + (f_R^2 - f_L^2)(g_{L,j\bar{k}}^2 - g_{R,j\bar{k}}^2)(2 \cos \theta_*) [q_j(x_A) \bar{q}_{\bar{k}}(x_B) - \bar{q}_{\bar{k}}(x_A) q_j(x_B)] \right\}$$

- $f_L, f_R$  are left-handed and right-handed  $V \ell \bar{\ell}'$  couplings
- $g_{L,j\bar{k}}, g_{R,j\bar{k}}$  are left-handed and right-handed  $V q_j \bar{q}_{\bar{k}}$  couplings

Leading order  
 $\gamma^*$  rest frame



The  $E, p_x, p_y, p_z$  components are

$$p_a = \frac{Q}{2} (1, 0, 0, 1); \quad p_b = \frac{Q}{2} (1, 0, 0, -1);$$

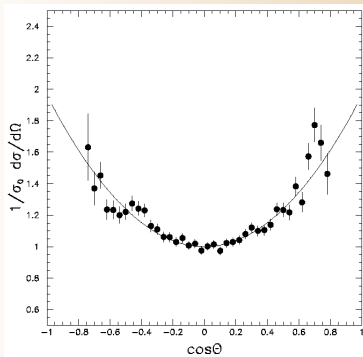
$$p_1 = \frac{Q}{2} (1, 0, 0, \cos \theta_*); \quad p_2 = \frac{Q}{2} (1, 0, 0, -\cos \theta_*);$$

# The Born cross section

$$\frac{d\sigma}{dQ^2 dy d\Omega} \propto \sum_{j, \bar{k}=u, \bar{u}, d, \bar{d}, \dots} \left\{ (f_R^2 + f_L^2)(g_{L, j\bar{k}}^2 + g_{R, j\bar{k}}^2)(1 + \cos^2 \theta_*) [q_j(x_A) \bar{q}_{\bar{k}}(x_B) + \bar{q}_{\bar{k}}(x_A) q_j(x_B)] \right. \\ \left. + (f_R^2 - f_L^2)(g_{L, j\bar{k}}^2 - g_{R, j\bar{k}}^2)(2 \cos \theta_*) [q_j(x_A) \bar{q}_{\bar{k}}(x_B) - \bar{q}_{\bar{k}}(x_A) q_j(x_B)] \right\}$$

■ The  $2 \cos \theta_*$  term vanishes in the parity-conserving case ( $f_L = f_R$  or  $g_L = g_R$ )

■ The  $(1 + \cos^2 \theta_*)$  dependence in the experimental data confirms the vector (spin-1) nature of low- $Q$  Drell-Yan process



# The Born cross section

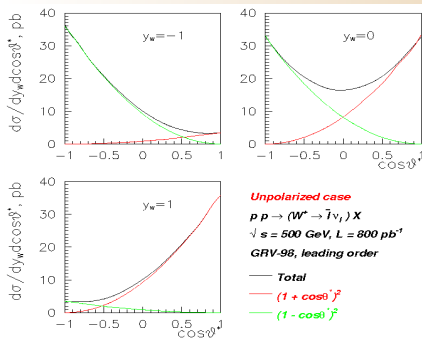
$$\frac{d\sigma}{dQ^2 dy d\Omega} \propto \sum_{j, \bar{k}=u, \bar{u}, d, \bar{d}, \dots} \left\{ (f_R^2 + f_L^2)(g_{L, j\bar{k}}^2 + g_{R, j\bar{k}}^2)(1 + \cos^2 \theta_*) [q_j(x_A) \bar{q}_{\bar{k}}(x_B) + \bar{q}_{\bar{k}}(x_A) q_j(x_B)] \right. \\ \left. + (f_R^2 - f_L^2)(g_{L, j\bar{k}}^2 - g_{R, j\bar{k}}^2)(2 \cos \theta_*) [q_j(x_A) \bar{q}_{\bar{k}}(x_B) - \bar{q}_{\bar{k}}(x_A) q_j(x_B)] \right\}$$

