

Using the substructure of jets

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- This talk is about analysis methods that use jet substructure.
- I first briefly define three analysis methods: mass drop plus filtering, trimming, & pruning.
- Then I examine the structure in nature that these methods try to exploit and that future methods can use.

Signal and background

- We seek new physics signals in a standard model background.
- In Eugene OR, there are many background creatures.



- There are signal creatures that look a somewhat like background creatures, but there are very few of them.

- A signal creature.

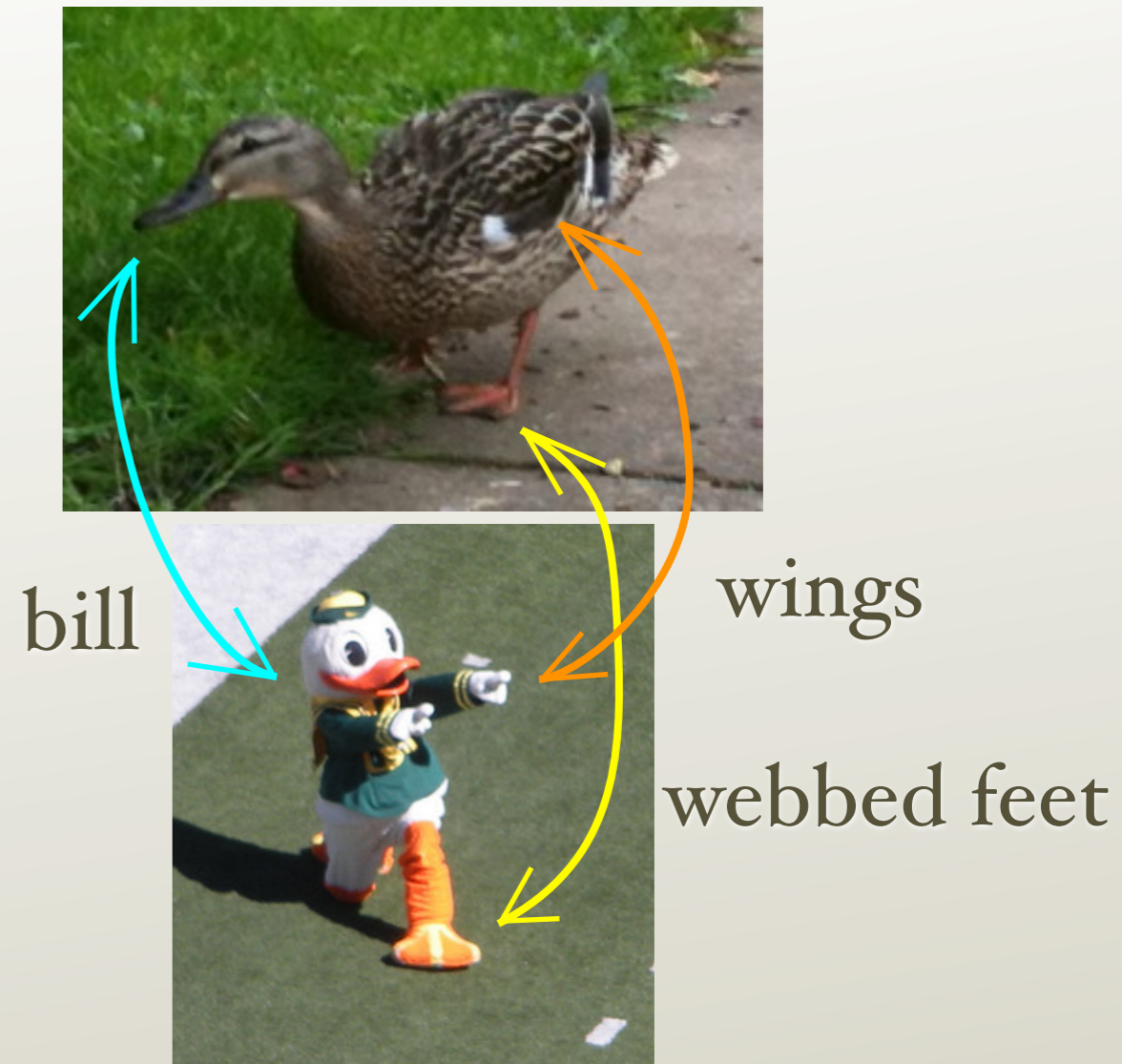


- There are many features in common between signal and background creatures.

- We need to find the differences. (Eg. one of these can't swim.)

- Unfortunately, background creatures come with a range of mutations that make them sometimes look like a signal creatures.

- Thus we look need a statistical method to tell if there are signal creatures.

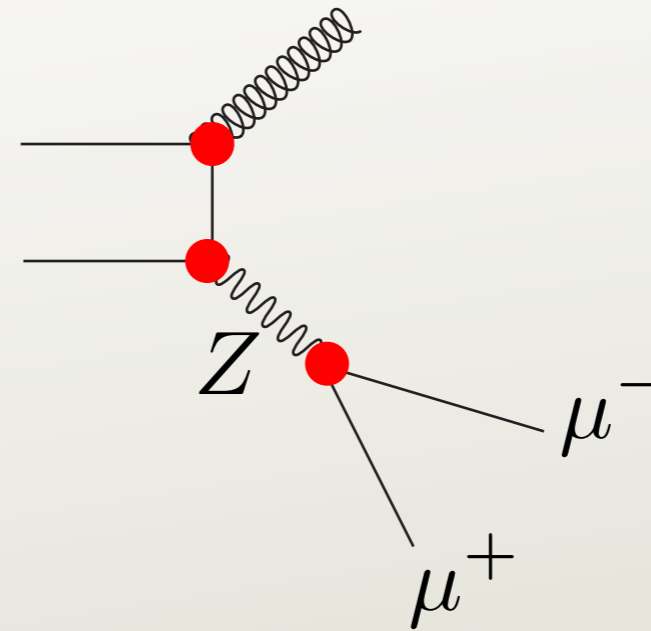
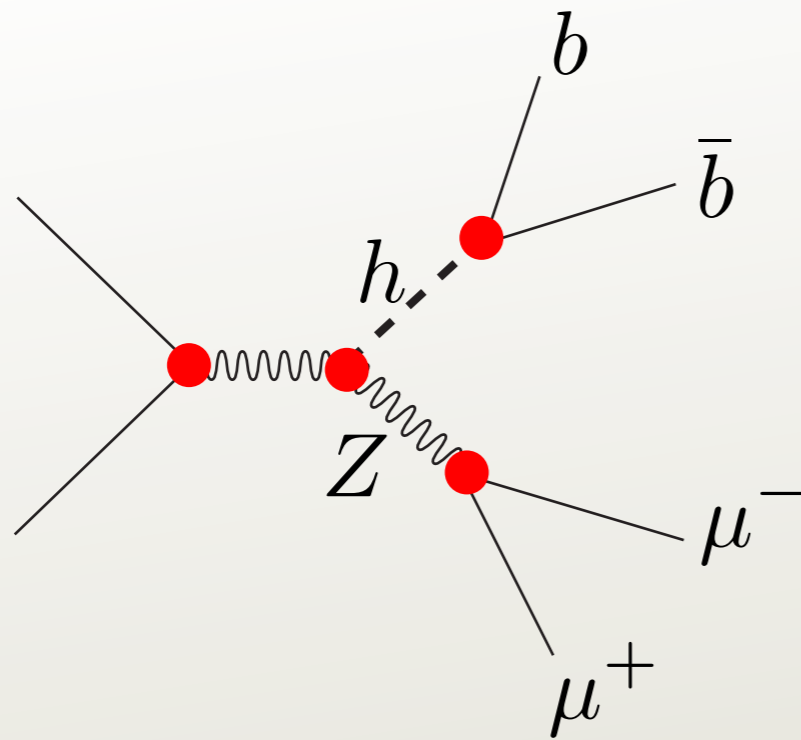


Signals and backgrounds at the LHC

Signal & background have jets

- Consider $p + p \rightarrow h + Z$. Butterworth, Davison,
Rubin, and Salam (2008)
$$\begin{array}{ccc} & & \ell^+ + \ell^- \\ & \swarrow & \searrow \\ & b + \bar{b} & \end{array}$$

- We demand that the Higgs have large p_T .
- That makes it easier to find.
- We may ask for b tags if we know where to look.
- Backgrounds: $p + p \rightarrow Z + jets$ and $p + p \rightarrow Z + Z$.
- The b and \bar{b} are seen as jets.
- Background events have jets.



We want to find this.

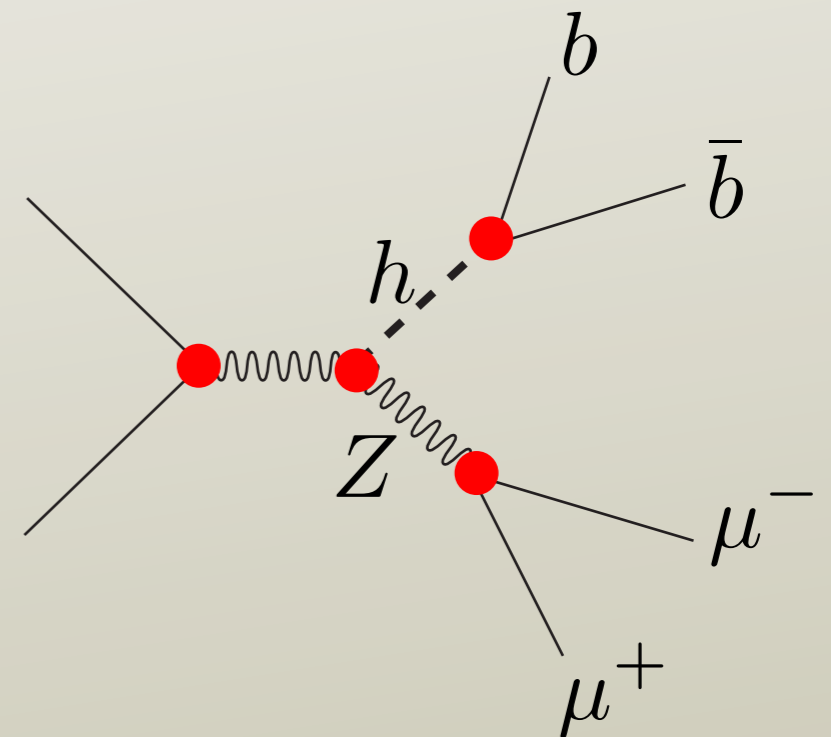
In a background of this.

- The gluon could split to two gluons, making the background look a lot like the signal.
- The gluon could split into $b\bar{b}$, making the background look even more like the signal.
- But the Higgs boson has a big mass, while a gluon has mass zero, so we can look for a mass bump.

Start with event selection

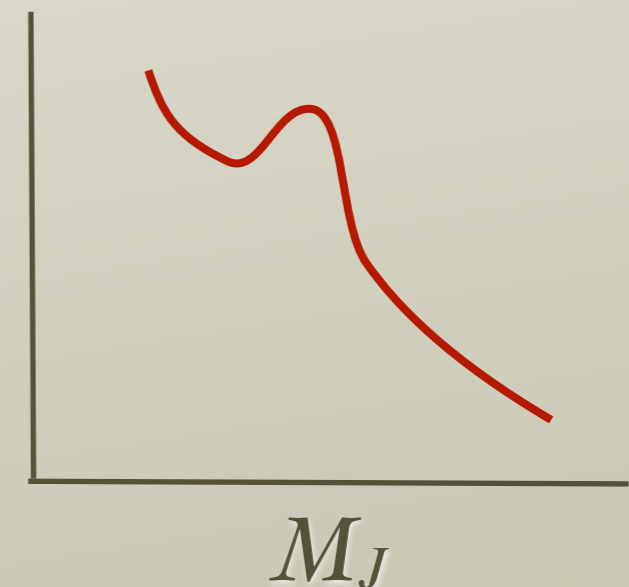
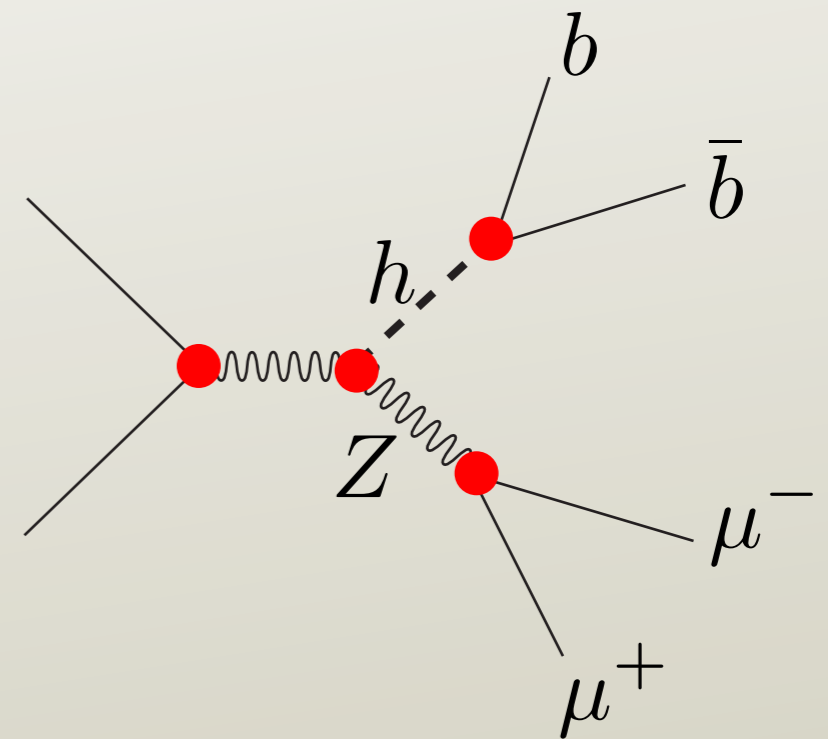
- Electron or muon pair near the Z mass.
- Large P_T of the lepton pair and of recoiling jet (>200 GeV).
- Large P_T implies that the possible Higgs decay products are easier to isolate: they are part of a (rather fat) jet.