■  $W$  boson production:

$$f_R = g_R = 0$$

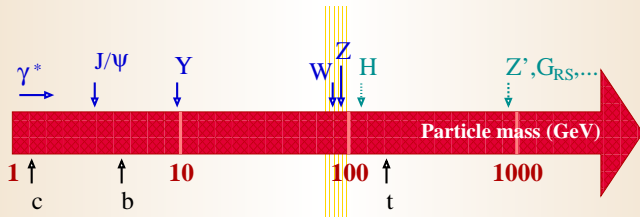
■  $W$  cross section depends on two functions  $(1 \pm \cos \theta_*)^2$  weighted by different parton luminosities

■ non-trivial correlation between  $y$  and  $\theta_*$  in the acceptance, etc.



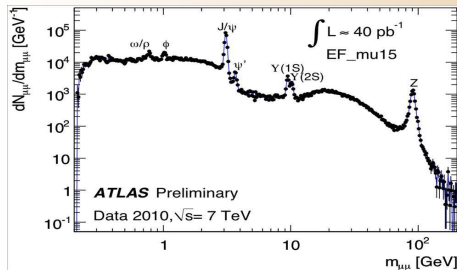


# Final states in DY-like processes



## W and Z boson production

- good convergence of the  $\alpha_s$  series
- small backgrounds
- separation of PDF flavors (via the CKM matrix)
- sensitivity to new physics



$Z$  pole and  $\gamma^*$  continuum in  $\ell^+ \ell^-$  production

# Leptonic vs. hadronic decay modes

The  $W$  and  $Z$  branching ratios  $\text{Br}_i \equiv \Gamma_i/\Gamma$  are

- $\text{Br}[W \rightarrow \ell\nu_\ell] \approx 3 \times 11\%$ ,  $\text{Br}[W \rightarrow \text{jets}] \approx 68\%$
- $\text{Br}[Z \rightarrow \ell^+\ell^-] = 3 \times 3.36\%$ ,  $\text{Br}[Z \rightarrow \nu_\ell\bar{\nu}_\ell] = 3 \times 6.67\%$ ,  
 $\text{Br}[Z \rightarrow \text{jets}] \approx 70\%$

At  $\sqrt{s}$  of a few TeV, hadronic  $W$ ,  $Z$  decays are hard to observe because of the large background from QCD jets

The most viable decay modes are

- $Z \rightarrow e^+e^-$ ,  $Z \rightarrow \mu^+\mu^-$
- $W \rightarrow e + \nu_e$ ,  $W \rightarrow \mu + \nu_\mu$ , with neutrinos identified by missing transverse energy  $E_T$

# W and Z observables

## ■ Total cross sections

$$\sigma_Z = \int \frac{d\sigma(pp \rightarrow (Z \rightarrow e^+e^-)X)}{d\vec{p}_{e^+}d\vec{p}_{e^-}} d\vec{p}_{e^+}d\vec{p}_{e^-}$$

## ■ Rapidity distributions and asymmetries

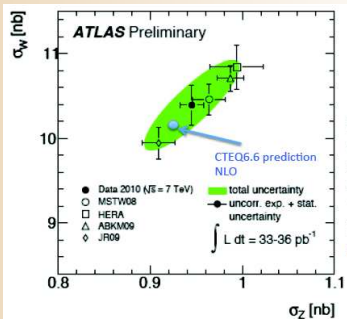
$$\frac{d\sigma_{W,Z}}{dQ^2 dy}, \text{ etc.}$$

## ■ W boson mass $M_W$

## ■ Transverse momentum and related distributions

$$\frac{d\sigma_{W,Z}}{dQ_T^2}, \frac{d\sigma_{W,Z}}{d(p_T^e)^2}, \frac{d\sigma_{W,Z}}{d(M_T^{l\nu})^2}$$