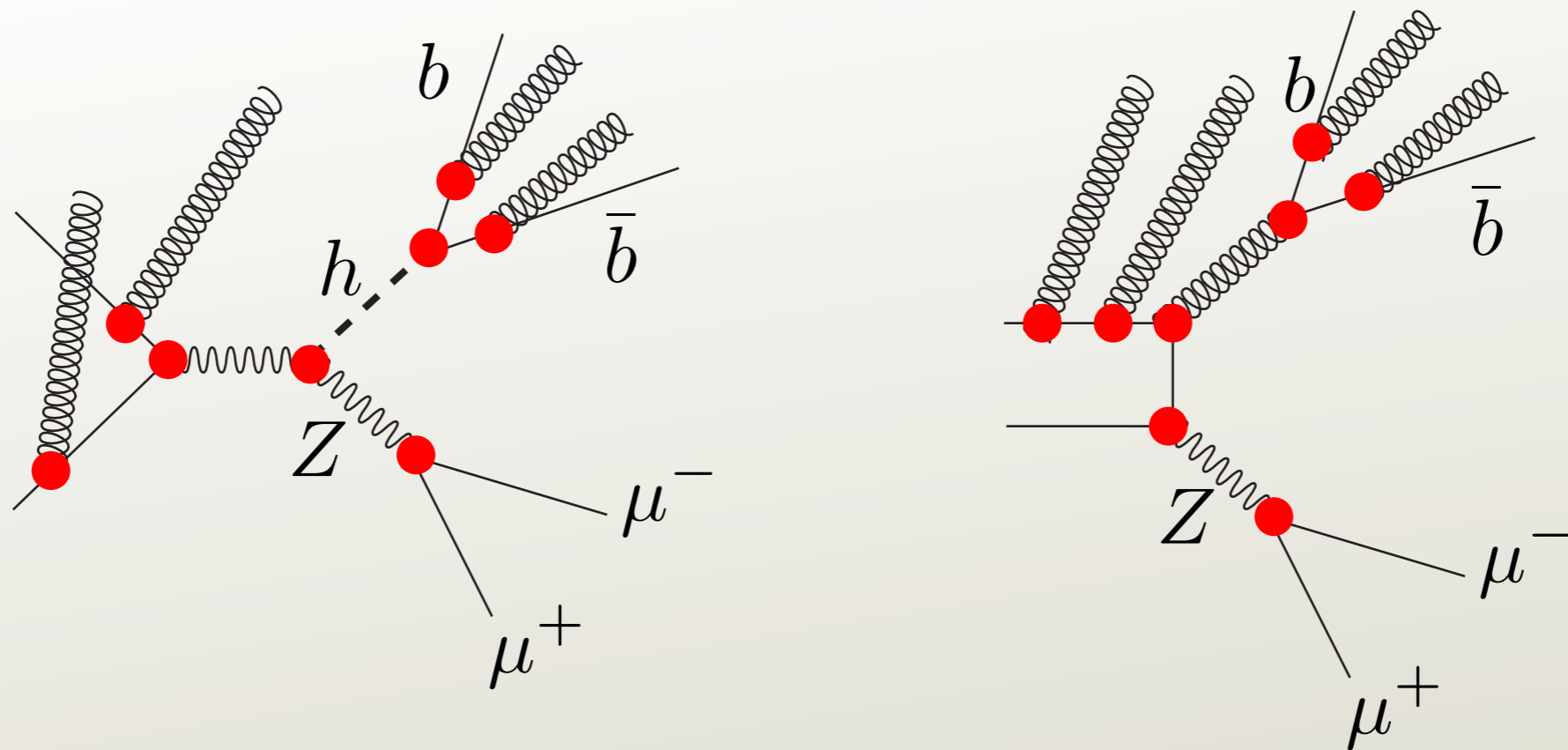
Butterworth, Davison, Rubin, and Salam (2008)



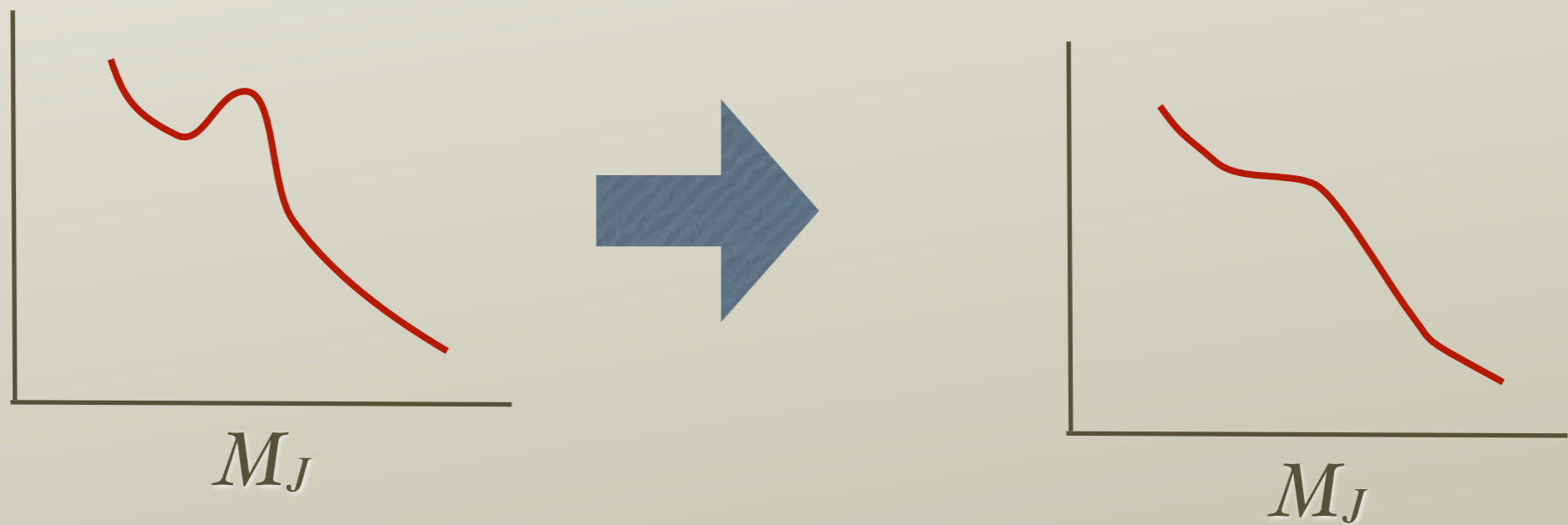
Define the fat jet

- Look for a high P_T jet using the Cambridge-Aachen (angle) algorithm with $R=1.2$.
- We might hope that the distribution of the mass of the fat jet shows a bump at the Higgs mass.



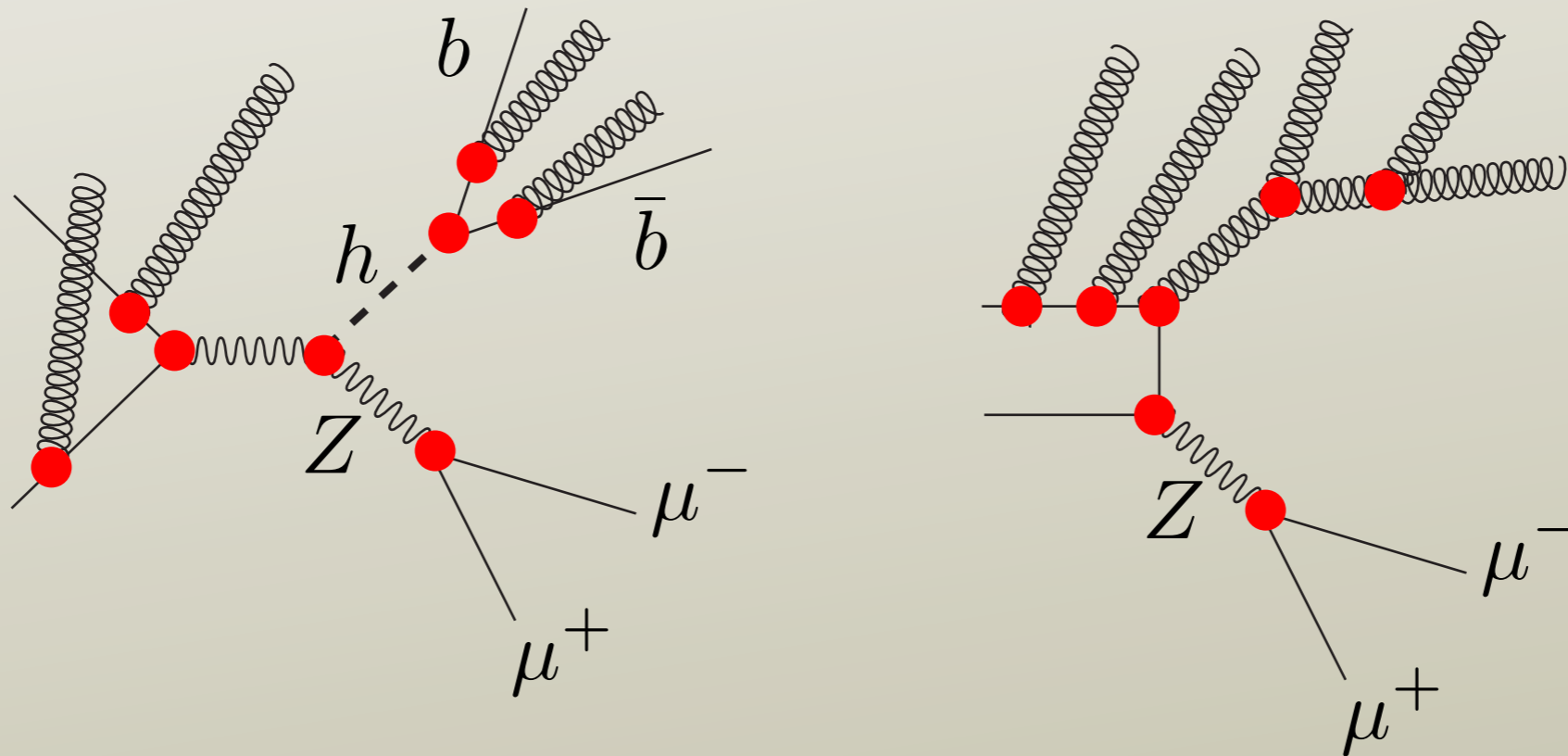


- Since QCD is operating, the mass bump gets smeared out.



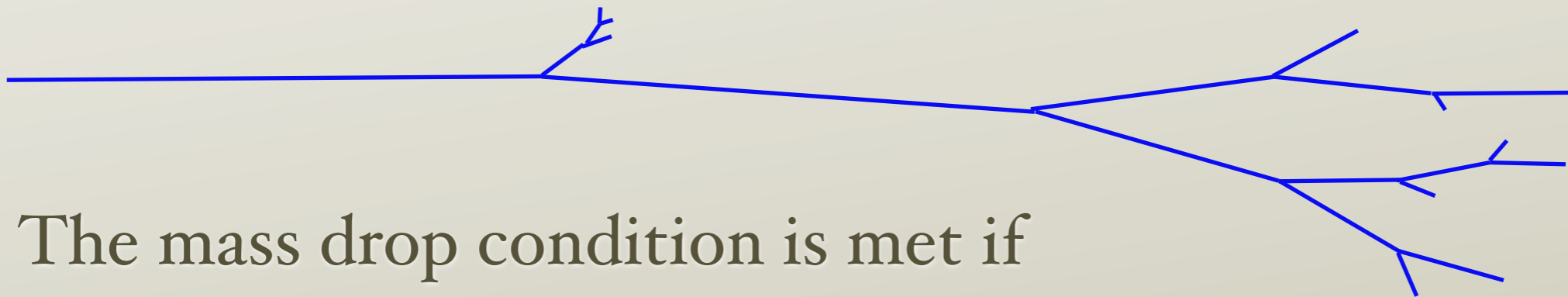
Subjet analysis

- We would like to take apart the fat jet in order to get rid of the contaminating initial state radiation.



Jet mass drop and filtering

- Step I: mass drop.
 - Examine the C-A splitting tree, starting at the trunk.



- The mass drop condition is met if

$$\max(M_i, M_j) < 0.67 M_{\{i,j\}}$$

$$\min(p_{T,i}^2, p_{T,j}^2) [(y_i - y_j)^2 + (\phi_i - \phi_j)^2] > 0.09 M_{\{i,j\}}^2$$

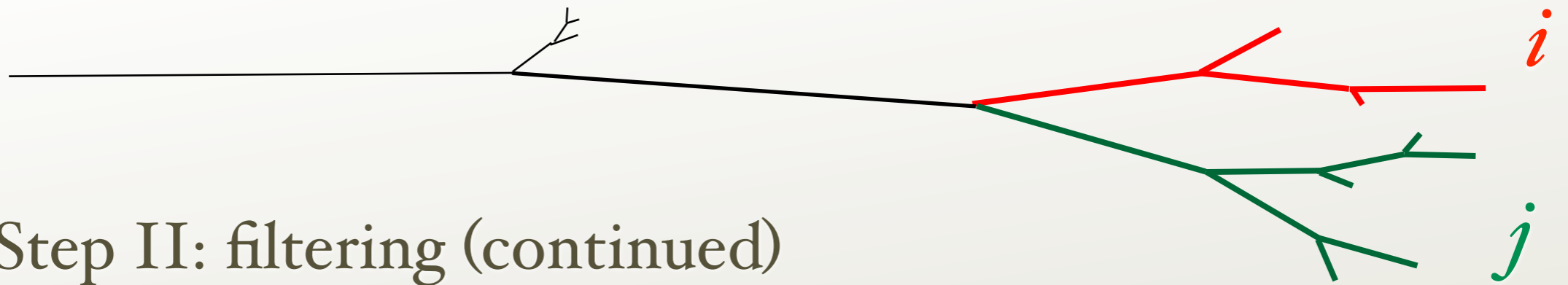


- If mass drop condition isn't met, drop smaller p_T daughter and keep looking.
- If it is never met, remove the event from your sample.





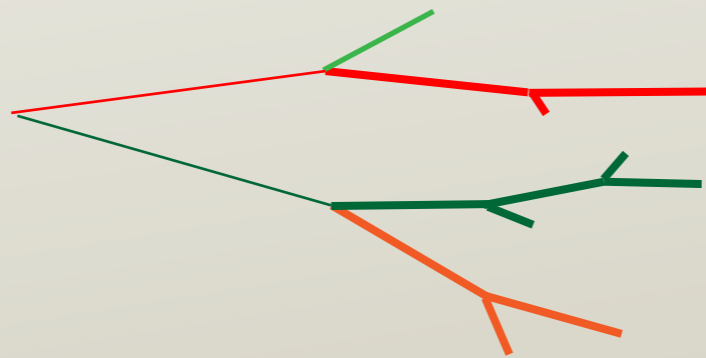
- Step II: filtering the prospective b -jets, i and j .
 - Are both prospective b -jets tagged as containing b -quarks?
 - (In simulating this, we assuming a b -tagging efficiency of 60% and a misstag probability of 2%)
 - If i and j are not b -tagged, reject the event.



- Step II: filtering (continued)

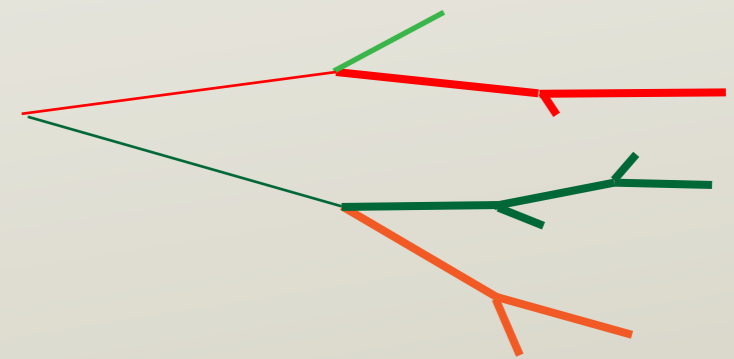
- Apply the C-A algorithm with to protojets i and j with

$$R = \min \left(\frac{1}{2} [(y_i - y_j)^2 + (\phi_i - \phi_j)^2]^{1/2}, 0.3 \right)$$

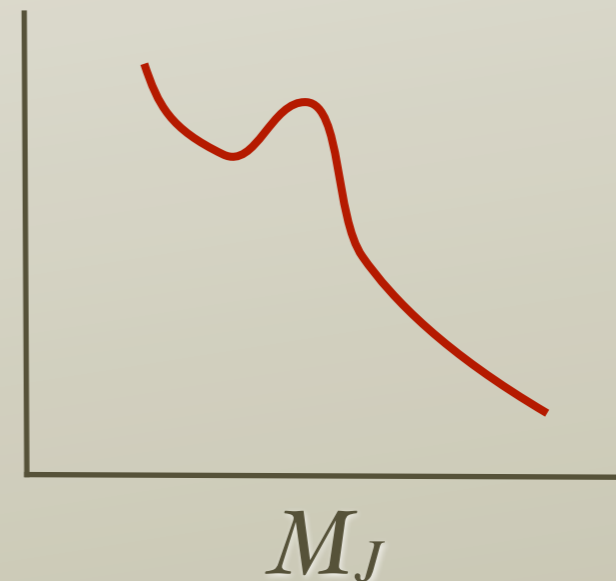
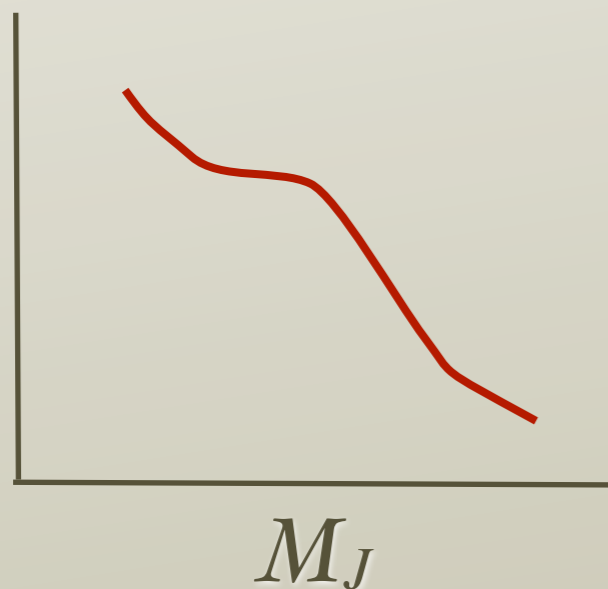


- Are the two highest p_T subjects thus found tagged as containing b-quarks?
- If not, throw out the event.

- Step II: filtering (continued some more)
 - Throw out all but the three highest p_T subjets thus found.
 - What remains is the filtered jet.

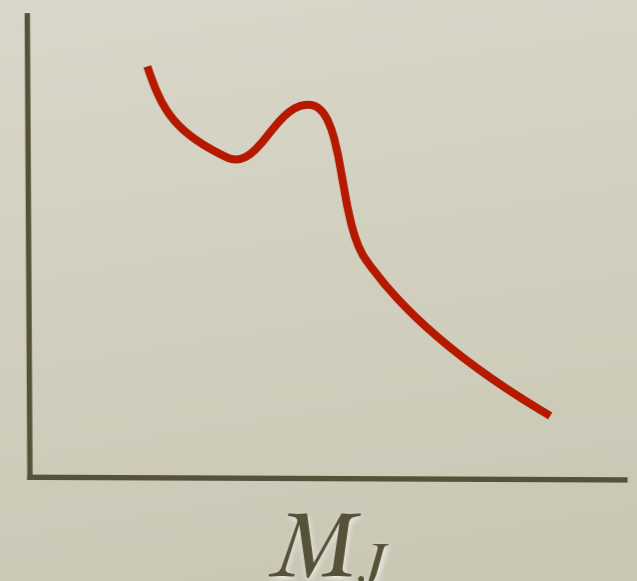
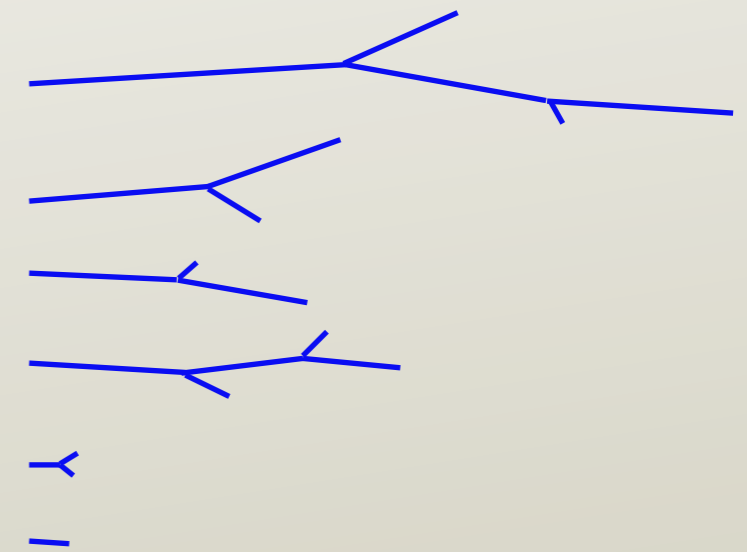


- Measure the mass of this filtered jet.



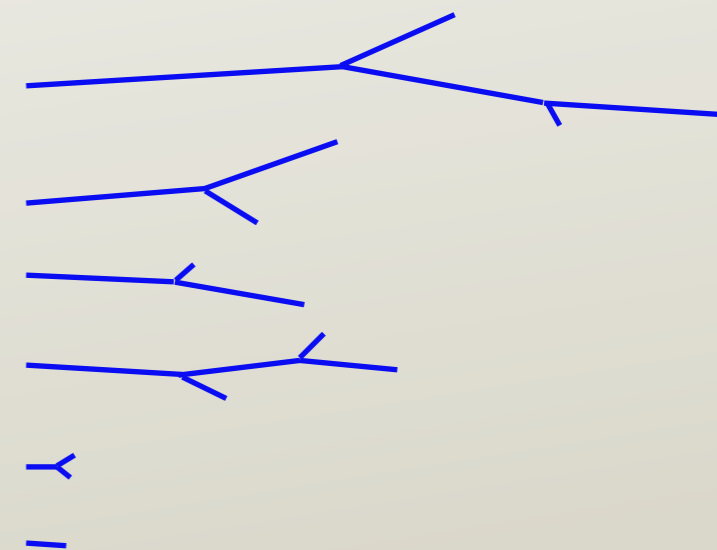
Jet trimming

- Define the fat jet with the anti- k_T algorithm with $R = 1.2$.
- Group starting protojets into successively fatter protojets with the k_T algorithm with $R = 0.2$.
- This gives several final jets, some with large p_T , some with small p_T .
- Now throw away the jets that are too soft. (Say, $p_T < 0.03 P_T(\text{fat jet})$.)
- Measure the mass of this trimmed jet.



Jet pruning

- Define the fat jet with the C-A algorithm with $R = 1.2$.
- Step I
 - Group starting protojets into successively fatter protojets with the C-A algorithm with
$$R = M(\text{fat jet}) / P_T(\text{fat jet})$$
 - That is, merge protojets until no pair has an angle smaller than this.



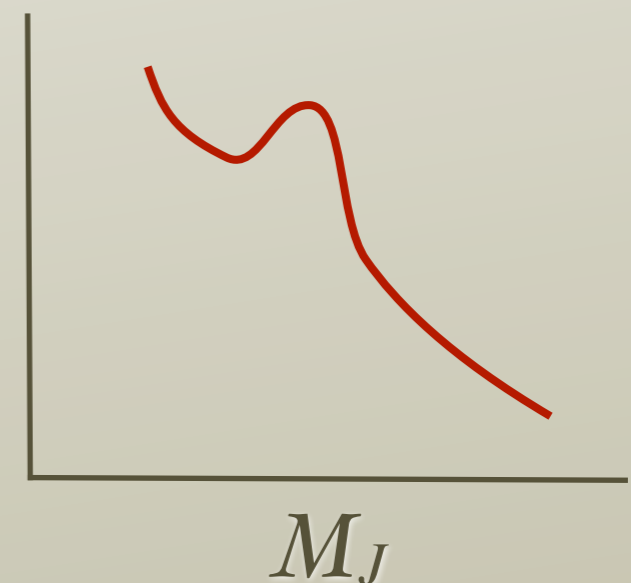
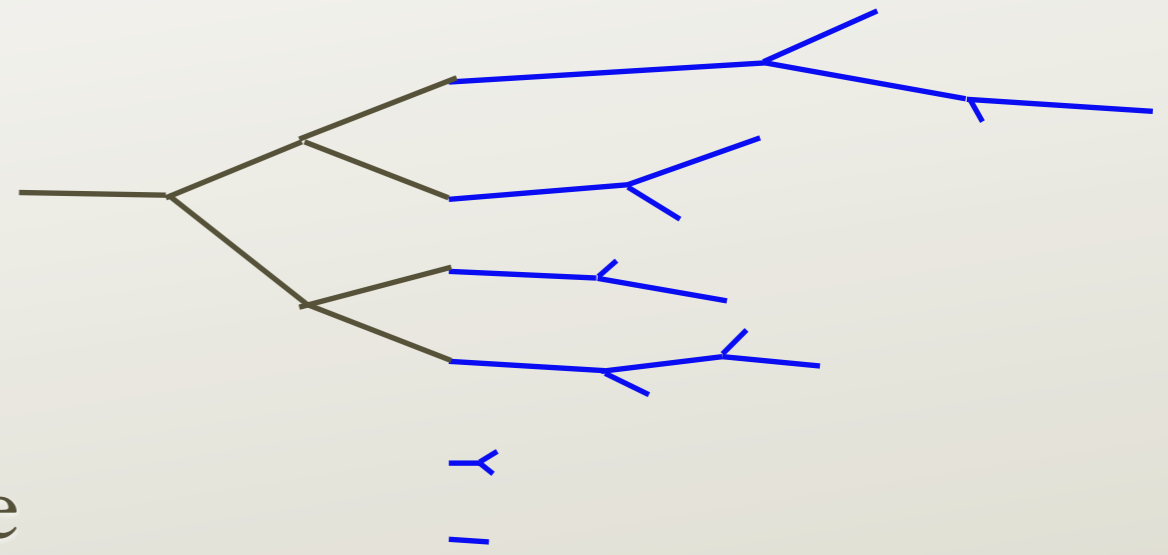
- Step II

- Continue merging up to larger angles. Examine

$$z = \frac{\min(p_{T,i}, p_{T,j})}{|\vec{p}_{T,i} + \vec{p}_{T,j}|}$$

- If $z < 0.1$, cancel the merge and omit the small p_T protojet.
- Continue until all protojets are merged or eliminated.

- Measure the mass of this pruned jet.

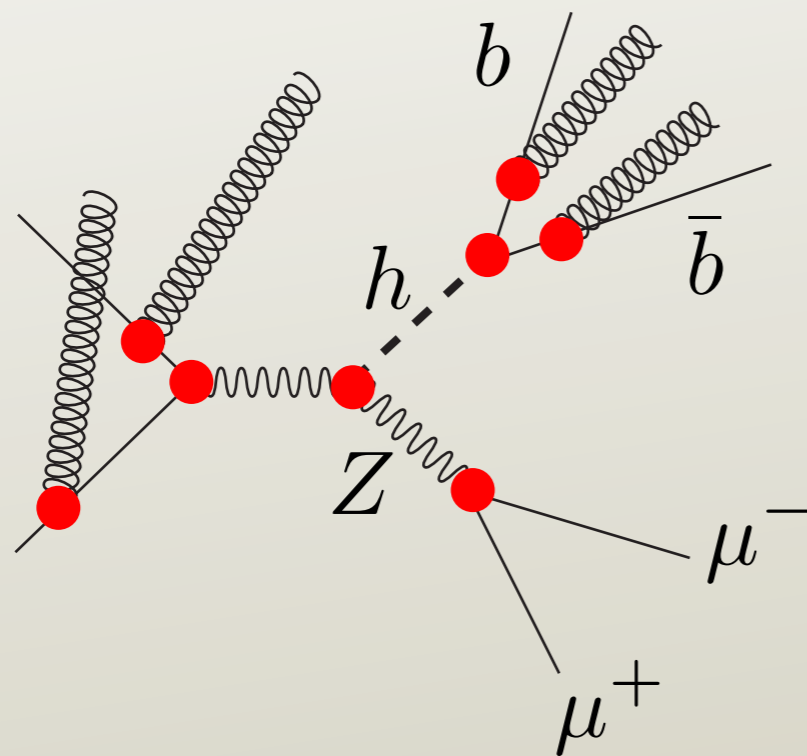


What gauge field theory has to say

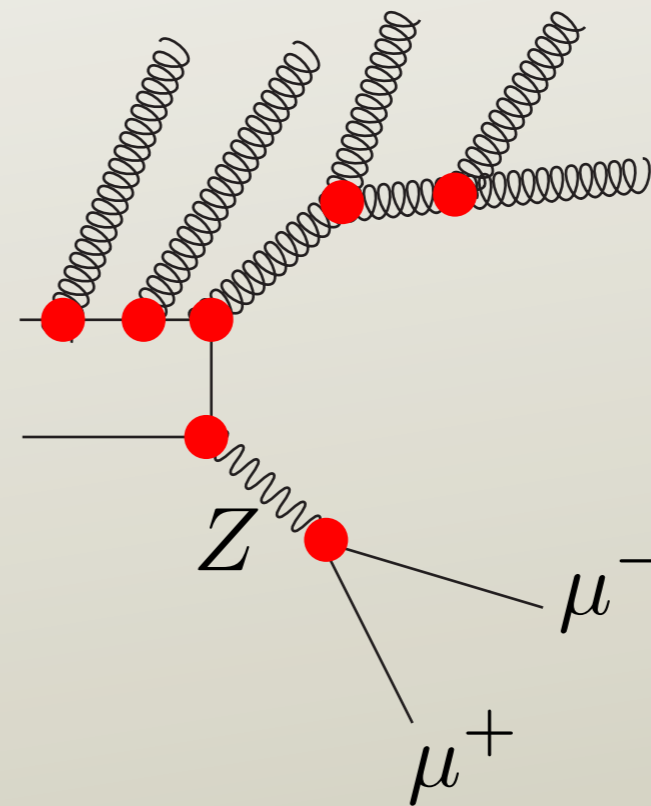
- One can use field theory to understand the characteristics of background events and the characteristics of signal events (with heavy particle decays).
- Schemes for selecting signal events depend on using the similarities and differences in signal and background events.
- I will try to outline the characteristics that can be used.