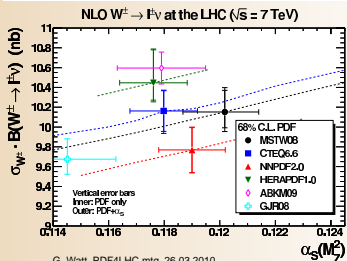
# Total $W$ and $Z$ cross sections



Provide tests of perturbative QCD and collider luminosity with accuracy 3-5%

Require understanding of

- $\mathcal{O}(\alpha_s^2)$ , or NNLO, QCD corrections
- $\mathcal{O}(\alpha)$ , or NLO, EW corrections
- PDF uncertainties
- Experimental acceptance
- QCD and EW showering (all-orders resummations)

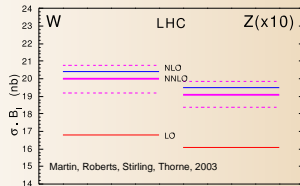


G. Watt, PDF4LHC mtg, 26.03.2010

# NNLO total section $\sigma_{tot}(AB \rightarrow W, Z)$

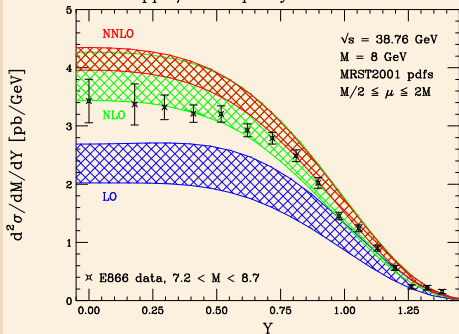
(Hamberg, van Neerven, Matsuura; Harlander, Kilgore)

- Scale dependence of order 1%
- NNLO  $K$ -factor is about 1.04 at the Tevatron and 0.98 at the LHC (MRST'03)

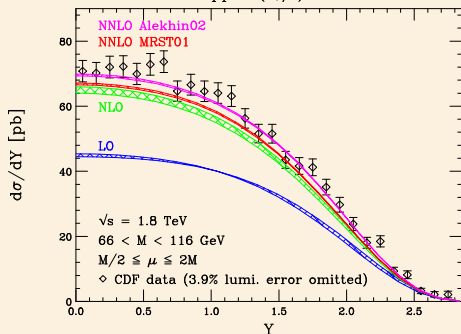


# NNLO differential cross sections (Anastasiou, Dixon, Melnikov, Petriello, 2003-05)

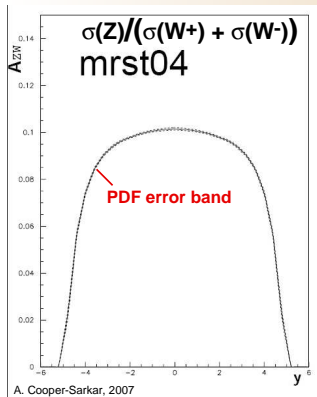
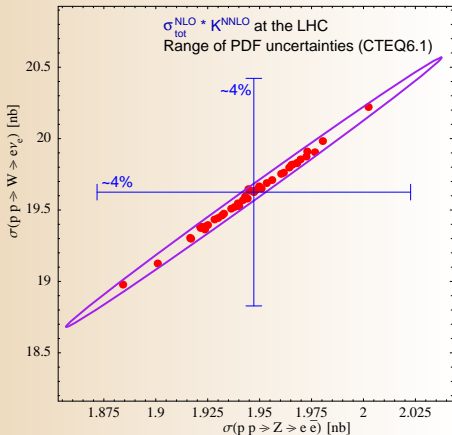
$pp \rightarrow \gamma^* + X$  Rapidity distribution



$p\bar{p} \rightarrow (Z, \gamma^*) + X$



# Ratios of $W$ and $Z$ cross sections



Radiative contributions, PDF dependence have similar structure in  $W$ ,  $Z$ , and alike cross sections; cancel well in Xsection ratios