Initial state radiation

- One immediate similarity is that both signal and background events have initial state radiation.



A Higgs signal event

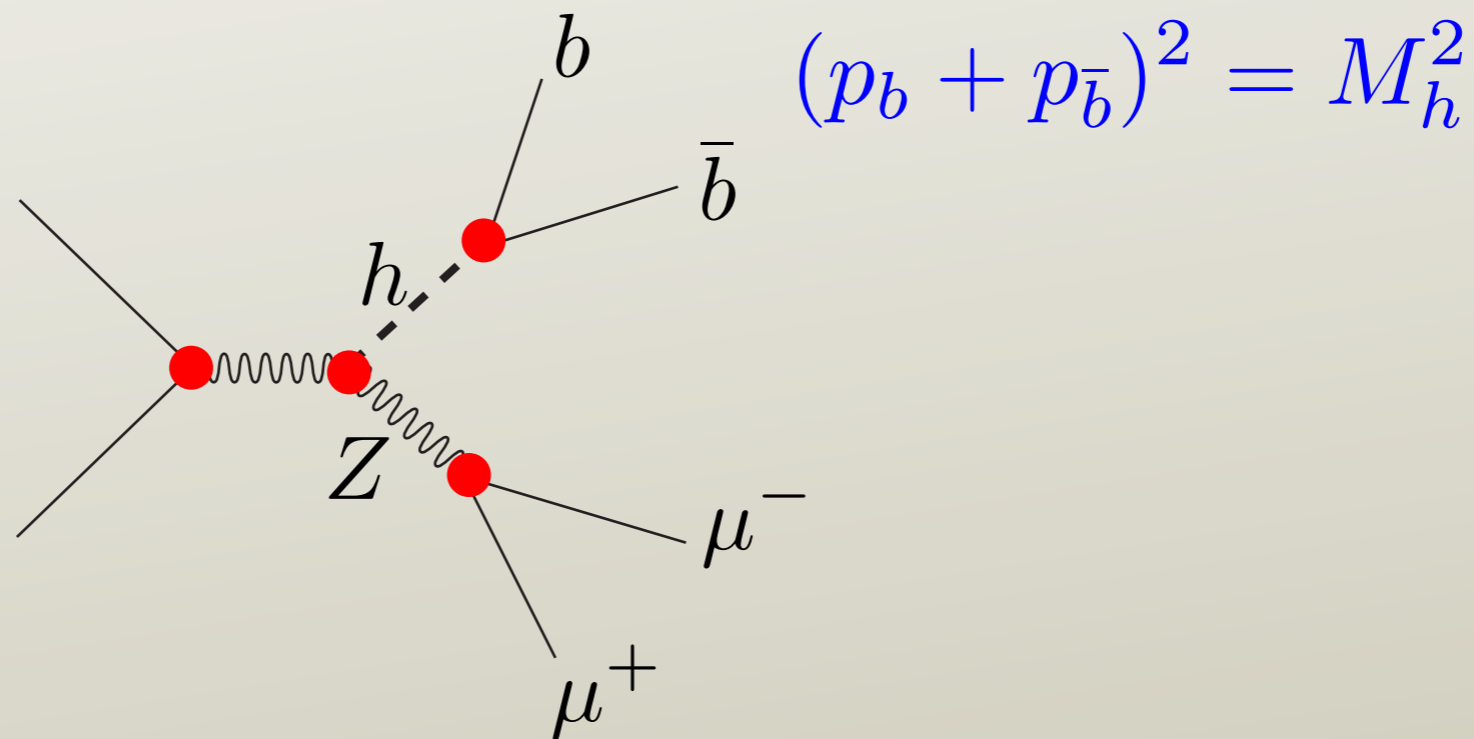


A similar background event

- This makes the signal/background separation difficult.
- More on this later.

Mass bumps

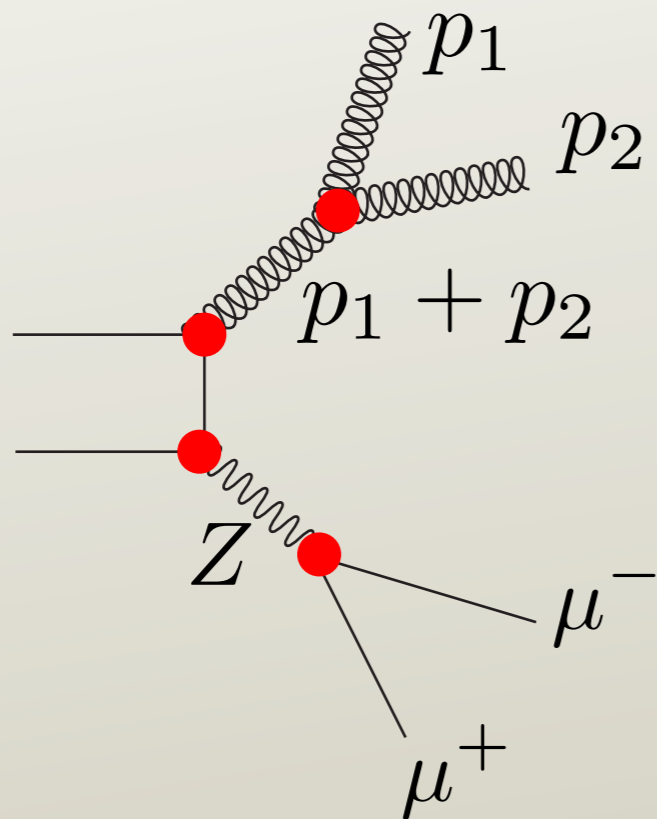
- One key feature of signal events is that the decay products of a heavy particle have a fixed mass.



- The theoretical uncertainty of this is $M_h \Gamma_h$.
- The practical uncertainty is much larger.

Mass in QCD splittings

- QCD splittings have a very different distribution as a function mass.



- I will use a scaled virtuality as a “hardness variable”:

$$v = \frac{(p_1 + p_2)^2}{(p_1 + p_2) \cdot Q_0}$$

- Q_0 is the momentum of the outgoing partons in the hard process.

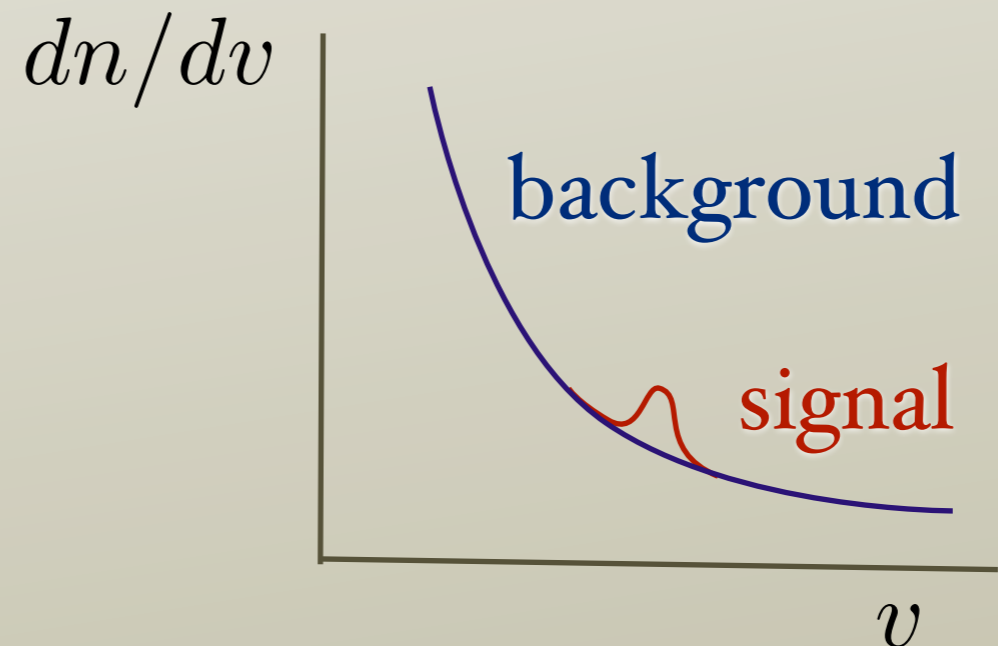
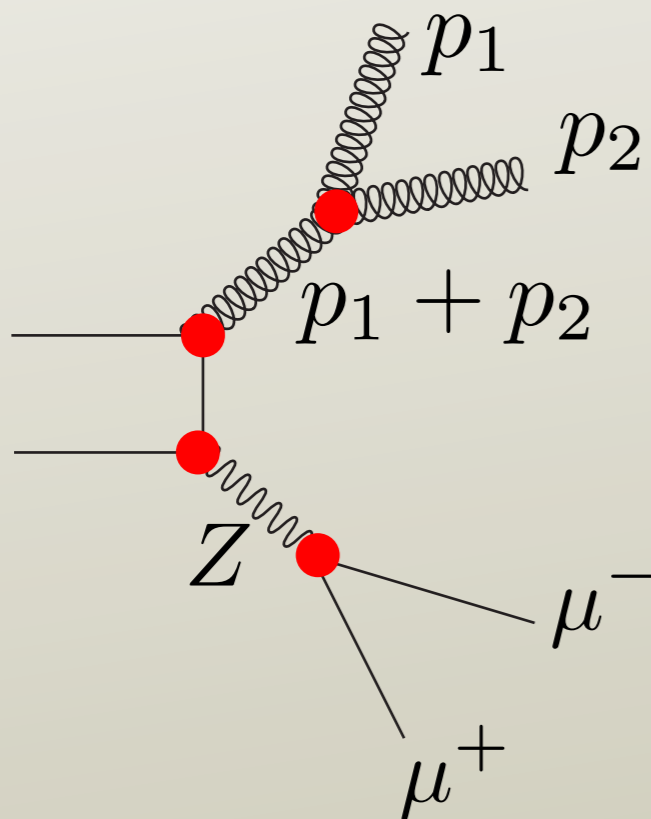
QCD tree graph results

$$v = \frac{(p_1 + p_2)^2}{(p_1 + p_2) \cdot Q_0}$$

- Differential probability is

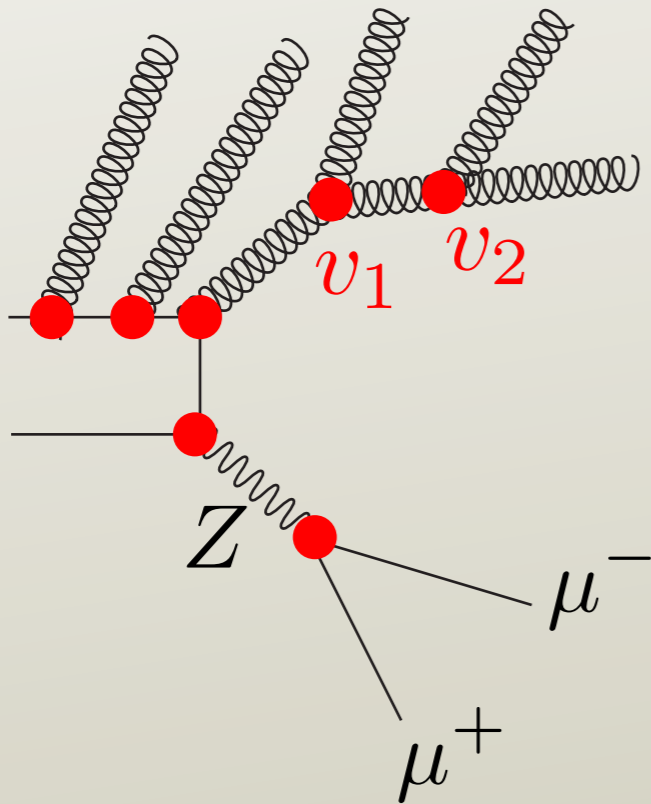
$$dn \propto \frac{dv}{v} \alpha_s \log(v/\tilde{v})$$

- The log (and \tilde{v}) comes from $\int dz$.



Nested splittings

- The same structure can be (approximately) iterated.

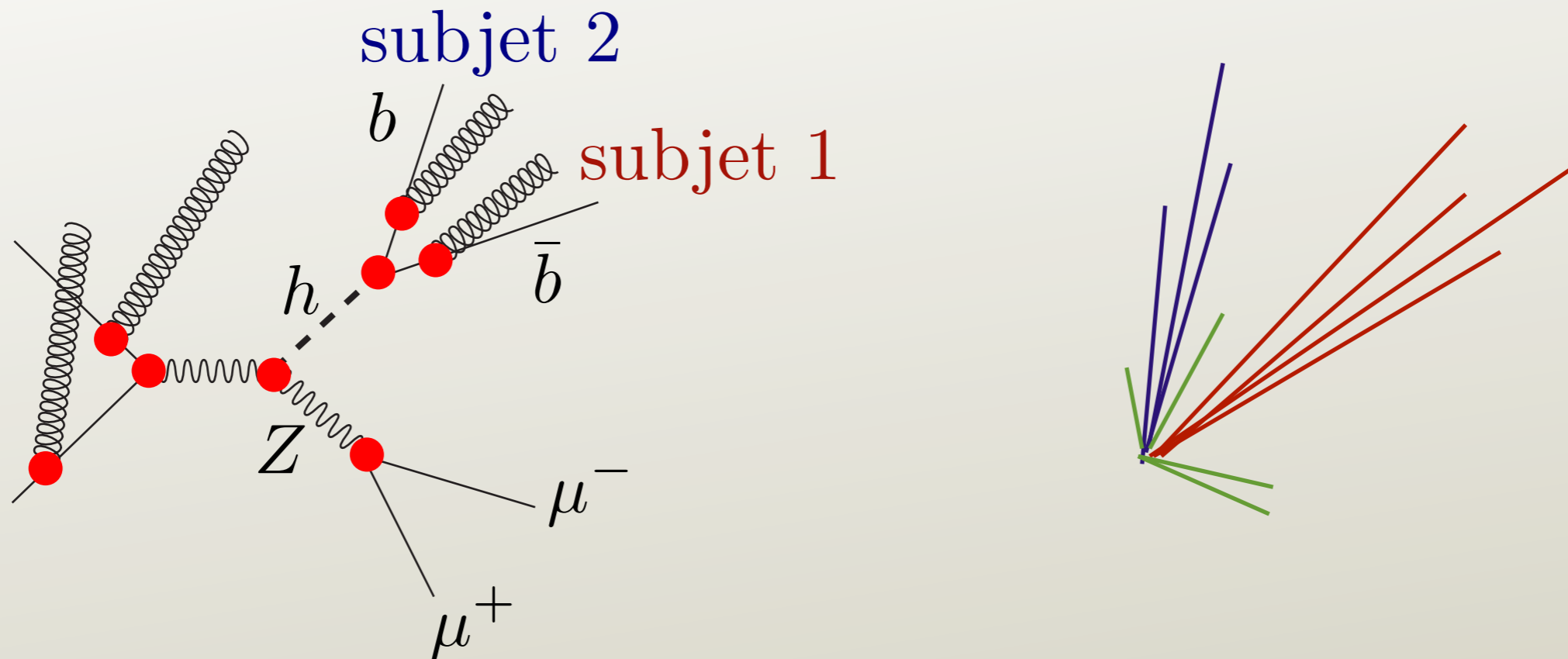


- $v_2 < v_1$.

- Set $v_2 = 0$ in splitting 1.

$$dn = \frac{dv_1}{v_1} \alpha_s \log(v_1/\tilde{v}_1) \times \frac{dv_2}{v_2} \alpha_s \log(v_1/\tilde{v}_2) \theta(v_2 < v_1)$$

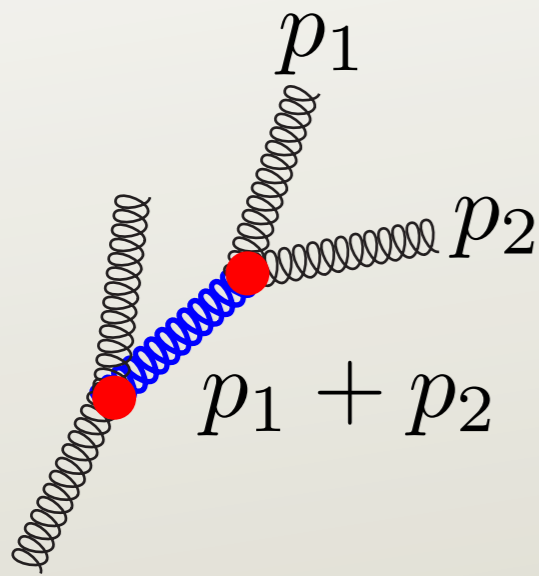
An application of this



- A Higgs boson will likely decay to two low mass subjects.
- Try to find the low mass subjects.
- A “mass drop” condition can be part of this.
(Butterworth, Davison, Rubin & Salam.)
- Measure the mass of subject pair.

Sudakov factor

- A better approximation for dn includes a Sudakov factor.



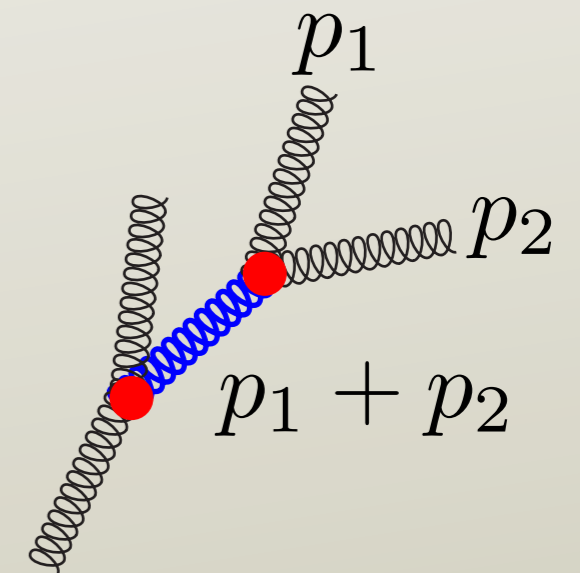
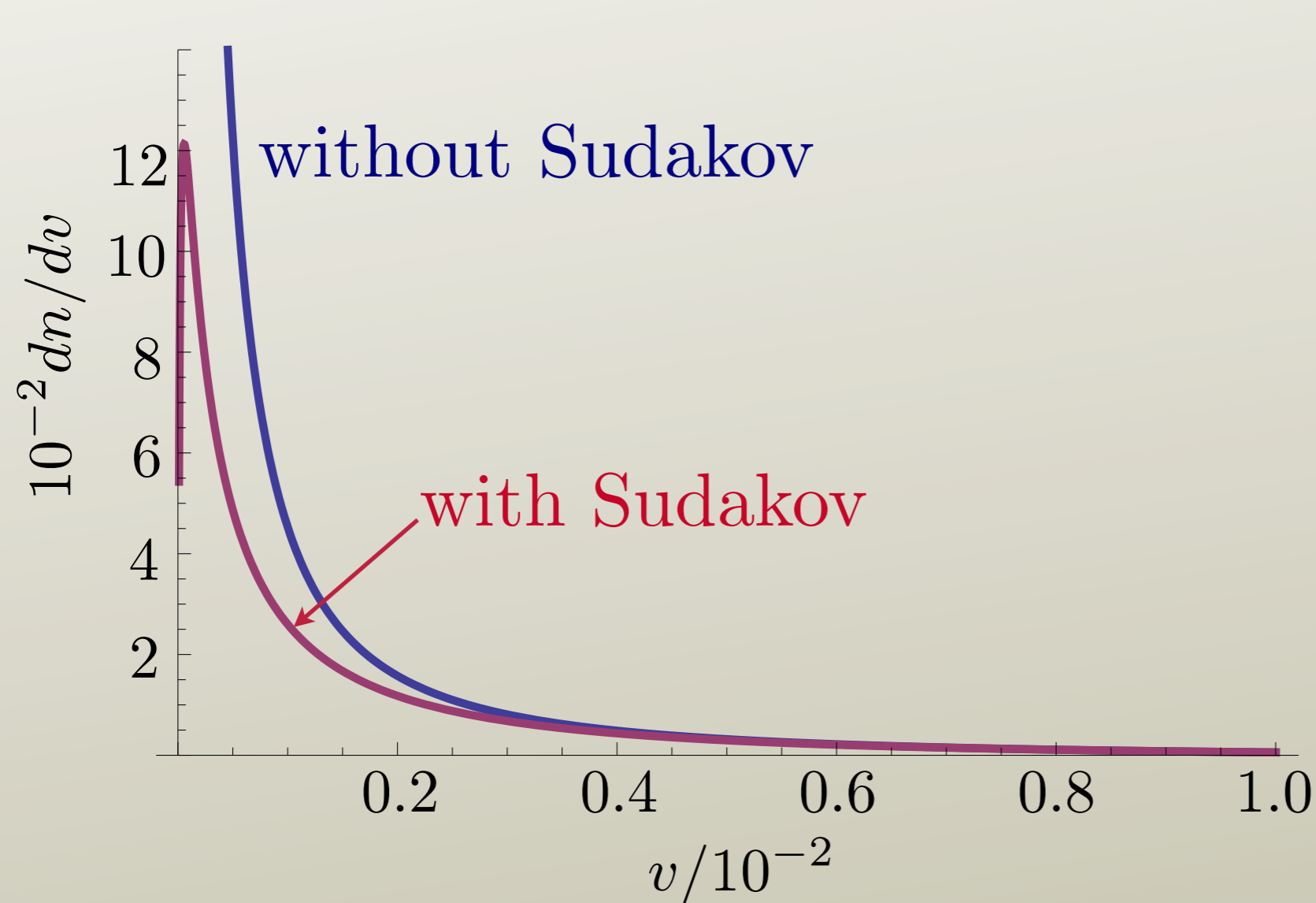
$$dn = \frac{dv}{v} \frac{\alpha_s}{2\pi} 2C_A \log(v/\tilde{v})$$

$$\exp\left(-\int_v^{v_1} \frac{d\bar{v}}{\bar{v}} \frac{\alpha_s}{2\pi} 2C_A \log(\bar{v}/\tilde{v})\right)$$

- We think of a renormalization group approach with a running resolution scale.
- The Sudakov factor accounts for virtual graphs and unresolved real parton emissions.

Example of effect of Sudakov

$$dn = \frac{dv}{v} \frac{\alpha_s}{2\pi} 2C_A \log(v/\tilde{v}) \exp\left(-\int_v^{v_1} \frac{d\bar{v}}{\bar{v}} \frac{\alpha_s}{2\pi} 2C_A \log(\bar{v}/\tilde{v})\right)$$



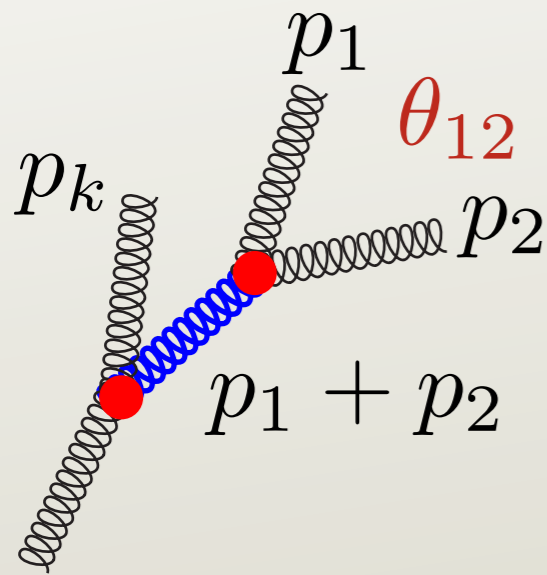
$$Q_0^0 = 1000 \text{ GeV}$$

$$|\vec{p}_1 + \vec{p}_2| = 100 \text{ GeV}$$

$$v_1 = 10^{-2}$$

$$\theta_{\max} = 0.3$$

Distribution in angles



- For a given v , what is the distribution in the angle θ_{12} between \vec{p}_1 and \vec{p}_2 ?

- Kinematically,

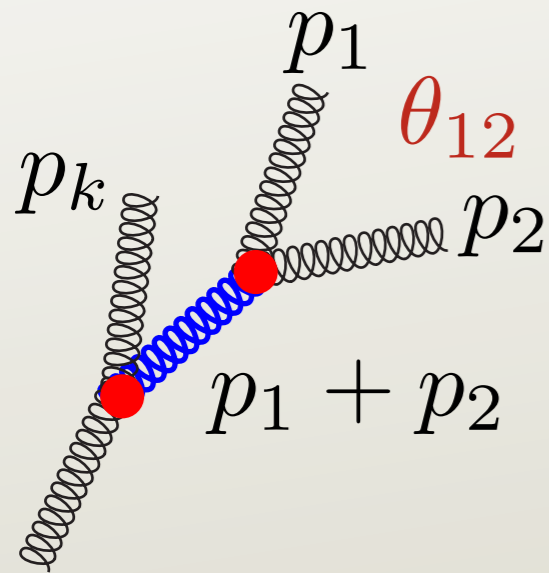
$$\theta_{12}^2 > v \frac{4Q_0^2}{(p_1 + p_2) \cdot Q_0}$$

- For larger, but not too large, θ_{12} ,

$$v = \frac{(p_1 + p_2)^2}{(p_1 + p_2) \cdot Q_0}$$

$$dn \propto \frac{d\theta_{12}^2}{\theta_{12}^2}$$

Large angles



- Large θ_{12} corresponds to $|\vec{p}_1| \ll |\vec{p}_2|$.
- (Or gluon 2 could be the soft one.)
- For emission of soft gluon 1, interference with emission from parton k is important.
- Parton k is the color connected partner.