# W and Z observables

## ■ Total cross sections

$$\sigma_Z = \int \frac{d\sigma(pp \rightarrow (Z \rightarrow e^+e^-)X)}{d\vec{p}_{e^+}d\vec{p}_{e^-}} d\vec{p}_{e^+}d\vec{p}_{e^-}$$

## ■ Rapidity distributions and asymmetries

$$\frac{d\sigma_{W,Z}}{dQ^2 dy}, \text{ etc.}$$

## ■ W boson mass $M_W$

## ■ Transverse momentum and related distributions

$$\frac{d\sigma_{W,Z}}{dQ_T^2}, \frac{d\sigma_{W,Z}}{d(p_T^e)^2}, \frac{d\sigma_{W,Z}}{d(M_T^{l\nu})^2}$$

# Charged lepton asymmetry at the Tevatron

$$A_{ch}(y_e) \equiv \frac{\frac{d\sigma^{W^+}}{dy_e} - \frac{d\sigma^{W^-}}{dy_e}}{\frac{d\sigma^{W^+}}{dy_e} + \frac{d\sigma^{W^-}}{dy_e}}$$

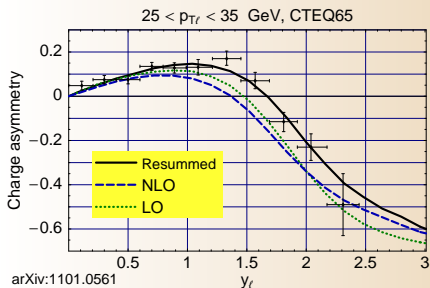
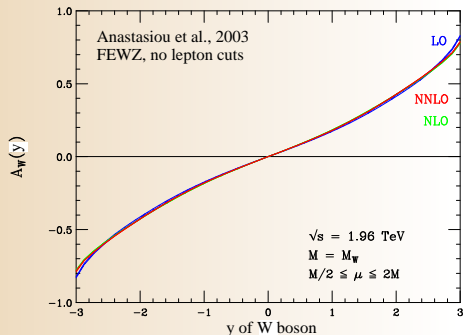
- related to the boson Born-level asymmetry when  $y_e$  is large

$$A_{ch}(y) \xrightarrow{y \rightarrow y_{max}} \frac{r(x_B) - r(x_A)}{r(x_B) + r(x_A)}, \quad r(x) \equiv \frac{d(x, M_W)}{u(x, M_W)}$$

- constrains the PDF ratio  $d(x, M_W)/u(x, M_W)$  at  $x \rightarrow 1$
- In experimental analyses, a selection cut  $p_{Te} > p_{Te}^{min}$  is imposed



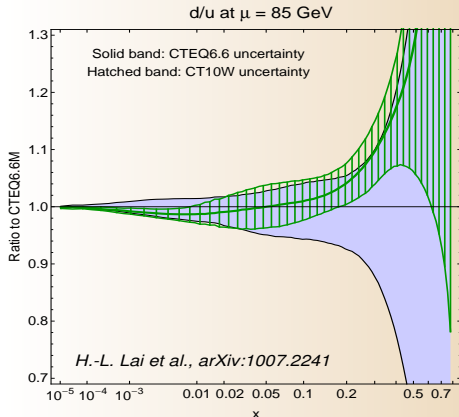
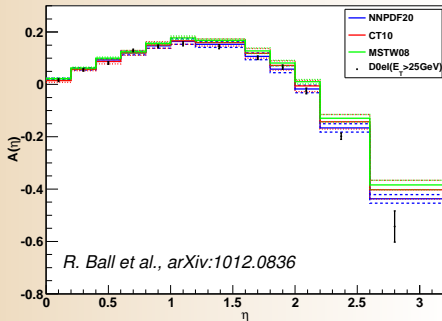
# Charge asymmetry in $p_T^e$ bins (CDF Run-2)



■ Without  $p_{Te}$  cuts,  $A_{ch}(y_e)$  is not sensitive to radiative contributions

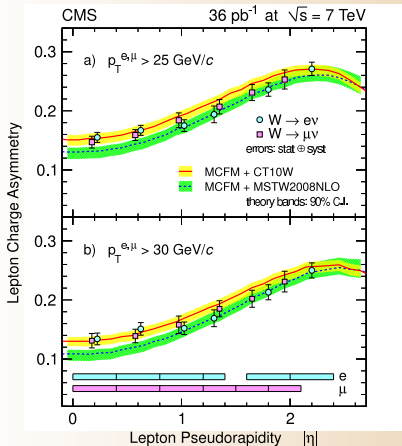
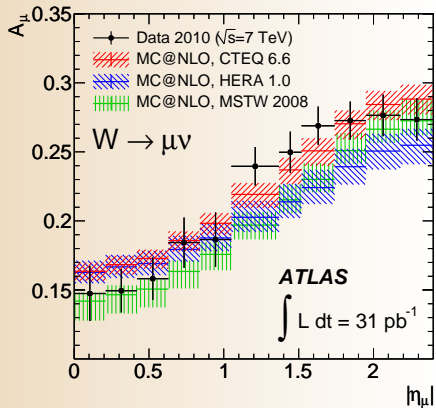
■ With  $p_{Te}$  cuts,  $A_{ch}(y_e)$  is sensitive to small- $Q_T$  resummation

# Impact of the Tevatron $A_{ch}$ data on PDFs



- The  $A_{ch}$  data distinguish between the PDF models, reduce the PDF uncertainty
- Very precise data!  $\Rightarrow$  Many subtleties in their analysis

# Charge asymmetry at the LHC



Sensitive both to  $d/u$  at  $x > 0.1$  **and**  $\bar{u}/\bar{d}$  at  $x \sim 0.01$  (not constrained well by other experiments)

# W and Z observables

## ■ Total cross sections

$$\sigma_Z = \int \frac{d\sigma(pp \rightarrow (Z \rightarrow e^+e^-)X)}{d\vec{p}_{e^+}d\vec{p}_{e^-}} d\vec{p}_{e^+}d\vec{p}_{e^-}$$

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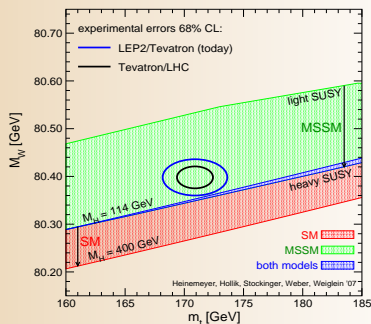
## Constraints on the Higgs sector and $W$ boson mass $M_W$

Both the Tevatron and LHC measure  $M_W$ . It provides key constraints on Higgs mass  $M_H$  in electroweak fits.

$$M_W = 80.3827 - 0.0579 \ln \left( \frac{M_H}{100 \text{ GeV}} \right) - 0.008 \ln^2 \left( \frac{M_H}{100 \text{ GeV}} \right)$$

In SM:

$$+0.543 \left( \left( \frac{m_t}{175 \text{ GeV}} \right)^2 - 1 \right) - 0.517 \left( \frac{\Delta\alpha_{had}^{(5)}(M_Z)}{0.0280} - 1 \right) - 0.085 \left( \frac{\alpha_s(M_Z)}{0.118} - 1 \right)$$



SM band:  $114 \leq M_H \leq 400 \text{ GeV}$

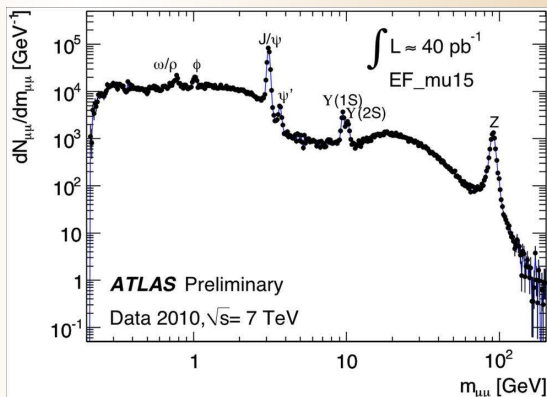
SUSY band: random scan

To know  $M_H$  to better than  $\pm 50 \text{ GeV}$  (50%) from the fit,  $M_W$  must be measured to better than  $\pm 0.030 \text{ GeV}$  (0.03%) – the accuracy that is already reached!