- With interference,

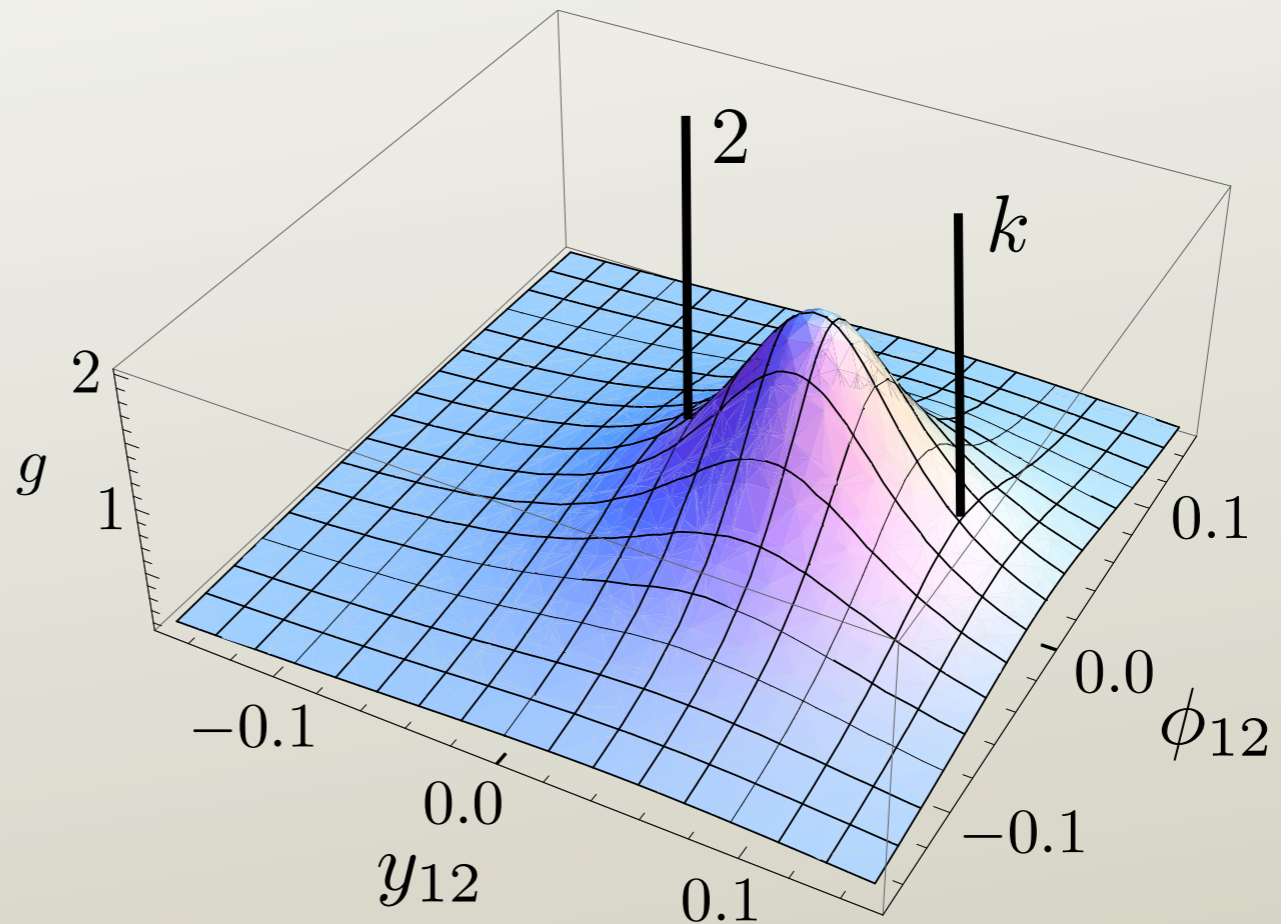
$$dn \propto \frac{d\theta_{12}^2}{\theta_{12}^2} g(\theta_{12}^2)$$

$$g(\theta_{12}^2) = \frac{\theta_{2k}^2}{\theta_{12}^2 + \theta_{1k}^2}$$

Effect of the angle factor

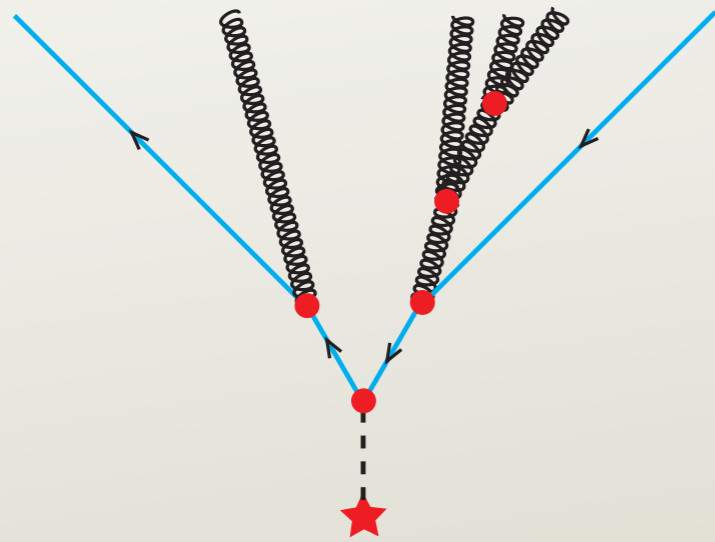
$$dn \propto \frac{d\theta_{12}^2}{\theta_{12}^2} g(\theta_{12}^2)$$

$$g(\theta_{12}^2) = \frac{\theta_{2k}^2}{\theta_{12}^2 + \theta_{1k}^2}$$



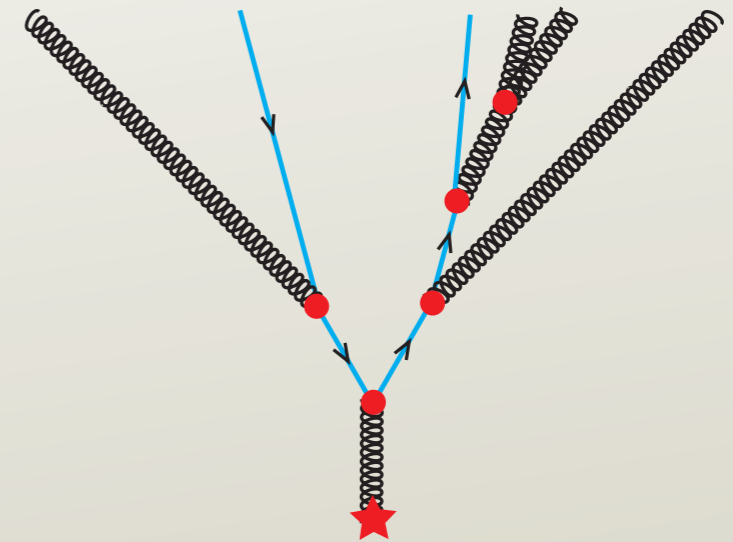
- Emission with $\theta_{12} \gg \theta_{2k}$ is suppressed.
- Emission between partons 2 and k is enhanced.

An application of this



After $H \rightarrow b + \bar{b}$

Soft gluons between b and \bar{b}



After $g \rightarrow b + \bar{b}$

Soft gluons away from b and \bar{b}

- Cf. “pull” (Gallicchio & Schwartz).

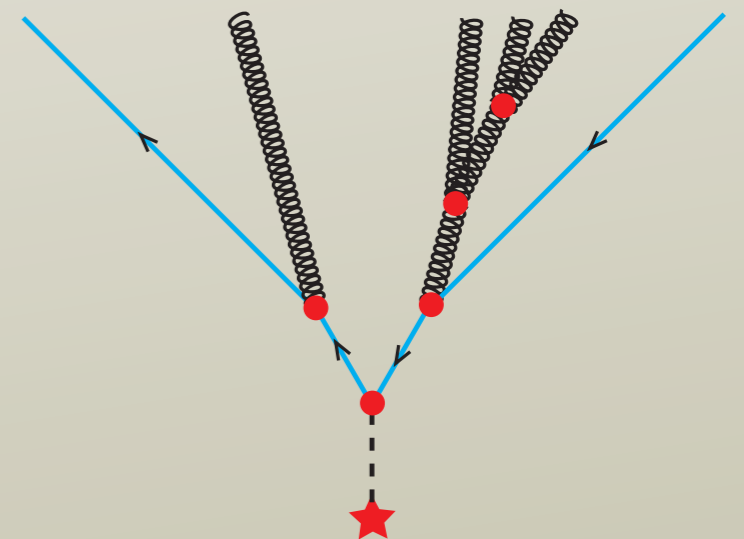
Gluons want to be soft

- Large angles \implies small z :

$$z(1 - z) = \frac{v}{\theta^2} \frac{Q_0^2}{(p_1 + p_2) \cdot Q_0}$$

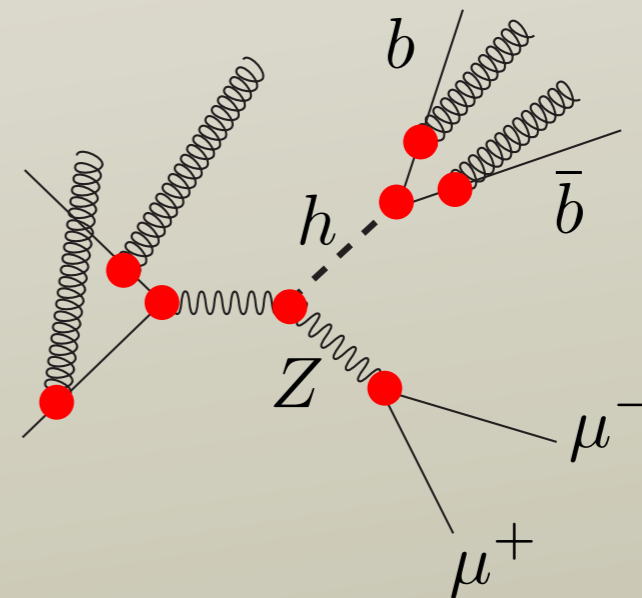
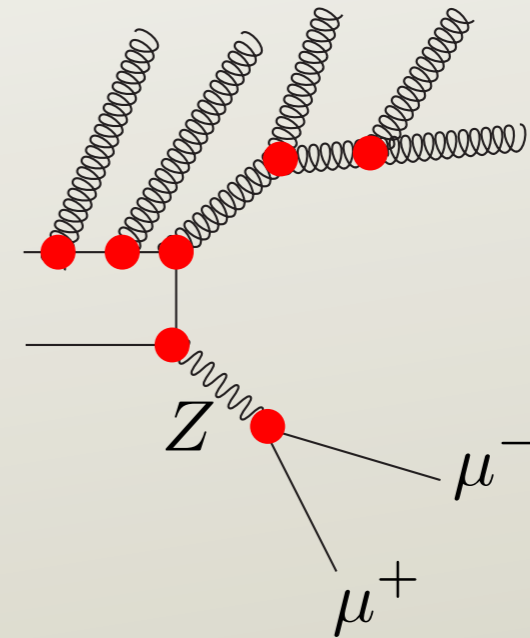
- So we expect lots of soft gluon radiation.

- However, soft gluon radiation is limited by “angular ordering” from $g(\theta)$.



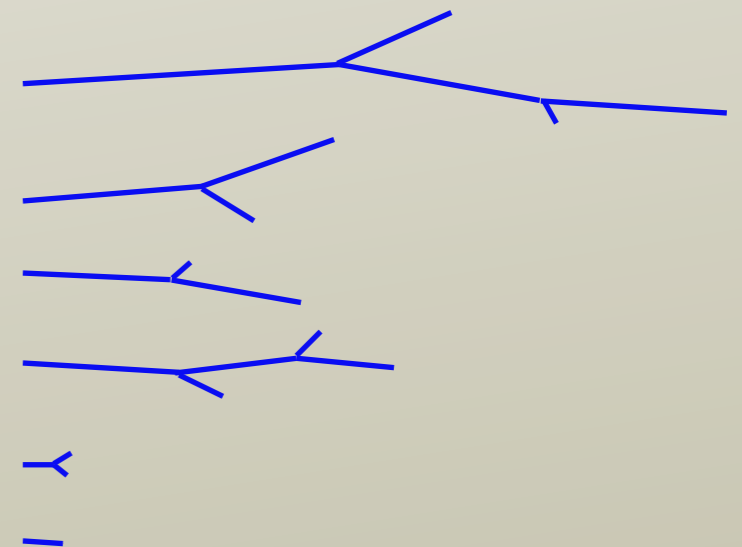
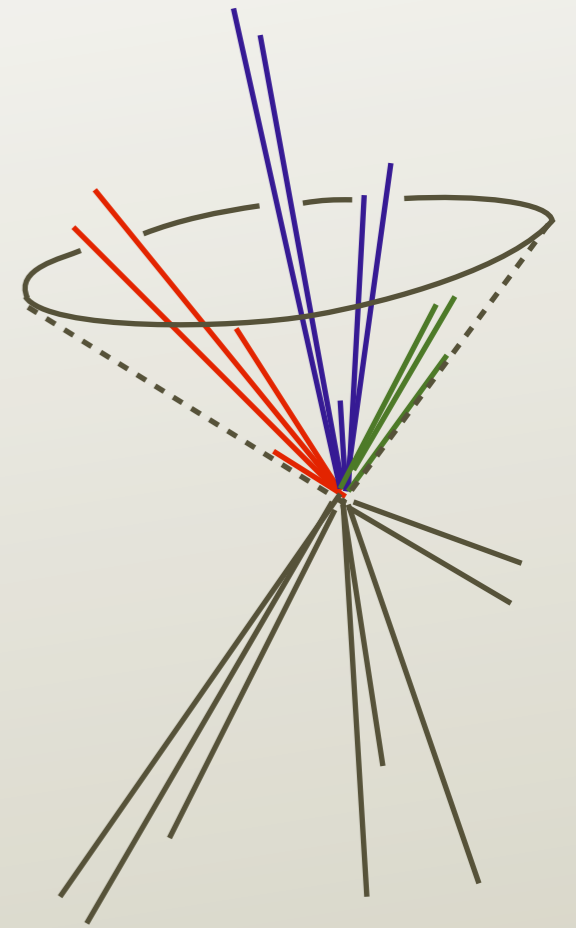
More soft gluons come from initial state radiation

- There is initial state radiation in both signal and background events.
- It can come at central rapidities.
- It is largely rather low transverse momentum.



An application

- Look at all of the hadrons or calorimeter clusters in an angular region that might contain a boosted heavy particle.
- The k_T jet algorithm can put the starting clusters together into jets in something like a shower history.
- Use a fairly small angular size parameter.
- The smallest P_T jets are likely from initial state radiation.
- Throw them out. (Krohn, Thaler & Wang).



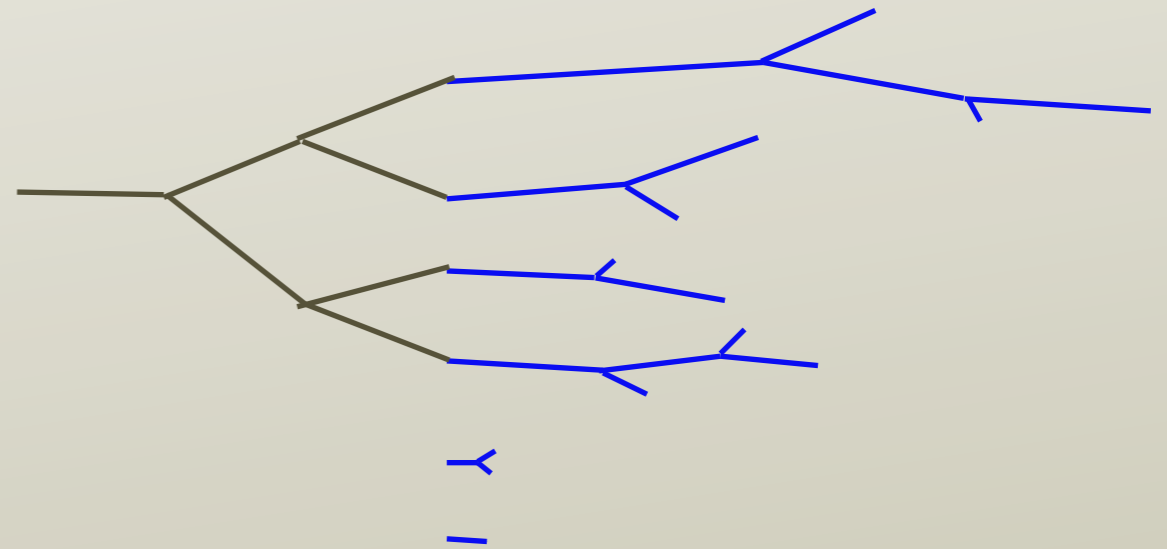
Another application

- It's hard to tell where soft gluons belong, so try to get rid of them.
- For instance, “pruning” joins protojets starting at small angular separations. But if

$$z = \frac{\min(p_{T,i}, p_{T,j})}{|\vec{p}_{T,i} + \vec{p}_{T,j}|}$$

is too small, one throws the softer protojet away.