## Question to the audience

In  $p\bar{p} \rightarrow (Z \rightarrow \mu^+\mu^-)X$ , the value of  $M_Z$  is found from the resonance in  $d\sigma/dM_{\mu^+\mu^-}$

But in  $p\bar{p} \rightarrow (W \rightarrow \ell\nu)X$ ,  $d\sigma/dM_{\ell\nu}$  is not observed, because the  $\nu$ 's longitudinal momentum  $p_{\nu 3}$  is not measured!

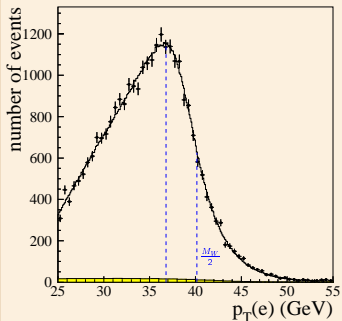


In this situation, which trick is used to measure  $M_W$ ?

# Jacobian peaks in distributions of decay leptons

Certain distributions contain a quasi-resonance (the Jacobian peak) that indicates the value of  $M_W$

## Electron's transverse momentum $p_T^e$



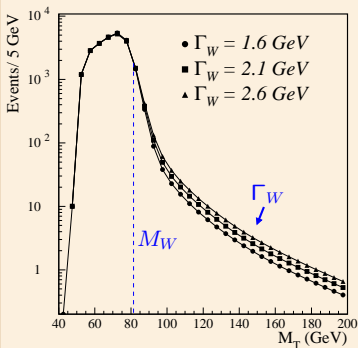
Jacobian peak at  
 $p_T^e = M_W/2 \approx 40$  GeV

# Jacobian peaks in distributions of decay leptons

Certain distributions contain a quasi-resonance (the Jacobian peak) that indicates the value of  $M_W$

## Leptonic transverse mass $M_T^{e\nu}$

(Smith, van Neerven, Vermaseren, 1983)



$$M_T^{e\nu} \equiv 2(p_T^e p_T^{\nu} - \vec{p}_T^e \cdot \vec{p}_T^{\nu})$$

Jacobian peak at  $M_T^{e\nu} = M_W$



# The origin of the Jacobian peak

In the  $W$  rest frame,  
for  $Q = M_W$ :

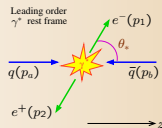
$$p_T^e = |\vec{p}_1| \sin \theta_* = \frac{M_W}{2} \sin \theta_*$$

$$\frac{d\sigma}{d \cos \theta_*} = \sum_j F_j(Q, Q_T, y) a_j(\theta_*, \varphi_*)$$

$a_1 = 1 + \cos^2 \theta_*$ ,  $a_2 = 2 \cos \theta_*$ , etc. (smooth functions)

$$\frac{d\sigma}{dp_T^e} = \underbrace{\left| \frac{d \cos \theta_*}{dp_T^e} \right|}_{\text{Jacobian}} \frac{d\sigma}{d \cos \theta_*} = \frac{1}{\sqrt{1 - \left( \frac{2p_T^e}{M_W} \right)^2}} \frac{4p_T^e}{M_W^2} \frac{d\sigma}{d \cos \theta_*}$$

$$\frac{d\sigma}{dp_T^e} \rightarrow \infty \text{ if } p_T^e \rightarrow M_W/2 (!)$$



# The origin of the Jacobian peak

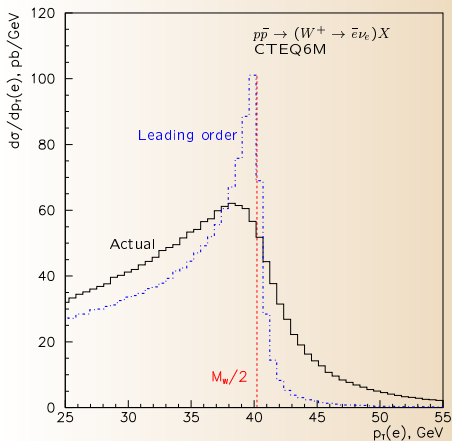
$$\text{If } Q_T = 0: (p_T^e)_{\text{lab frame}} = (p_T^e)_{\text{CS frame}}$$

(the boost from the CS frame to the lab frame is along the  $z$ -axis)

Corrections to  $d\sigma/dp_T^e$  are of order

■  $\mathcal{O}(\Gamma_W^2/M_W^2)$  due to the non-zero  $W$  width  $\Gamma_W$  ( $Q \neq M_W$ )

■  $\mathcal{O}(Q_T/Q)$  due to the boost  $\Rightarrow$  sensitivity to the shape of  $d\sigma/dQ_T$  (soft radiation) at  $Q_T \ll Q$



A similar Jacobian peak is present in  $d\sigma/dp_T^{\nu}$

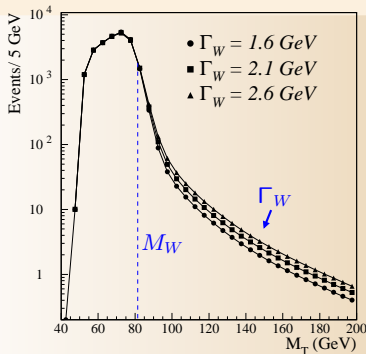
# More on lepton transverse mass

## Exercise

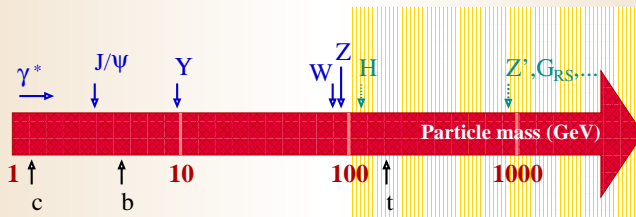
Assuming  $Q_T = 0$ , verify that there is a Jacobian peak in  $d\sigma/dM_T^{e\nu}$  at  $M_T^{e\nu} = M_W$

■ Corrections to  $d\sigma/dM_T^{e\nu}$  are of order  $\mathcal{O}(Q_T^2/Q^2) \Rightarrow$  reduced sensitivity to small- $Q_T$  soft contributions

■  $d\sigma/dM_T^{e\nu}$ ,  $d\sigma/dp_T^e$ , and  $d\sigma/dp_T^\nu$  are commonly used to measure  $M_W$ .  $\Gamma_W$  is found from  $d\sigma/dM_T^{e\nu}$  at large  $M_T^{e\nu}$

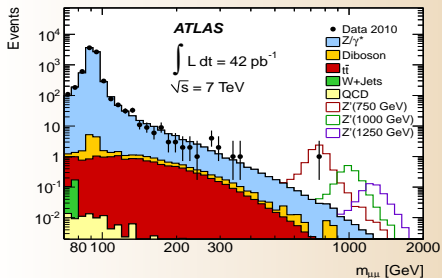


# Final states in DY-like processes

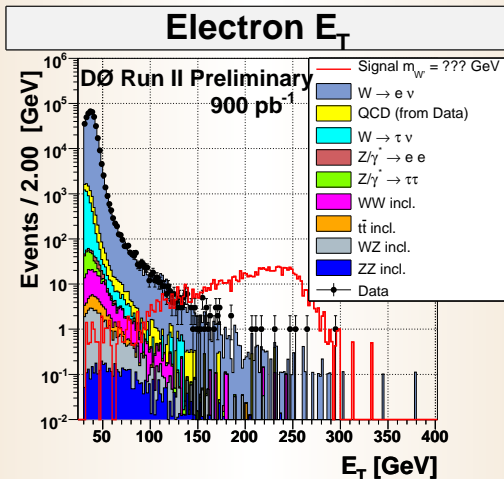


## New physics at $Q > 100$ GeV

- Indirect constraints from electroweak precision measurements
- direct new physics searches