(Ellis, Vermilion & Walsh)



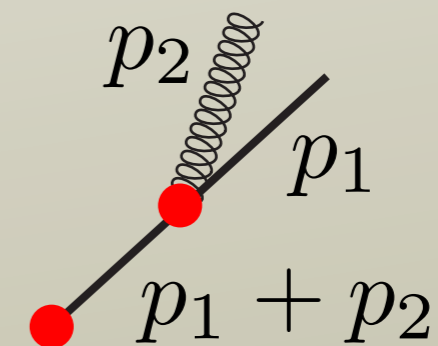
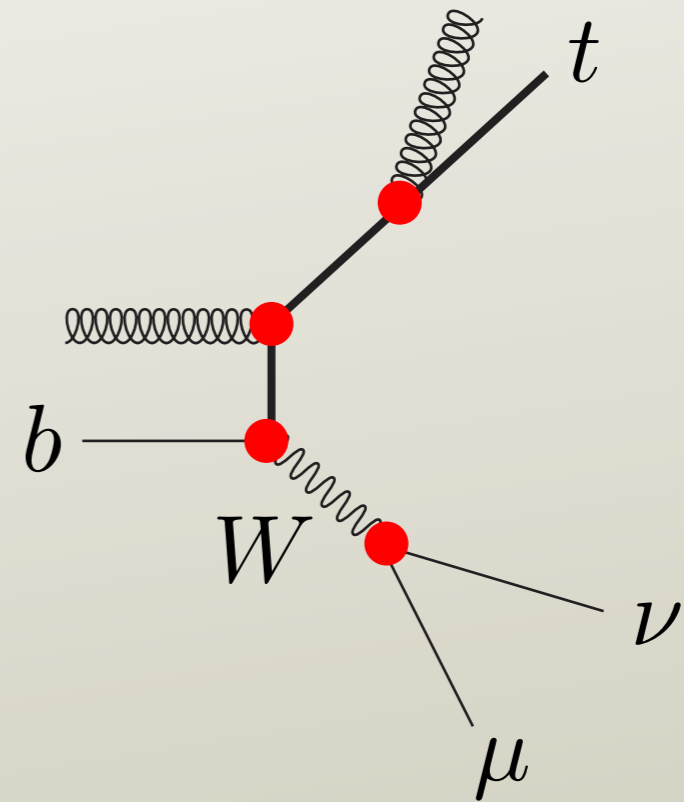
Heavy particles with color

- A heavy particle with color will radiate gluons.
- There is singularity in $|\mathcal{M}|^2$.

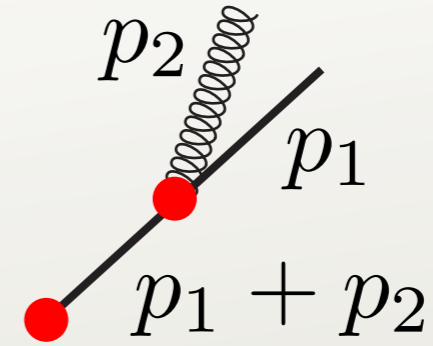
$$dn \propto \frac{dv}{v} \alpha_s \log(\theta_{\min}/\theta_{\max})$$

where the hardness v is now

$$v = \frac{(p_1 + p_2)^2 - M^2}{(p_1 + p_2) \cdot Q_0}$$



- The collinear singularity is cut off:

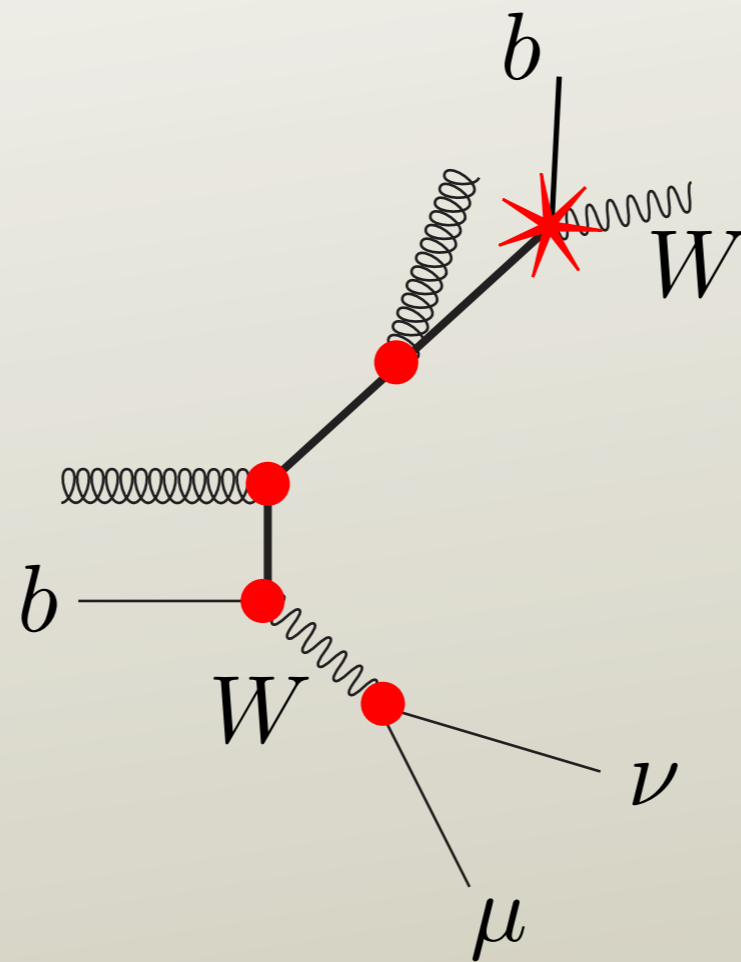


$$\theta_{\min}^2 \sim \min \left(\frac{M^2 Q_0^2}{((p_1 + p_2) \cdot Q_0)^2}, v \frac{4Q_0^2}{(p_1 + p_2) \cdot Q_0} \right)$$

- There are no emissions that take longer than the particle lifetime:

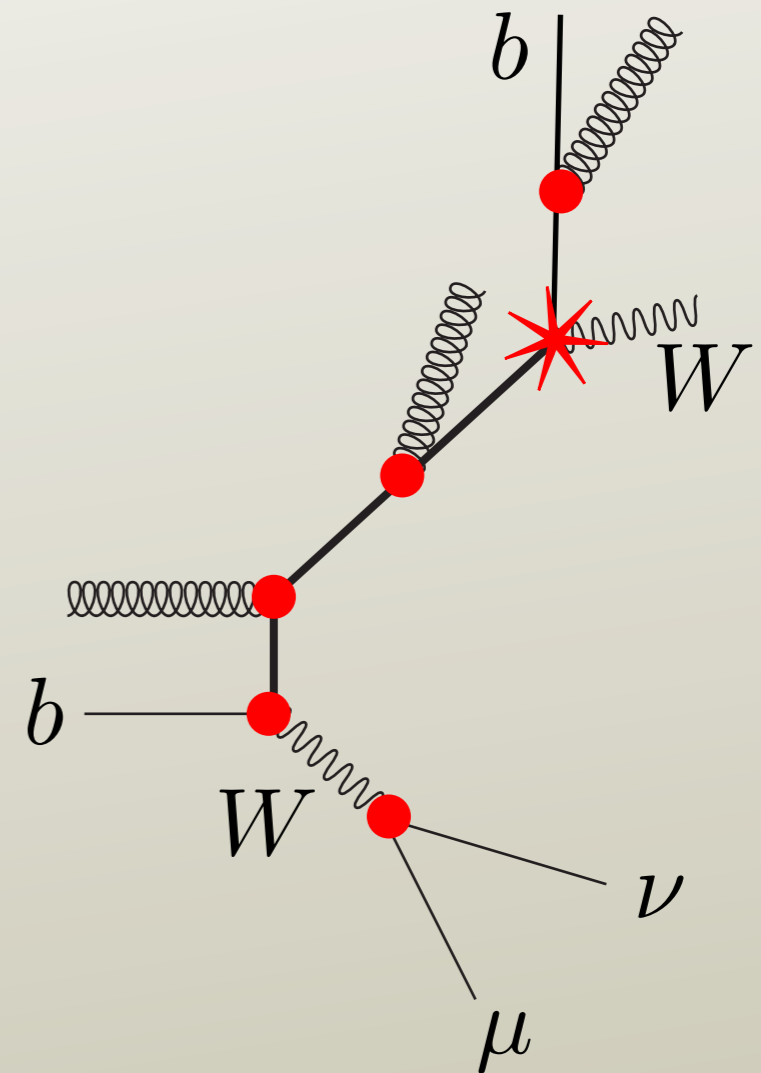
$$v > \frac{M\Gamma}{(p_1 + p_2) \cdot Q_0}$$

Heavy particles decay



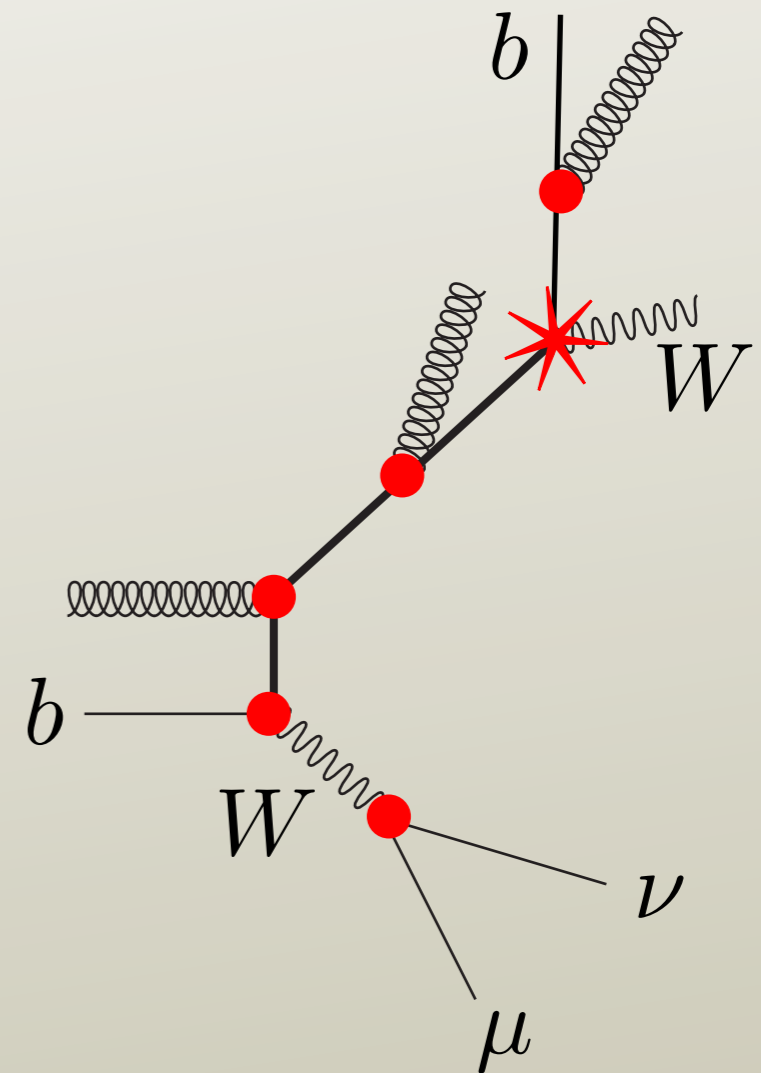
Daughters radiate

- In $t \rightarrow b + W$, a lot of energy is released.
- Color charge is accelerated.
- Gluons are radiated.
- The first radiation is from a color dipole of
 - The final state b -quark;
 - The “initial state” t -quark;



Where does the radiation go?

- The first radiation is from a color dipole of
 - The final state b -quark;
 - The “initial state” t -quark;
- Direction of g is likely collinear with the b .
- Direction of g is likely within angle $M/|\vec{P}_t|$ of the top.
- If the top is highly boosted, this is a narrow cone.



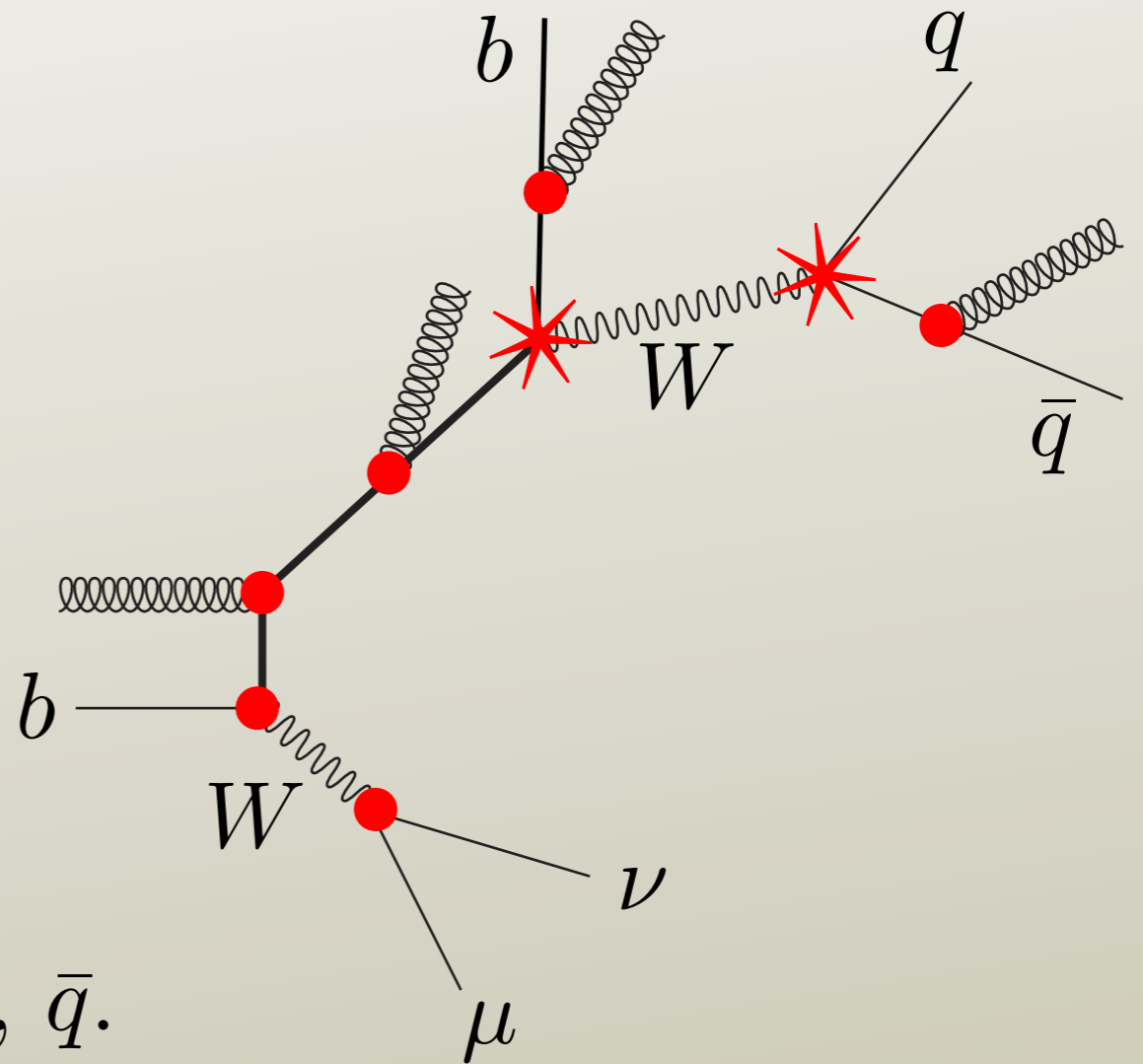
Daughters radiate

- In $W \rightarrow q + \bar{q}$, a lot of energy is released.