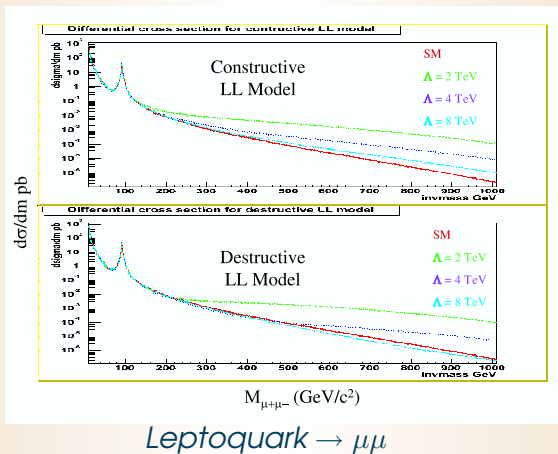


# Search for heavy states at D0

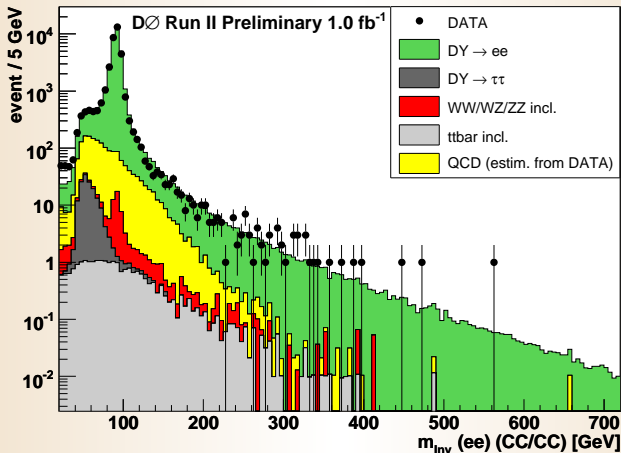


$$W' \rightarrow l\nu$$

# Search for heavy states at DO

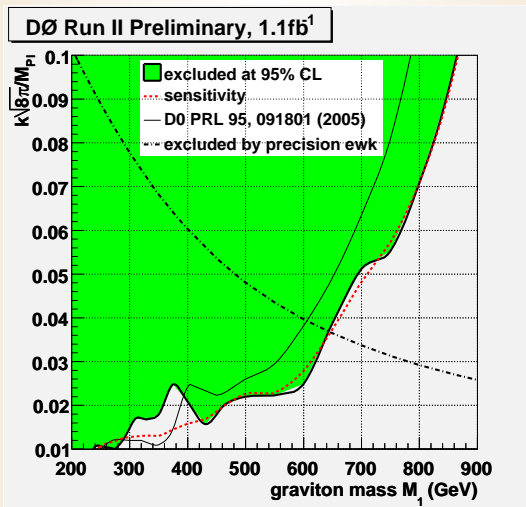


# Search for heavy states at D0



Contact interactions:  $p\bar{p} \rightarrow e(e^* \rightarrow e\gamma)X$

# Search for heavy states at DØ



Randall-Sundrum graviton  $\rightarrow ee, \gamma\gamma$



# Summary

Essential applications of Drell-Yan-like processes

- clean tests of QCD factorization
- studies of the nucleon structure (quark sea, flavor separation,...)
- “standard candle” processes (NNLO,...)
- electroweak precision measurements
- searches for new physics

Many interesting topics were not covered

- Polarized Drell-Yan-like processes (measurements of new nucleon structure functions)
- Connections to  $k_T$  factorization
- Various resummations ( $Q_T$ , small  $x$ , threshold, heavy-quark....)
- Drell-Yan production in heavy-ion scattering