- Color charge is accelerated.

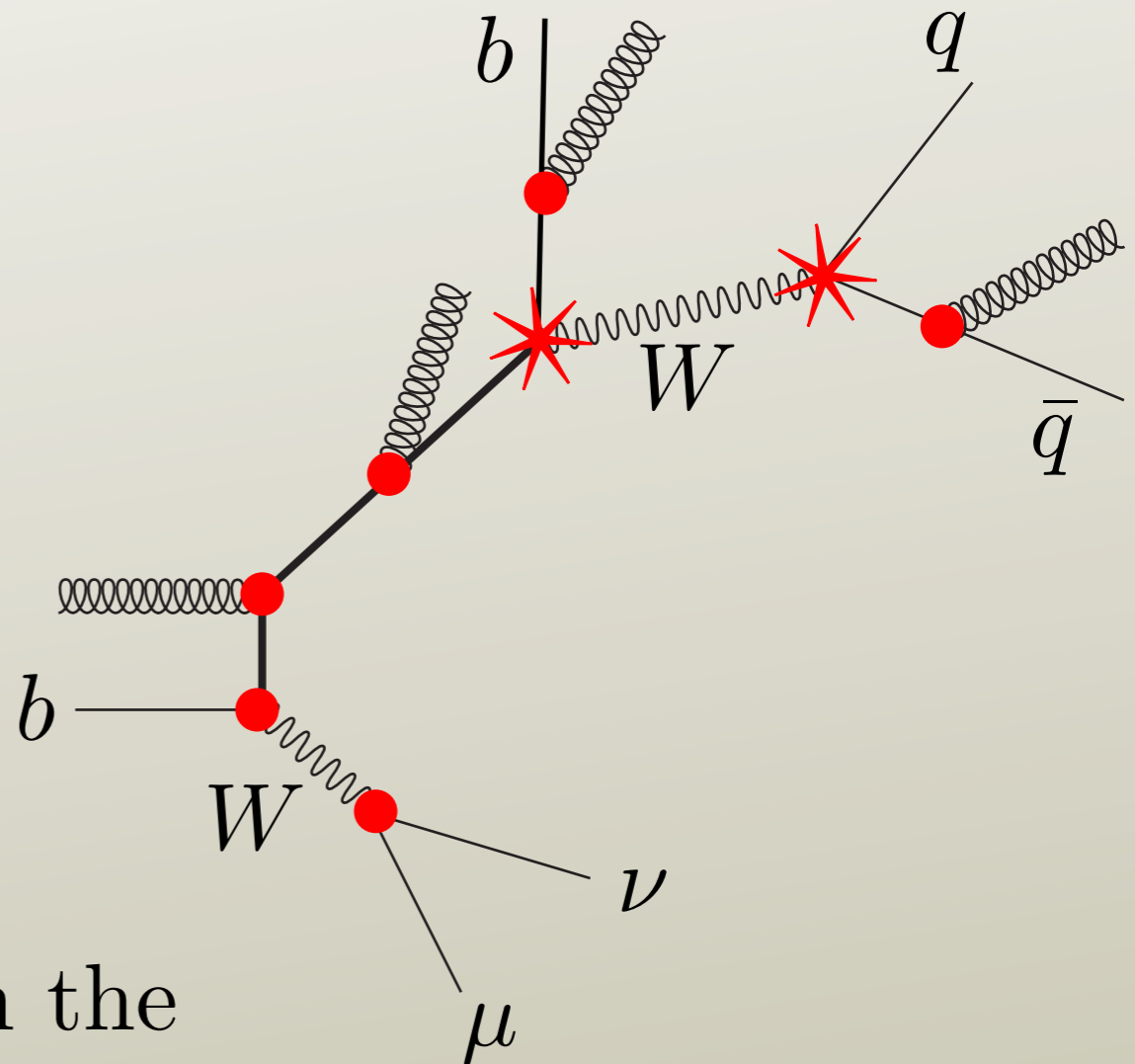
- Gluons are radiated.

- The first radiation is from a color dipole of
 - The final state quark, q ;
 - The final state anti-quark, \bar{q} .



Where does the radiation go?

- The first radiation is from a color dipole of
 - The final state quark, q ;
 - The final state anti-quark, \bar{q} .
- Direction of g is likely collinear with the q or \bar{q} .
- In any case, it is likely between the q and \bar{q} .

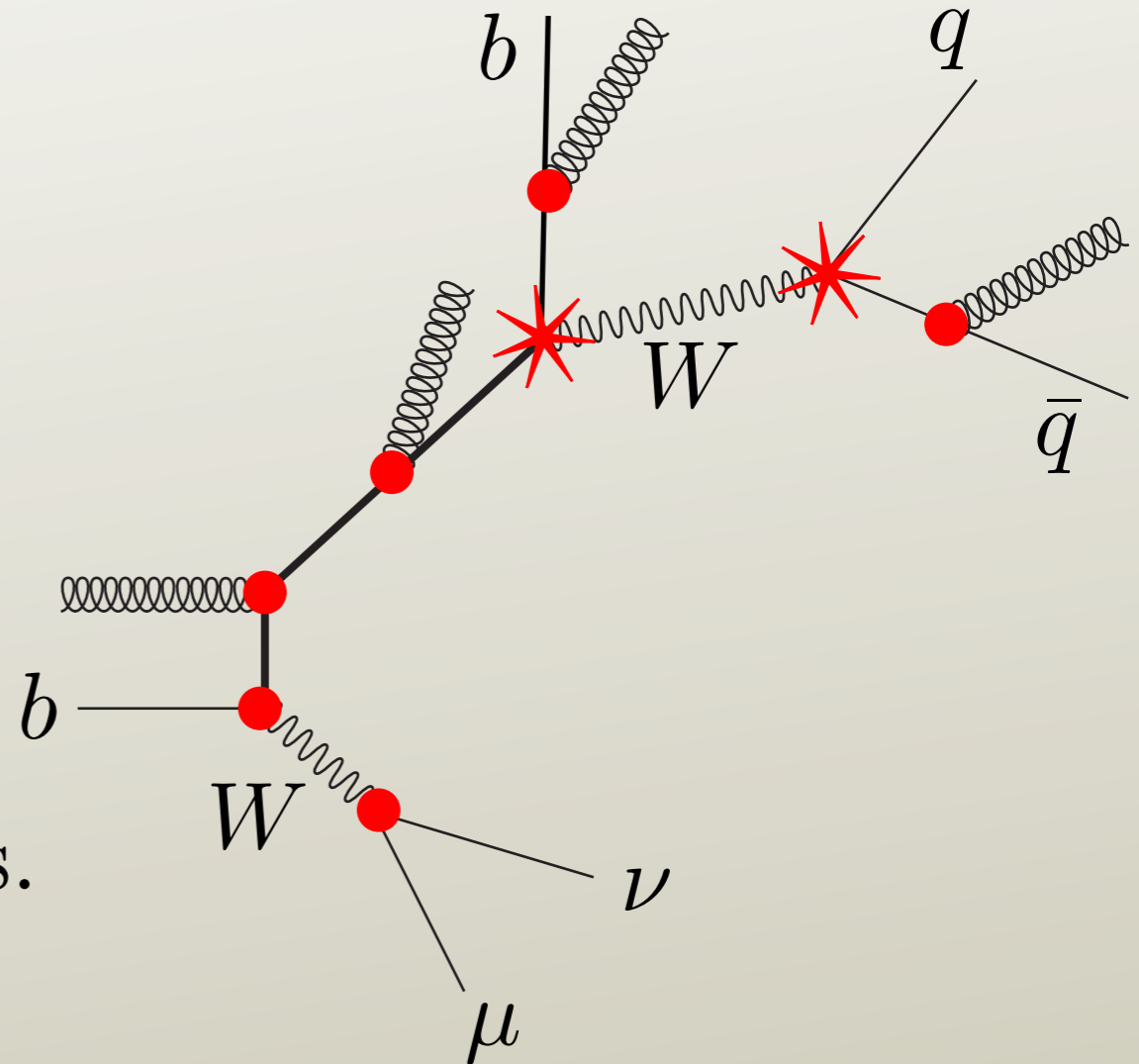


Very soft radiation

- For very soft emissions,

$$v < \frac{M_t \Gamma_t}{p_t \cdot Q_0} \sim \frac{M_W \Gamma_W}{p_W \cdot Q_0}$$

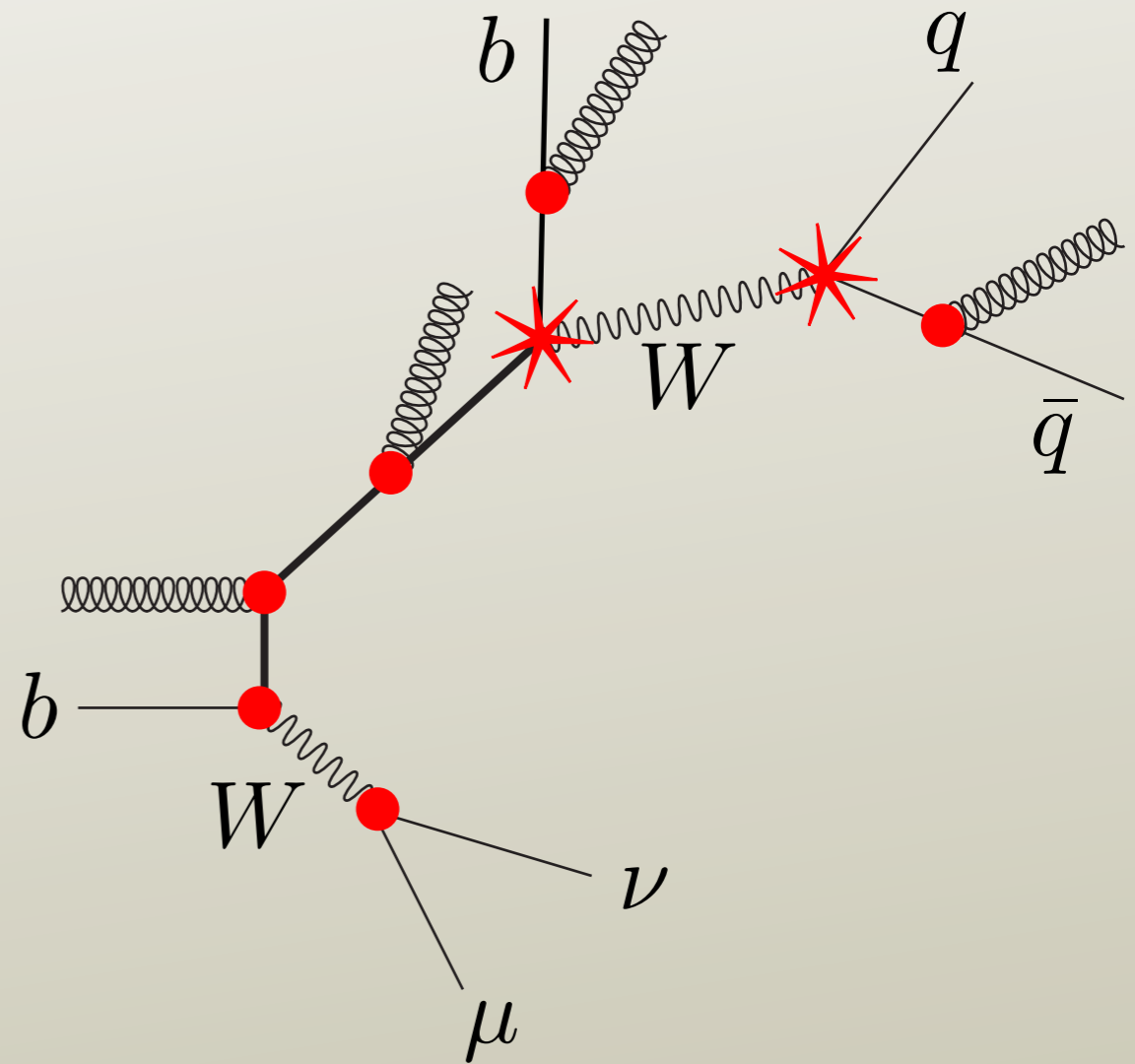
there is quantum interference between emissions from any two (color connected) particles.



- Probably the structure of these emissions is too complicated to be useful for separating signal from background.

Comments

- Since we know something about where the collinear or soft radiation goes in a heavy particle decay, sequential heavy particle decays should have good signatures.
- We do have the problem of contamination from initial state radiation.
- Having highly boosted heavy objects helps with this.



Summary

- With a model for sequential heavy particle decays and knowledge of the structure of radiation in gauge theories, one can build filters for separating background events from signal events.

